

# Flow Visualization



## ■ Introduction, overview

- ◆ Flow data
- ◆ Simulation vs. measurement vs. modelling
- ◆ 2D vs. surfaces vs. 3D
- ◆ Steady vs time-dependent flow
- ◆ Direct vs. indirect flow visualization

## ■ Experimental flow visualization

- ◆ Basic possibilities
- ◆ PIV (Particle Image Velocimetry) + Example



# Overview: Flow Visualization (2)

- Visualization of models
- Flow visualization with arrows
- Numerical integration
  - ◆ Euler-integration
  - ◆ Runge-Kutta-integration
- Streamlines
  - ◆ In 2D
  - ◆ Particle paths
  - ◆ In 3D, sweeps
  - ◆ Illuminated streamlines
- Streamline placement



- Flow visualization with integral objects
  - ◆ Streamribbons,
  - ◆ Streamsurfaces, stream arrows
- Line integral convolution
  - ◆ Algorithm
  - ◆ Examples, alternatives
- Glyphs & icons, flow topology



## ■ Introduction:

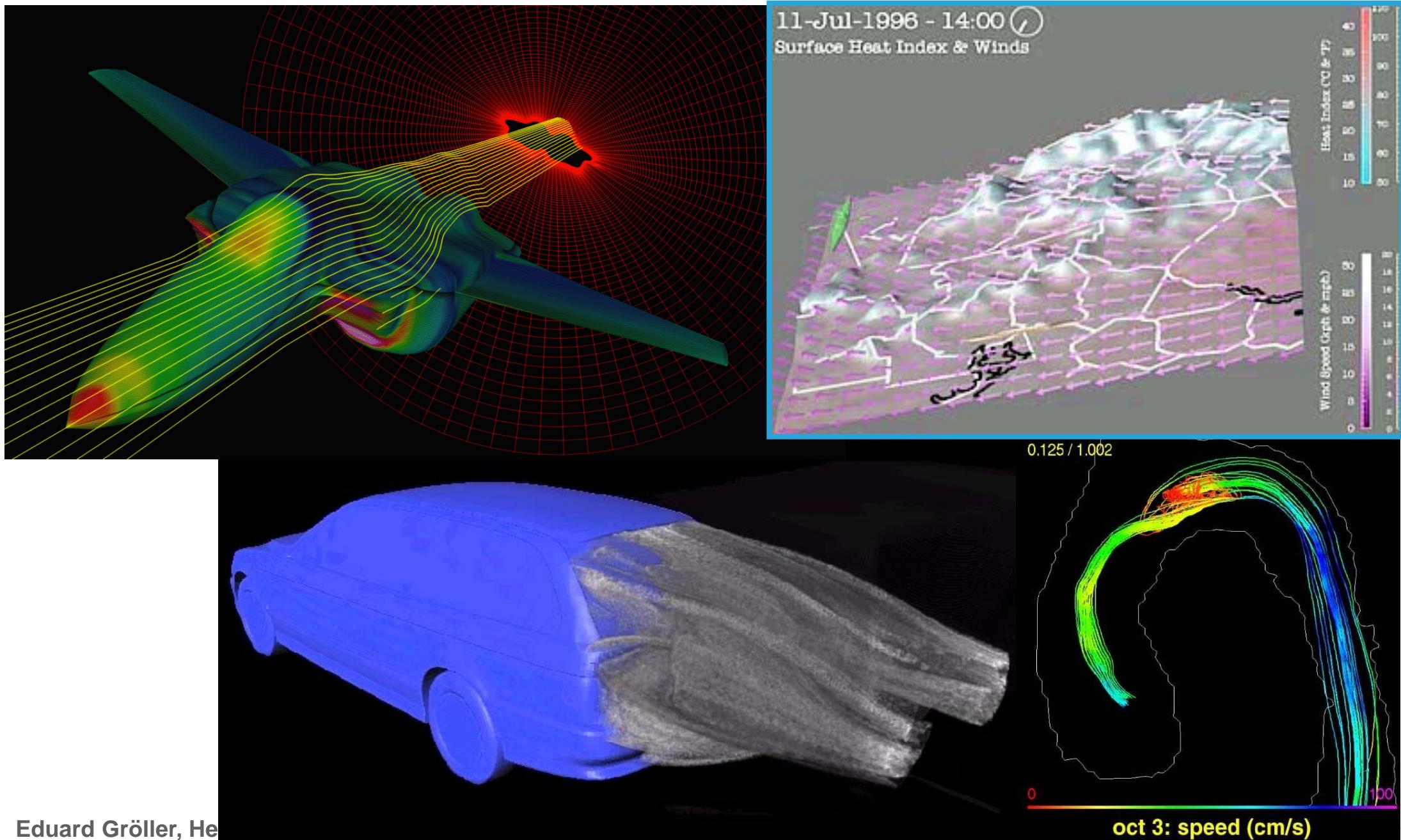
- ◆ FlowVis = visualization of flows
  - Visualization of change information
  - Typically: more than 3 data dimensions
  - General overview: even more difficult
- ◆ Flow data:
  - $nD \times nD$  data,  $1D^2 / 2D^2 / nD^2$  (models),  $2D^2 / 3D^2$  (simulations, measurements)
  - Vector data ( $nD$ ) in  $nD$  data space
- ◆ User goals:
  - Overview vs. details (with context)



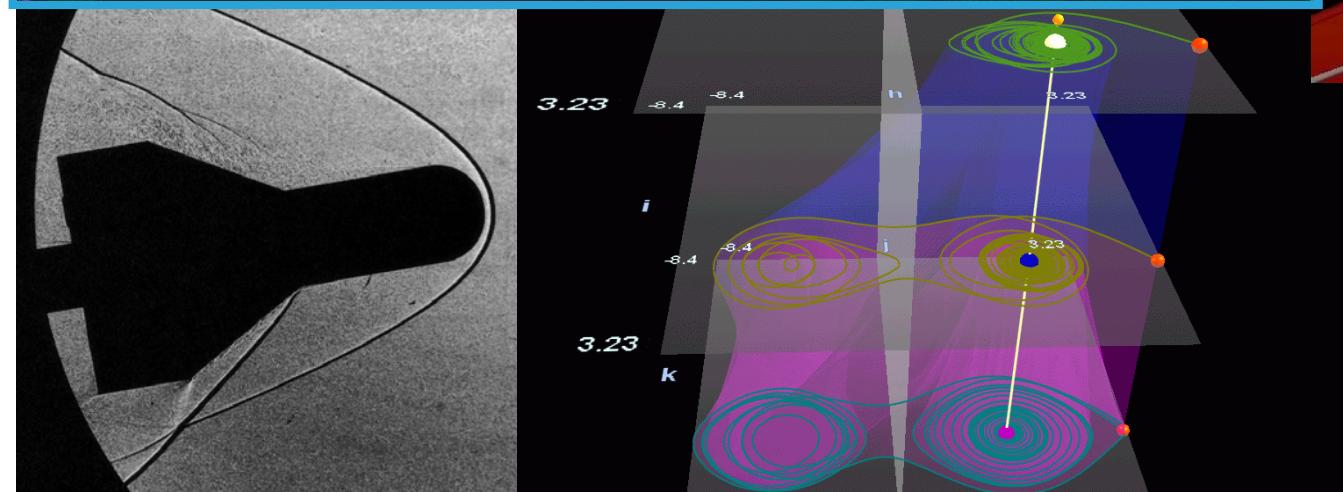
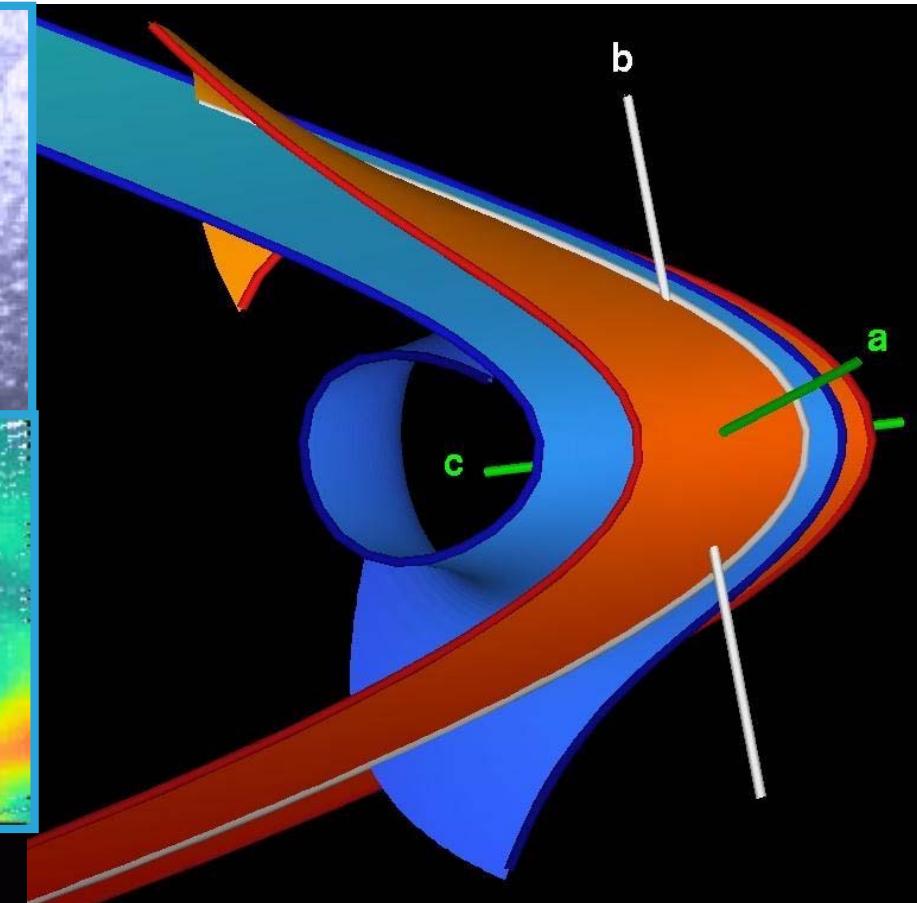
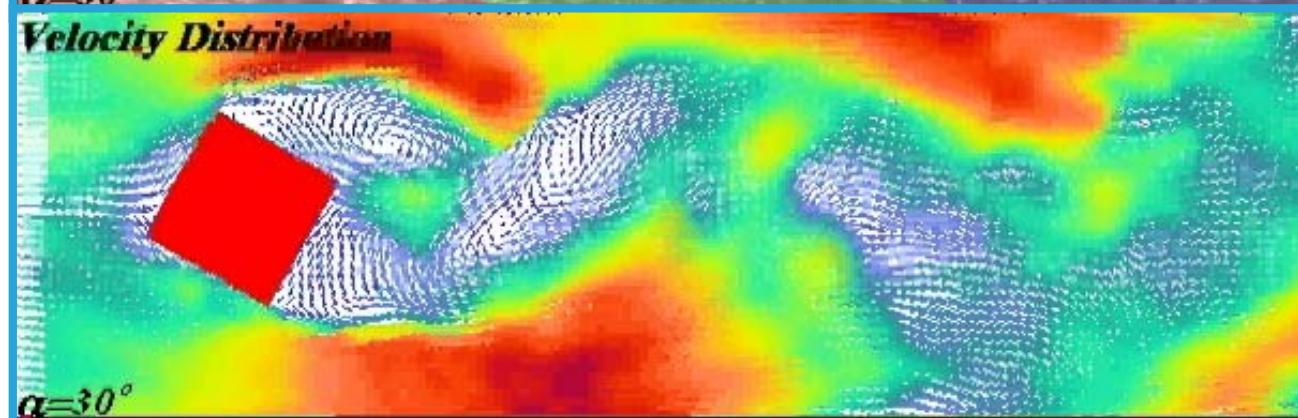
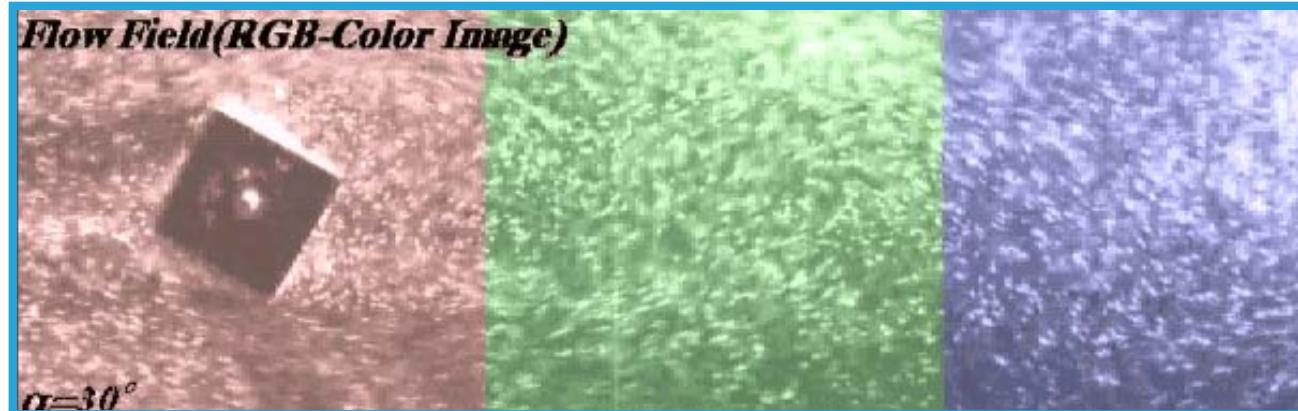
- Where do the data come from:
  - ◆ Flow simulation:
    - Airplane- / ship- / car-design
    - Weather simulation (air-, sea-flows)
    - Medicine (blood flows, etc.)
  - ◆ Flow measurements:
    - Wind tunnel, fluid tunnel
    - Schlieren-, shadow-technique
  - ◆ Flow models:
    - Differential equation systems (ODE)  
(dynamical systems)



# Data Source – Examples 1/2



# Data Source – Examples 2/2

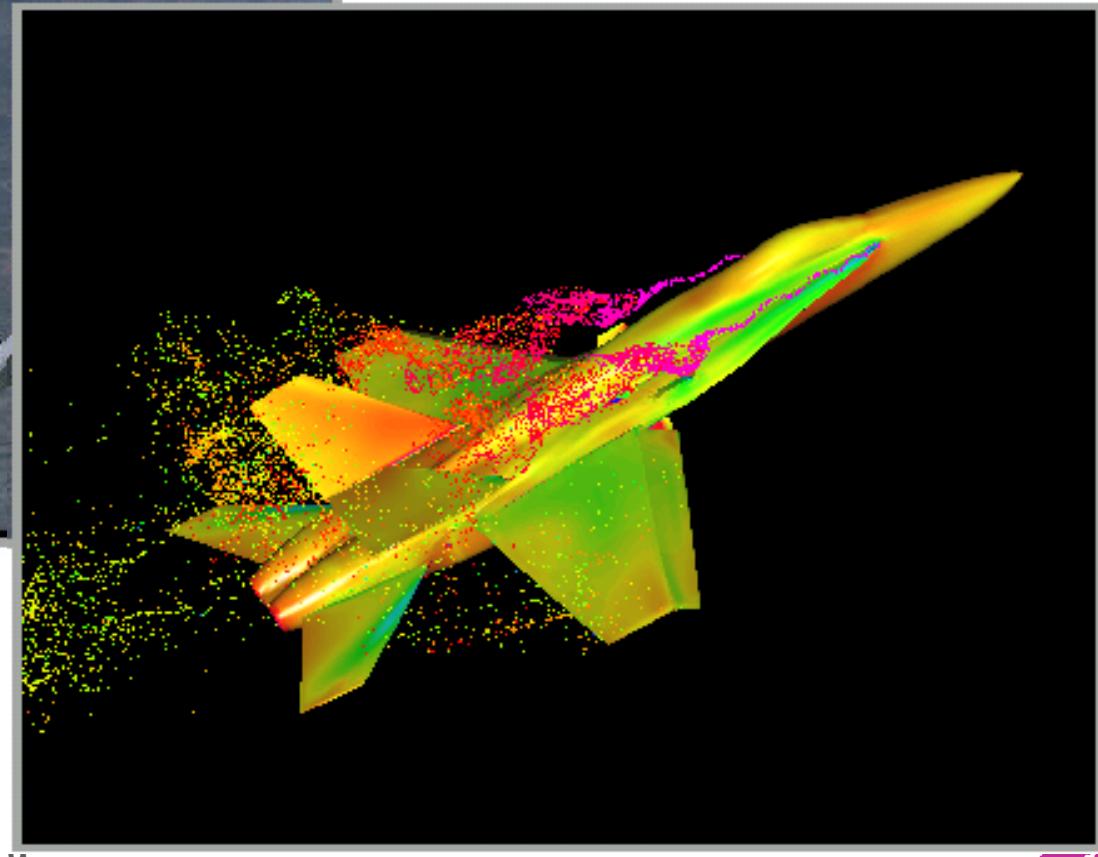


# Comparison with Reality



Experiment

Simulation



## ■ 2D-Flow visualization

- ◆ 2D×2D-Flows
- ◆ Models, slice flows (2D out of 3D)

## ■ Visualization of surface flows

- ◆ 3D-flows around “obstacles”
- ◆ Boundary flows on surfaces (2D)

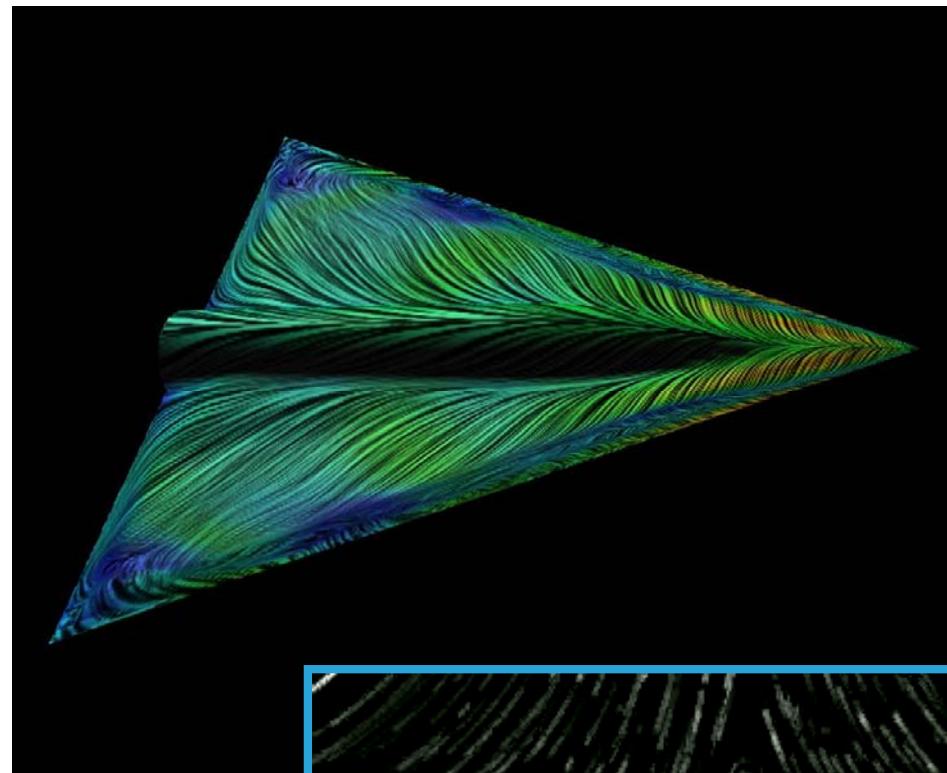
## ■ 3D-Flow visualization

- ◆ 3D×3D-flows
- ◆ Simulations, 3D-models



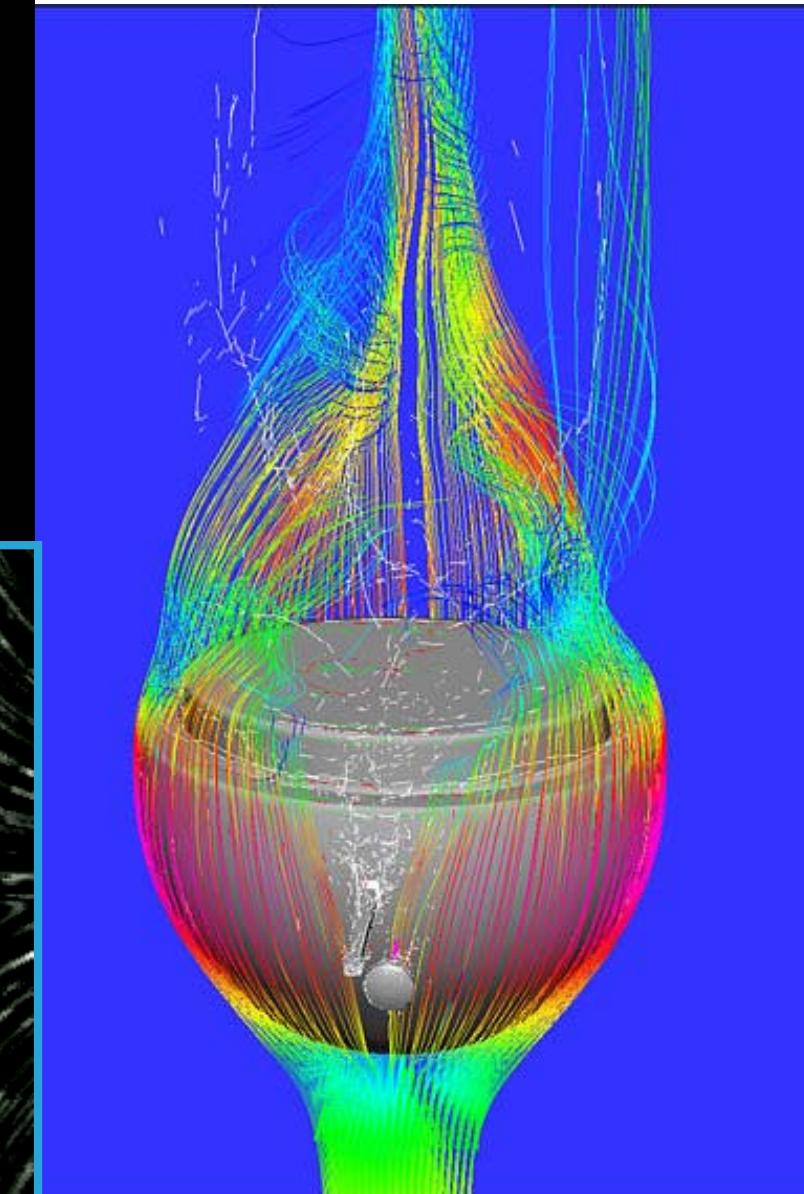
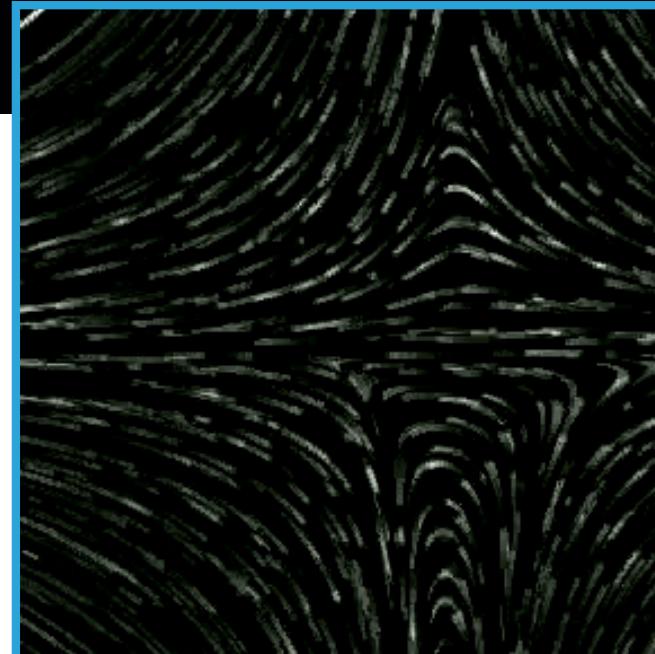
# 2D/Surfaces/3D – Examples

Surface



2D

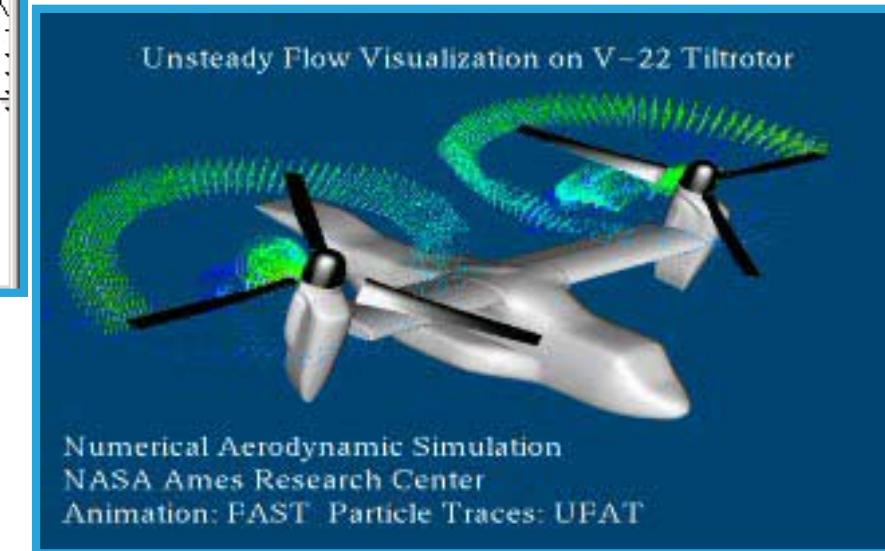
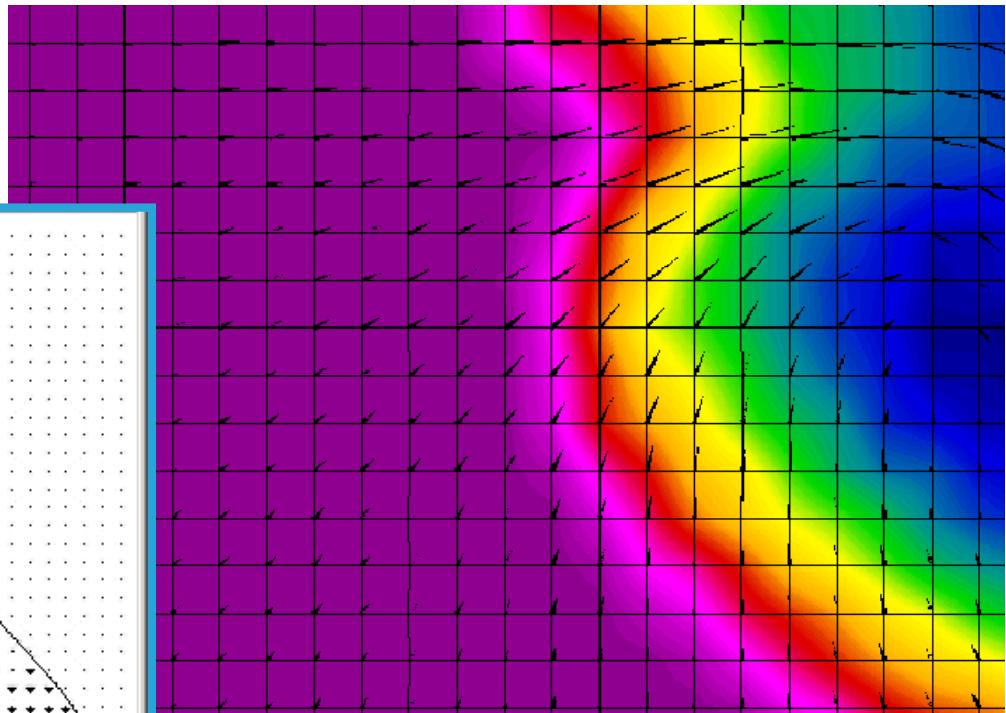
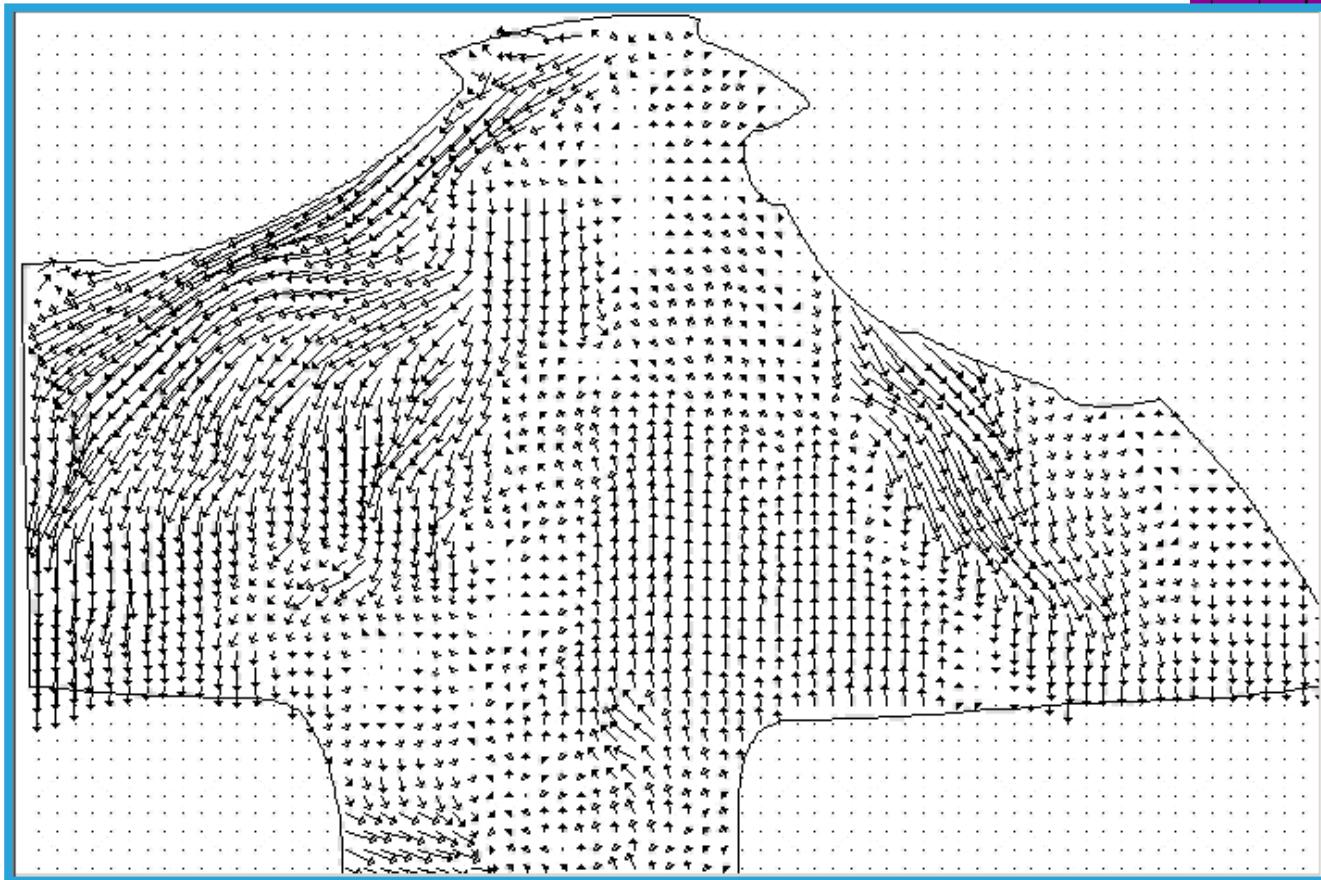
3D



- Steady (time-independent) flows:
  - ◆ Flow static over time
  - ◆  $\mathbf{v}(\mathbf{x}) : \mathbb{R}^n \rightarrow \mathbb{R}^n$ , e.g., laminar flows
  - ◆ Simpler interrelationship
- Time-dependent (unsteady) flows:
  - ◆ Flow itself changes over time
  - ◆  $\mathbf{v}(\mathbf{x}, t) : \mathbb{R}^n \times \mathbb{R}^1 \rightarrow \mathbb{R}^n$ , e.g., turbulent flows
  - ◆ More complex interrelationship



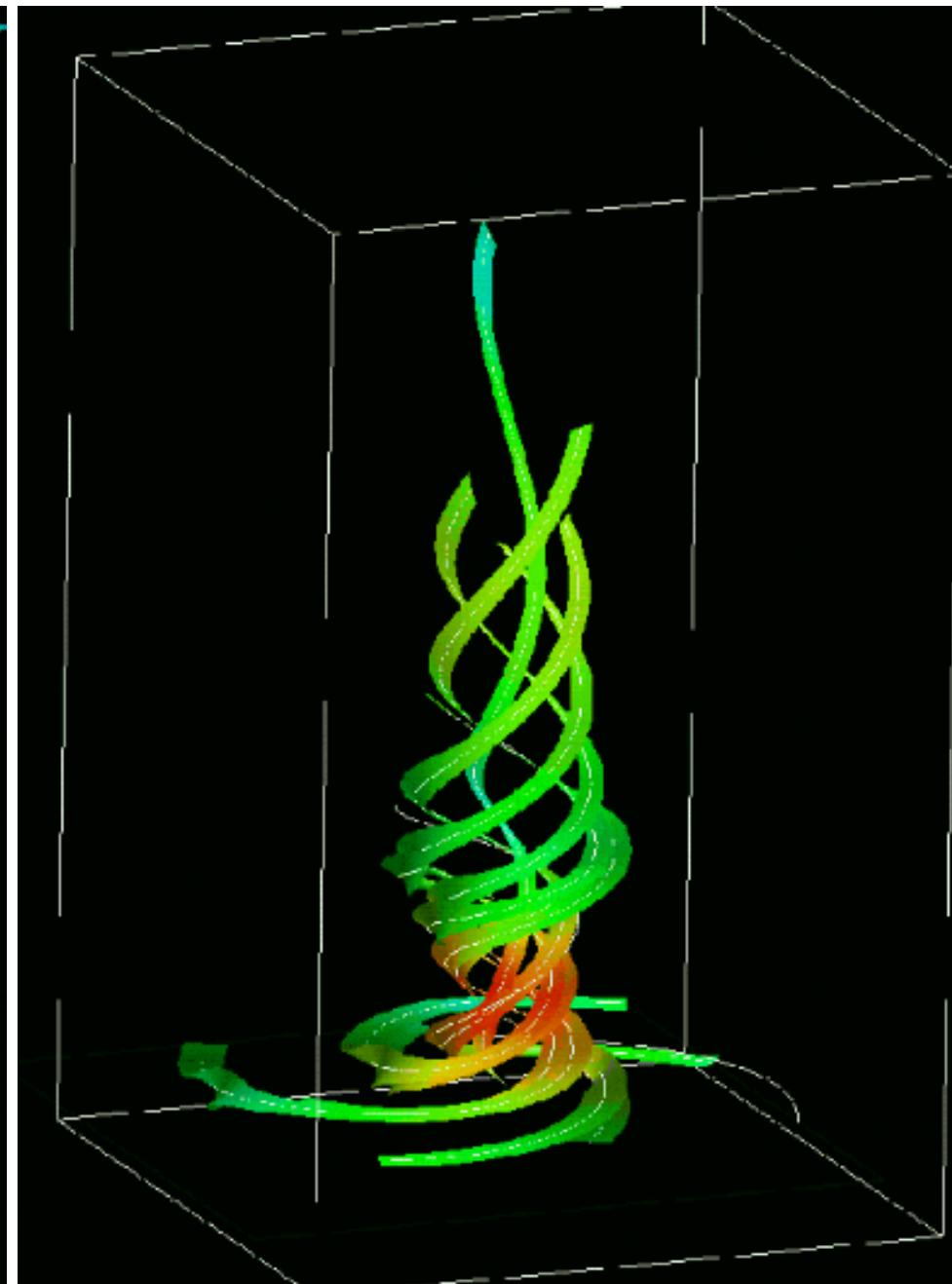
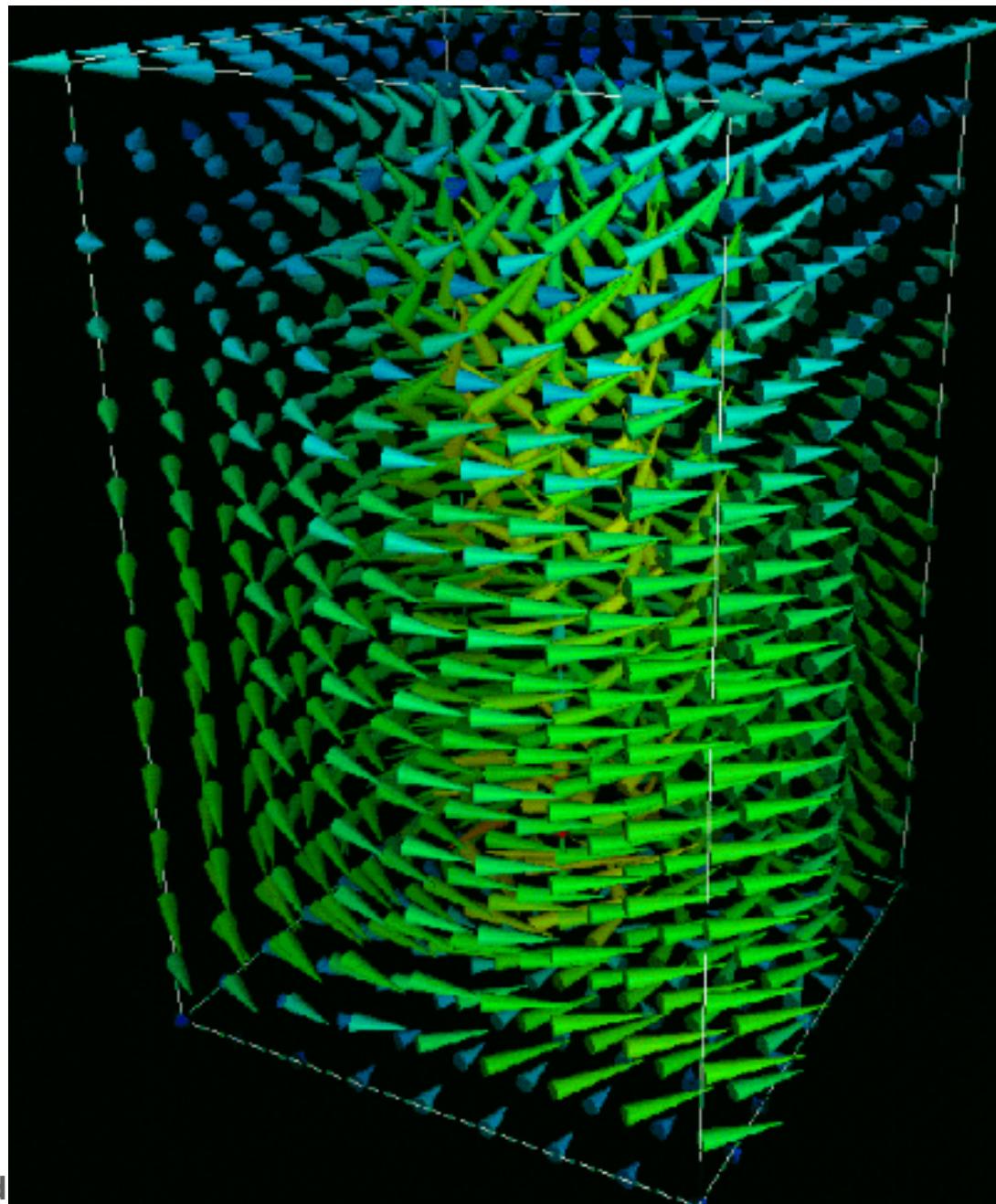
# Time-Dependent vs. Steady Flow



- Direct flow visualization:
  - ◆ Overview on current flow state
  - ◆ Visualization of vectors
  - ◆ Arrow plots, smearing techniques
- Indirect flow visualization:
  - ◆ Usage of intermediate representation:  
vector-field integration over time
  - ◆ Visualization of temporal evolution
  - ◆ Streamlines, streamsurfaces



# Direct vs. Indirect Flow Vis. – Example



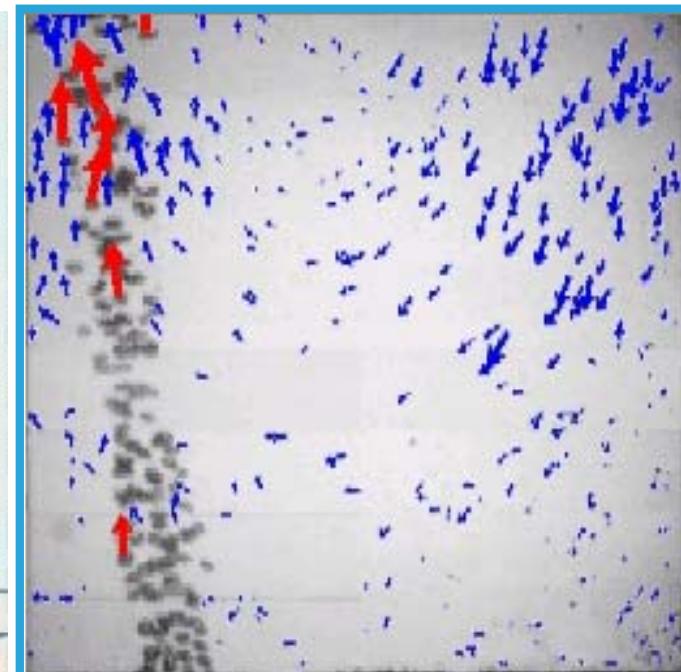
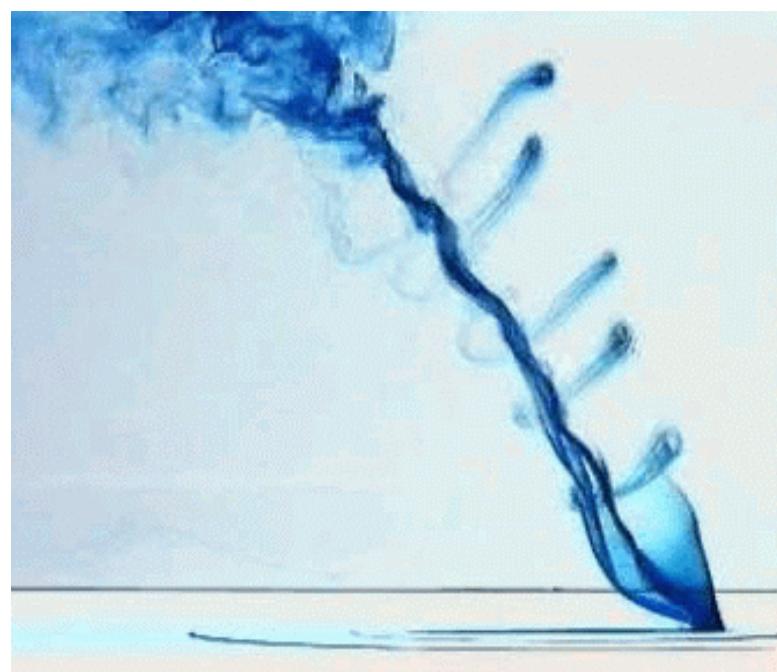
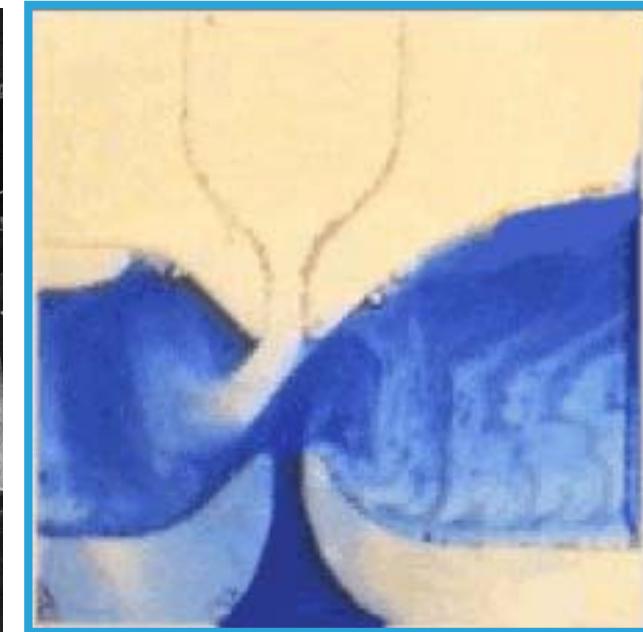
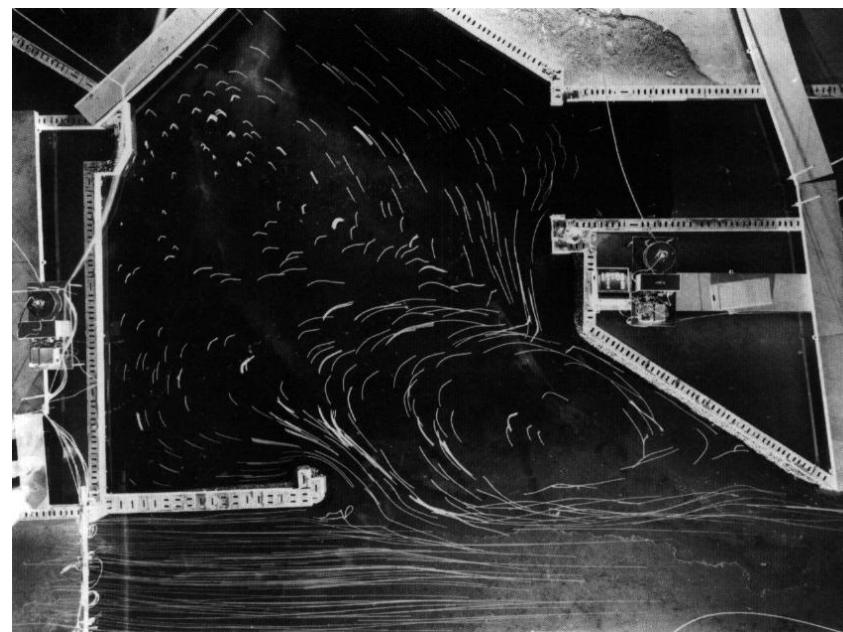
# **Experimental Flow Visualization**

Optical Methods, etc.



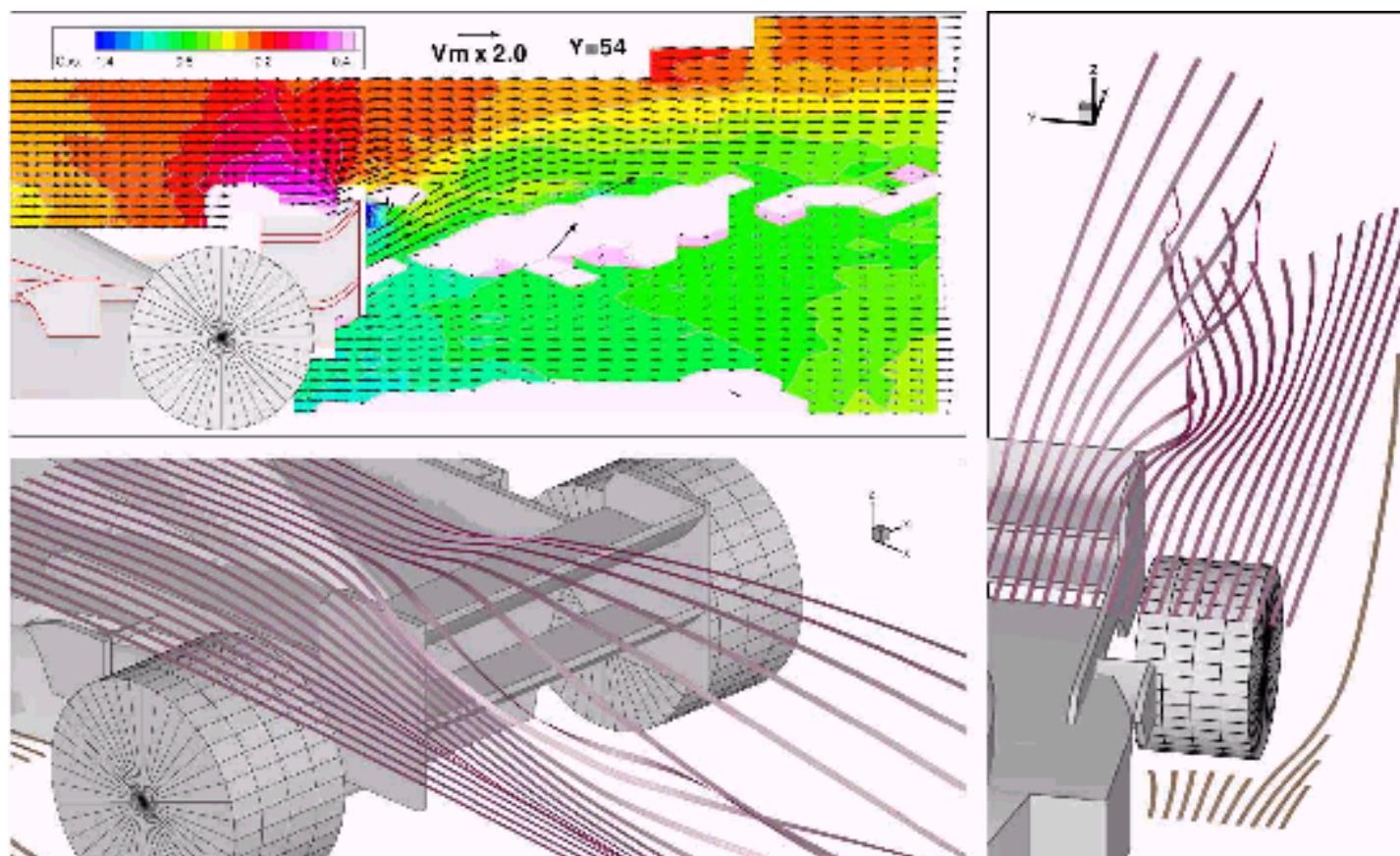
# With Smoke rsp. Color Injection

- Injection of color, smoke, particles
- Optical methods:
  - ◆ Schlieren, shadows



# Example: Car-Design

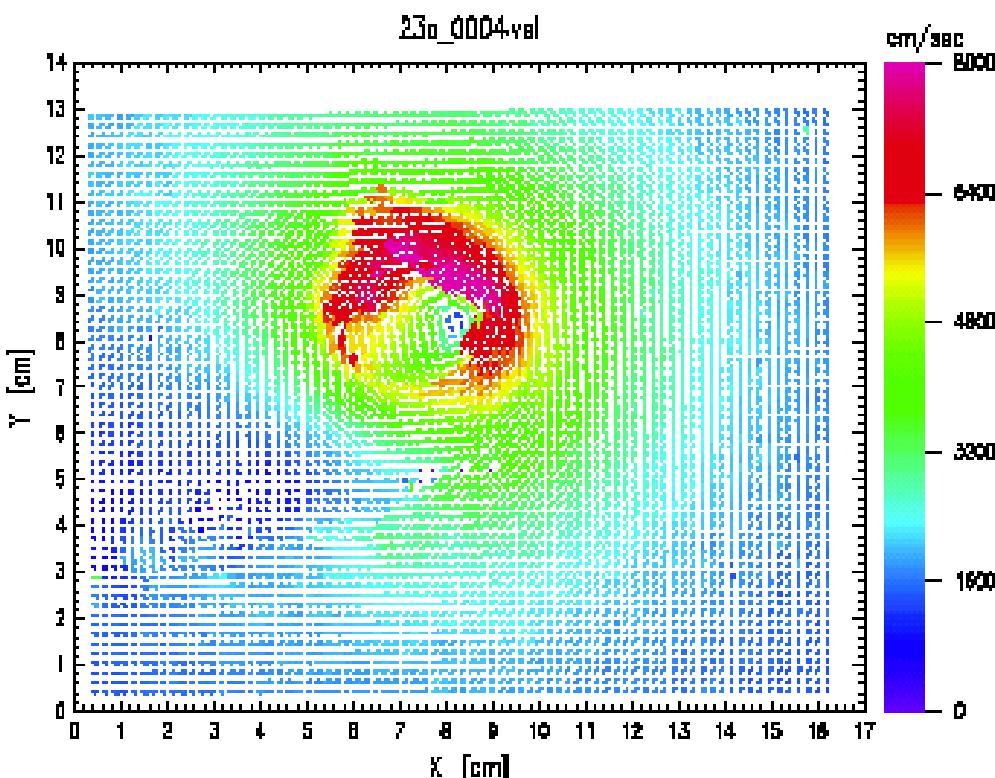
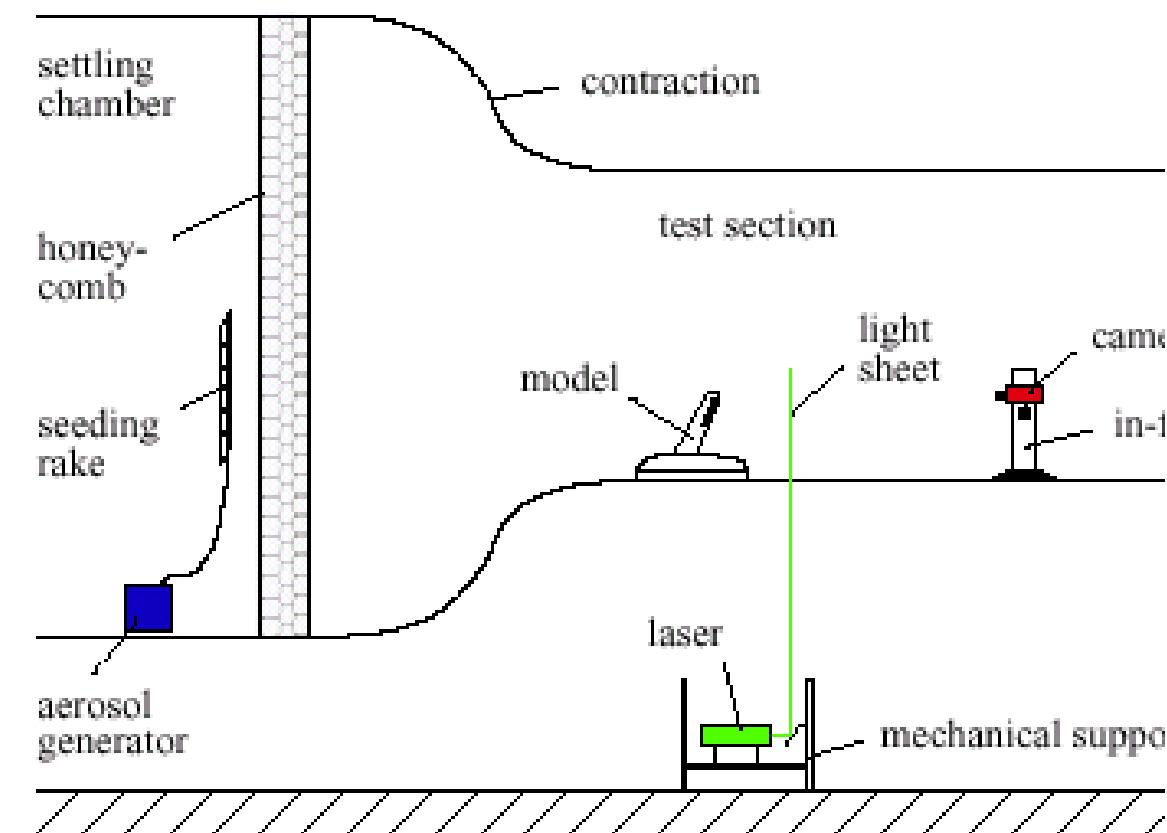
- Ferrari-model,  
so-called five-  
hole probe (no  
back flows)



- Laser + correlation analysis:
  - ◆ Real flow, e.g., in wind tunnel
  - ◆ Injection of particles (as uniform as possible)
  - ◆ At interesting locations:
    - 2-times fast illumination with laser-slice
  - ◆ Image capture (high-speed camera),  
then correlation analysis of particles
  - ◆ Vector calculation / reconstruction,  
typically only 2D-vectors

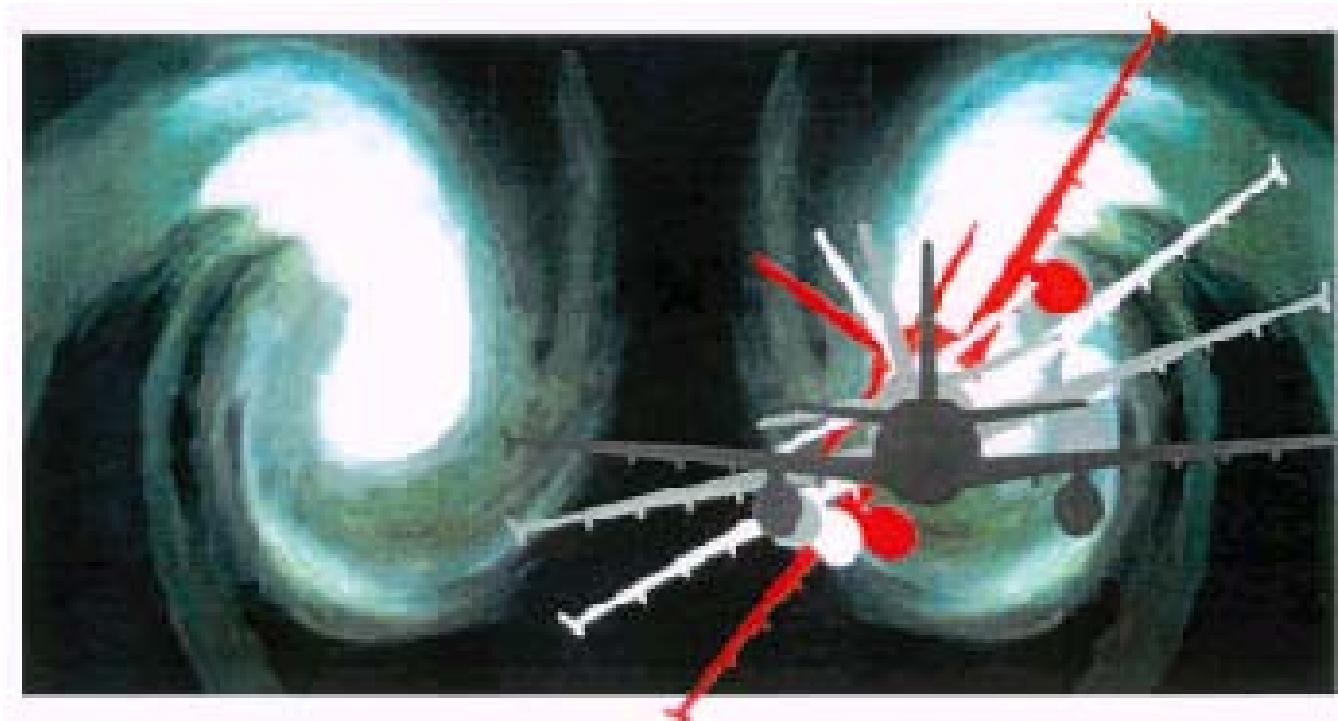
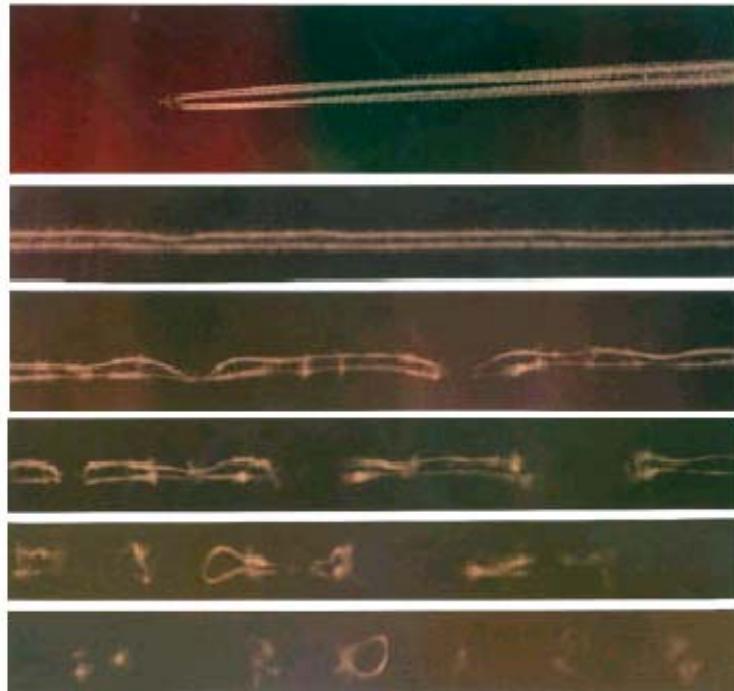


## ■ Setup and typical result:



# Example: Wing-Tip Vortex

- Problem: Air behind airplanes is turbulent



t + 2min



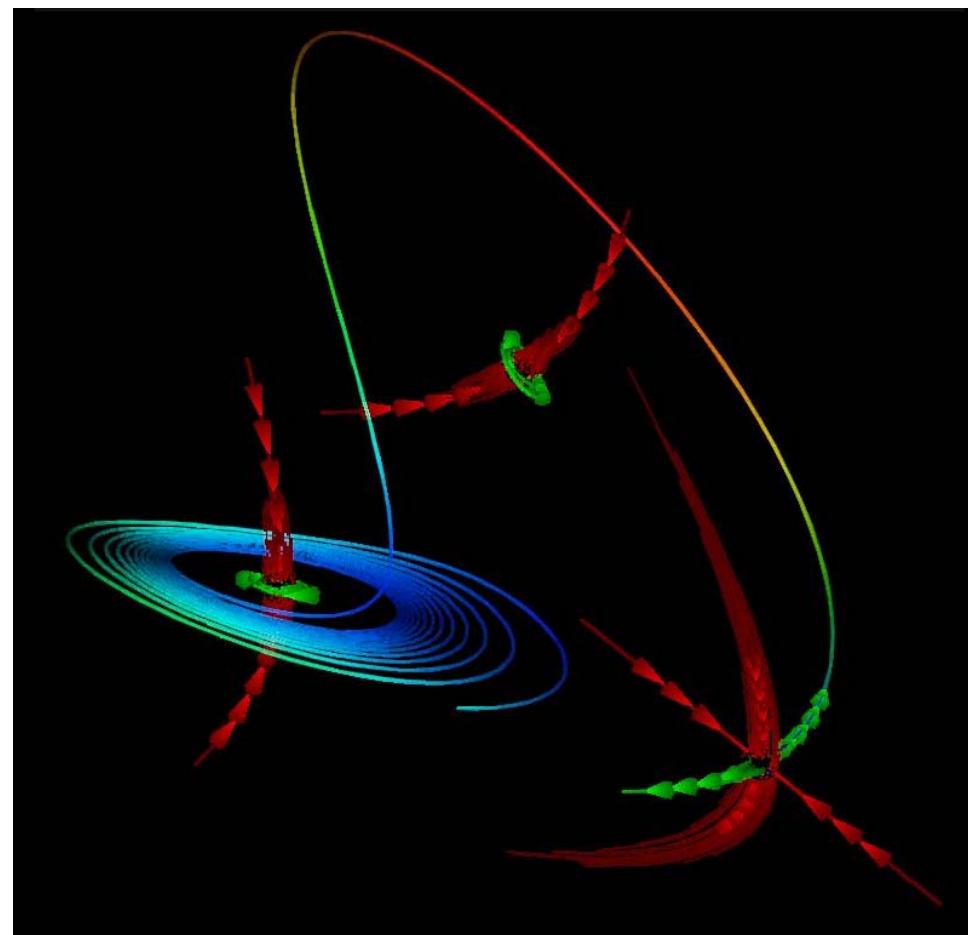
# **Visualization of Models**

**Dynamical Systems**



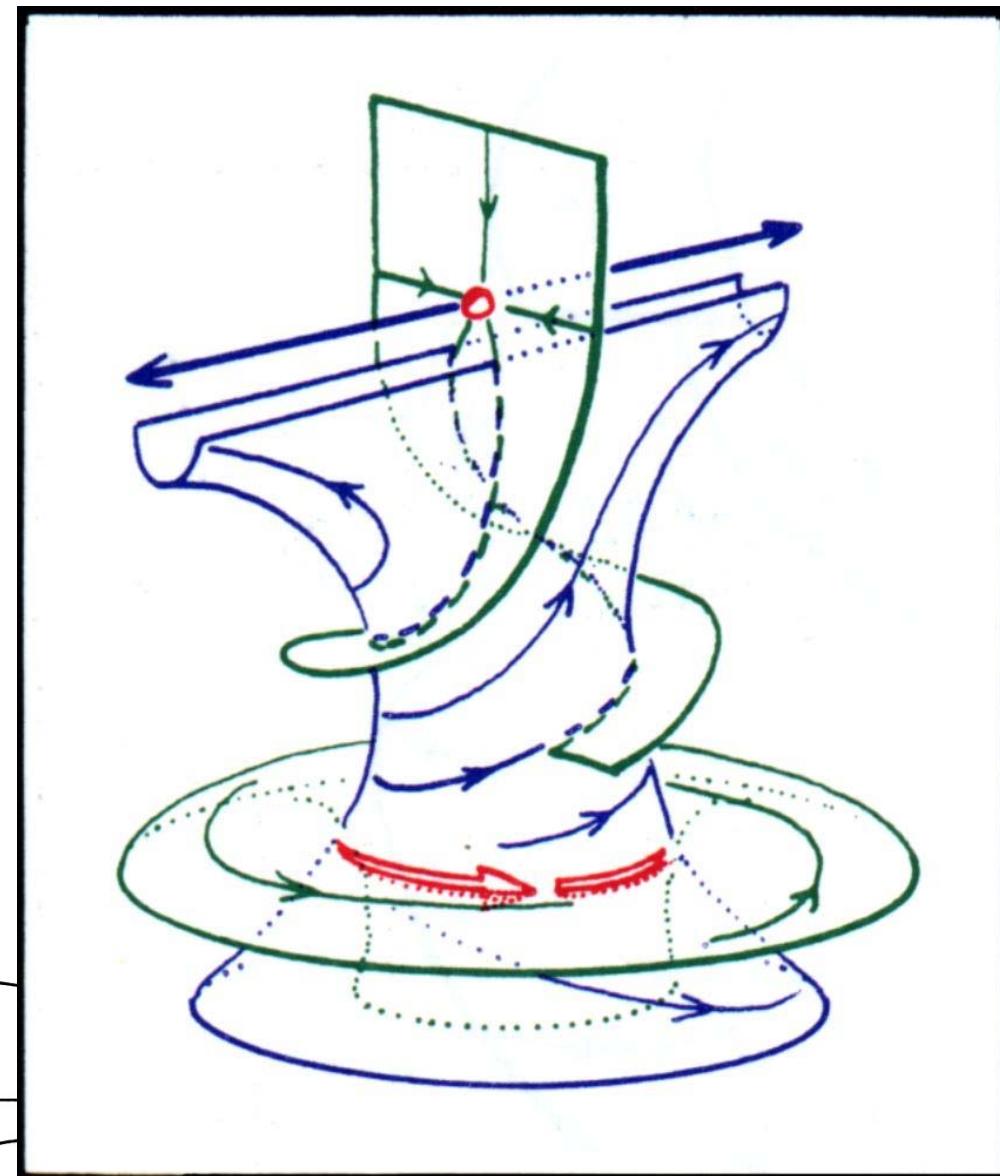
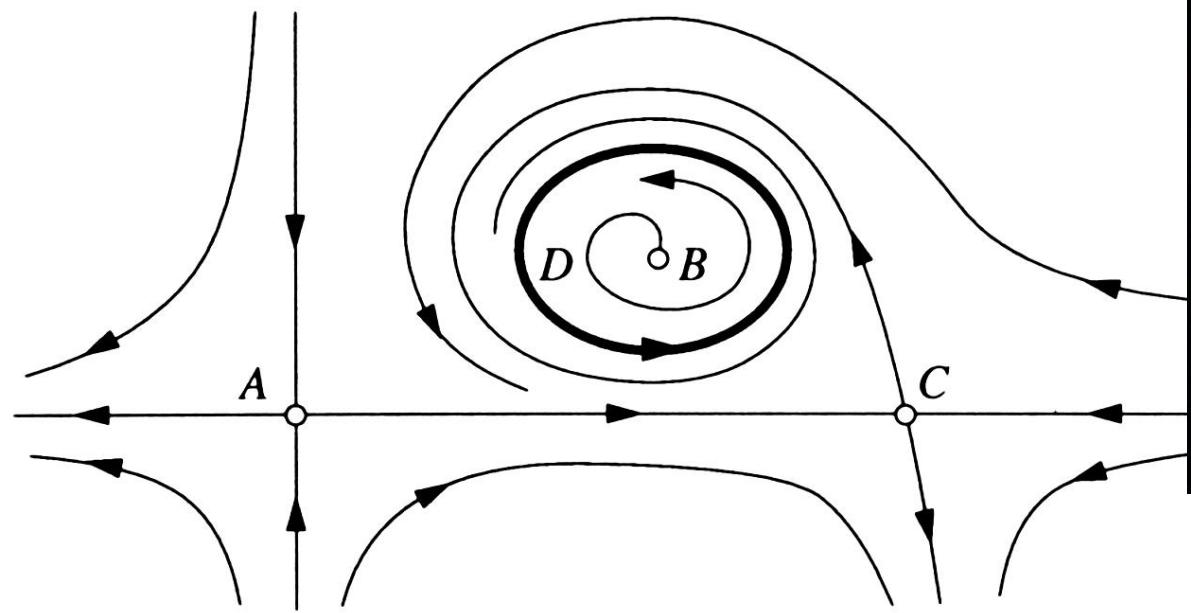
## ■ Differences:

- ◆ Flow analytically def.:  
 $dx/dt = \mathbf{v}(\mathbf{x})$
- ◆ Navier-Stokes equations
- ◆ E.G.: Lorenz-system:  
 $dx/dt = \sigma(y-x)$   
 $dy/dt = rx-y-xz$   
 $dz/dt = xy-bz$
- ◆ Larger variety in data:
  - 2D, 3D, nD
  - Sometimes no natural constraints like non-compressibility or similar

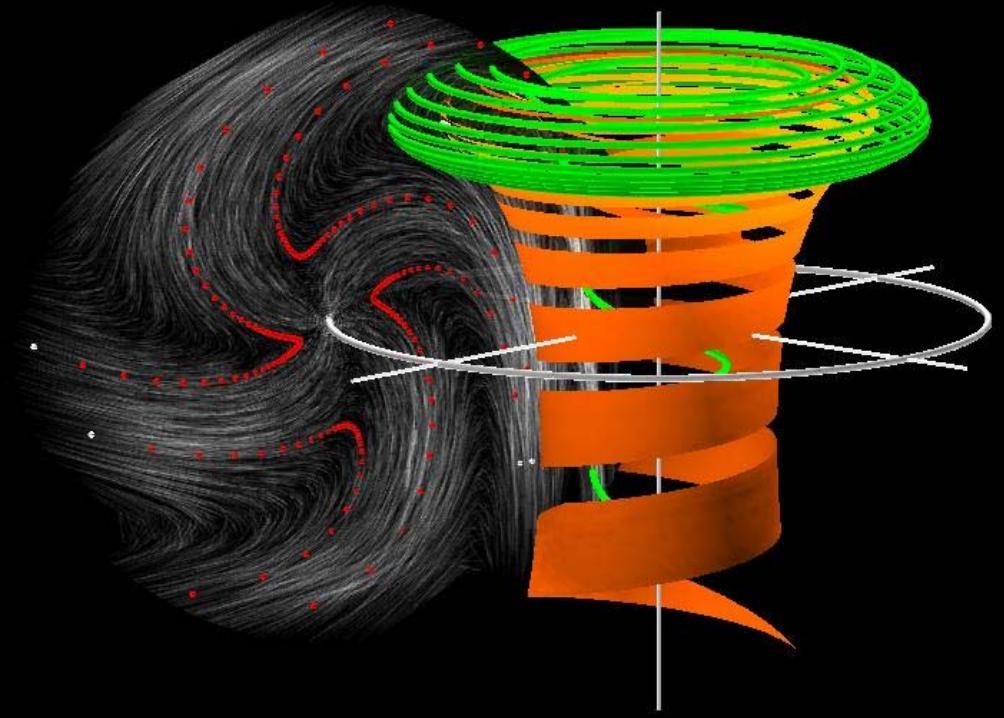
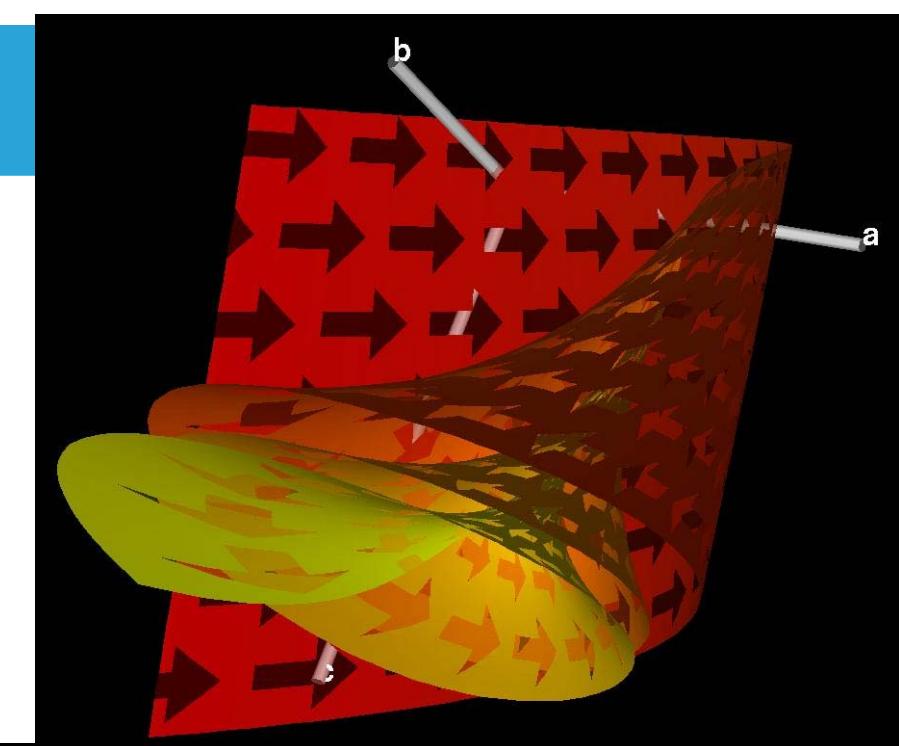
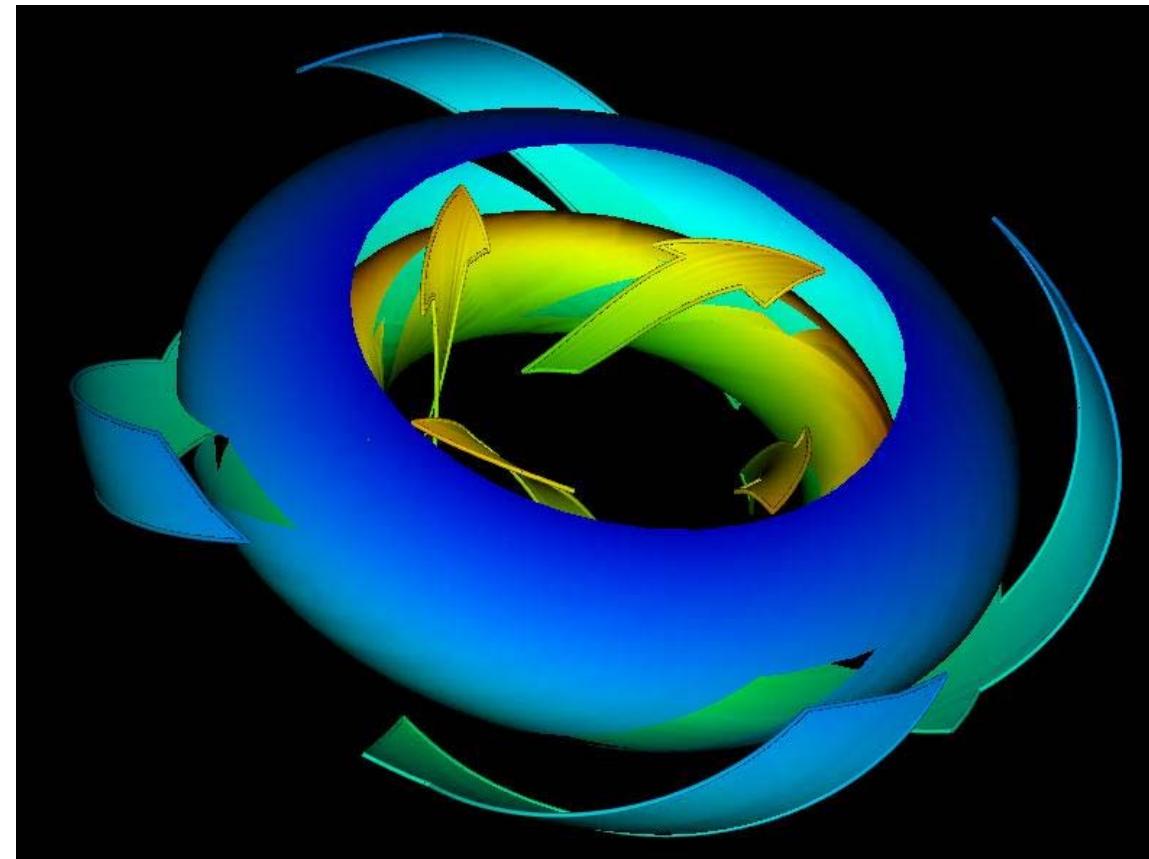


# Visualization of Models

## ■ Sketchy, “hand drawn”



# Visualization of 3D Models



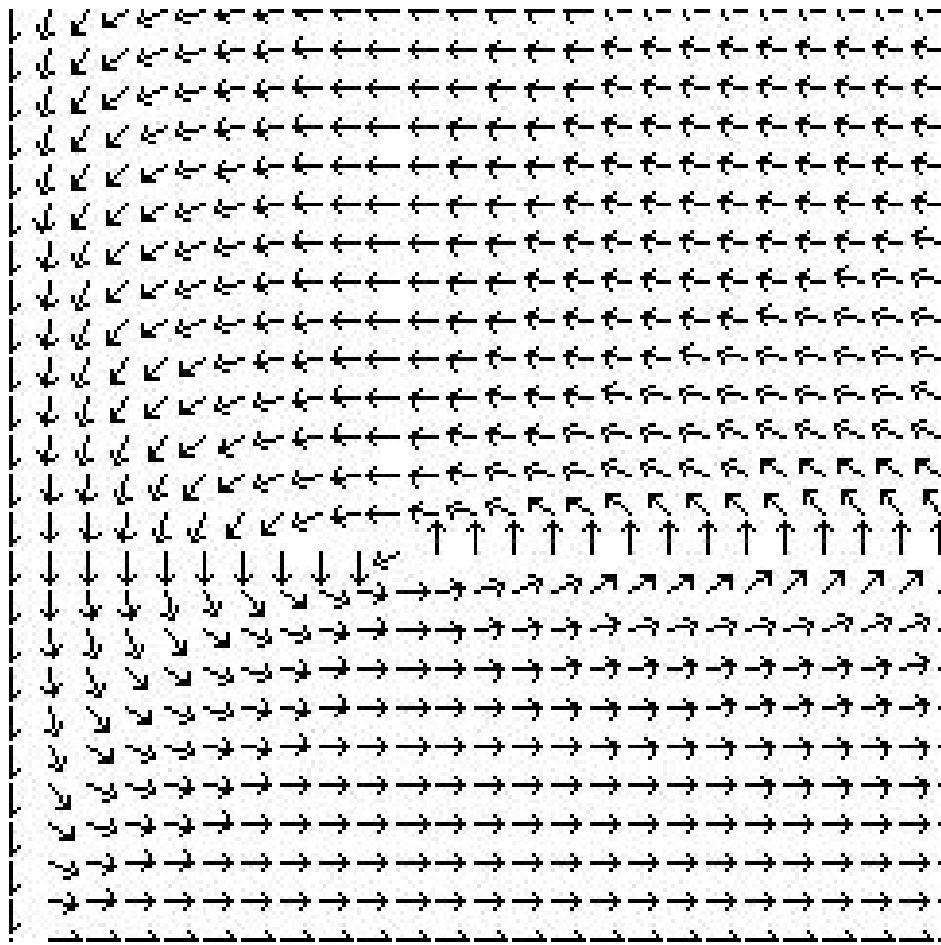
# **Flow Visualization with Arrows**

Hedgehog plots, etc.

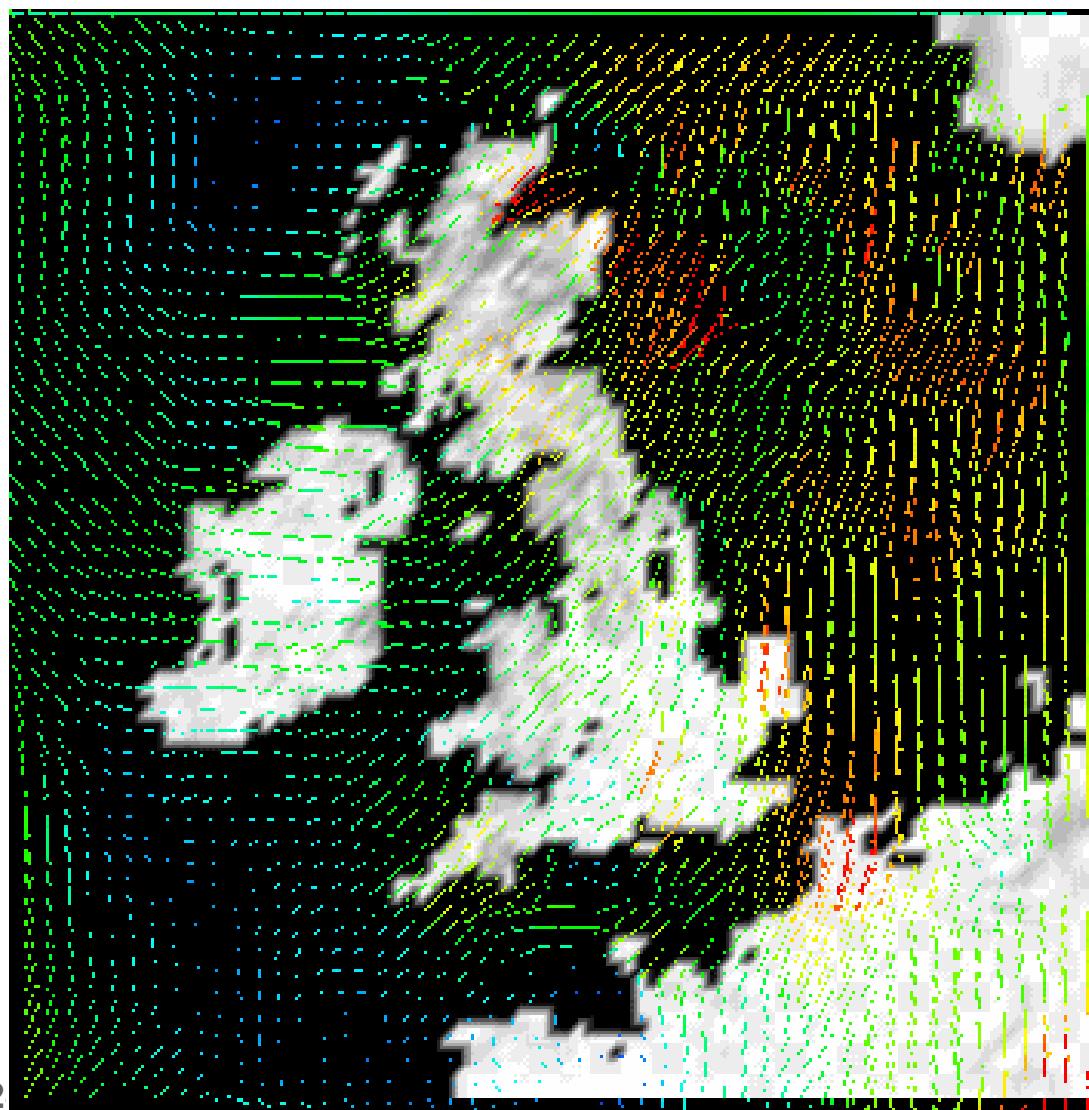
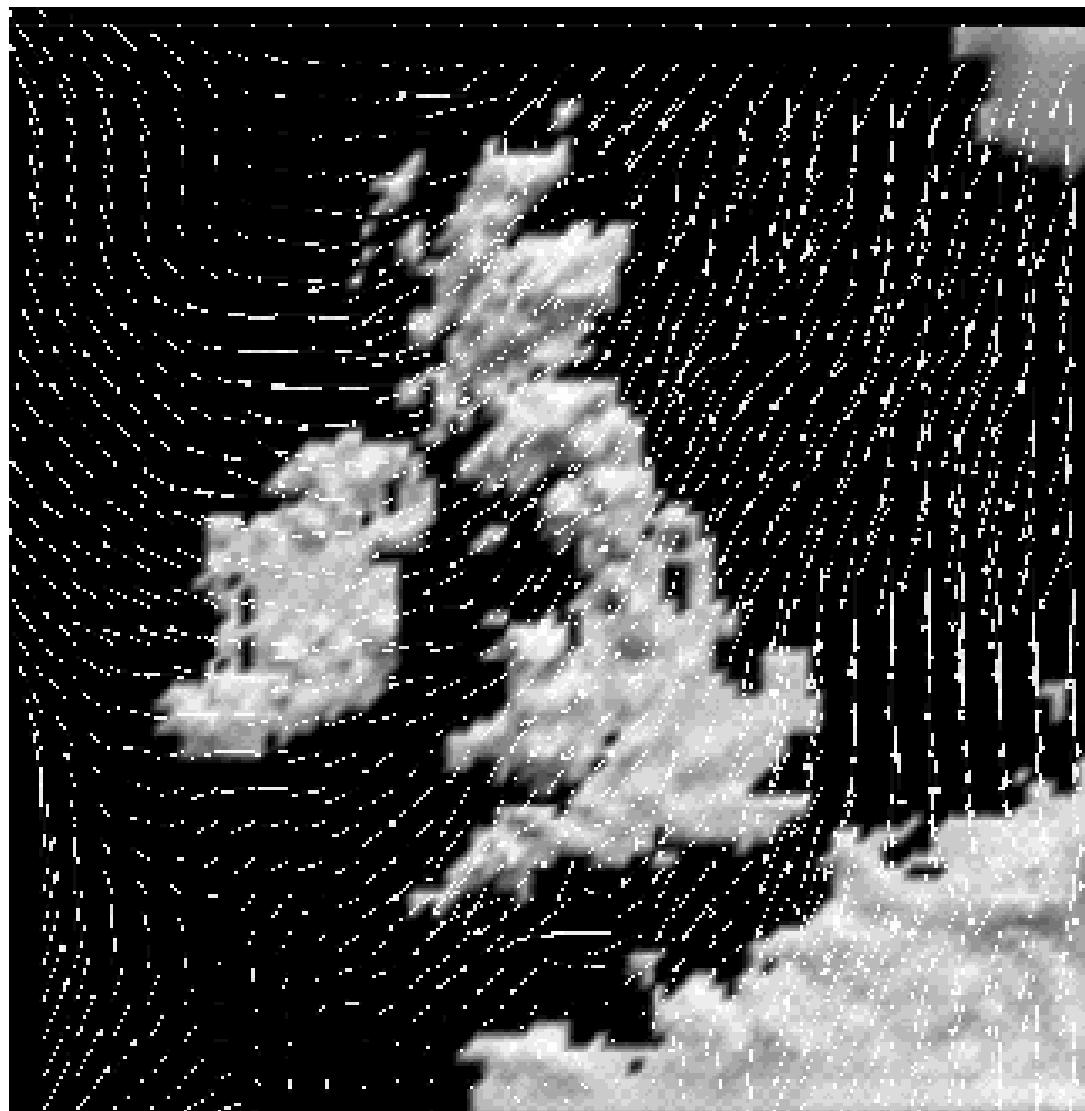


## ■ Aspects:

- ◆ Direct Flow Visualization
- ◆ Normalized arrows vs. scaling with velocity
- ◆ 2D: quite usable,  
3D: often problematic
- ◆ Sometimes limited expressivity (temporal component missing)
- ◆ Often used!



- Scaled arrows vs. color-coded arrows

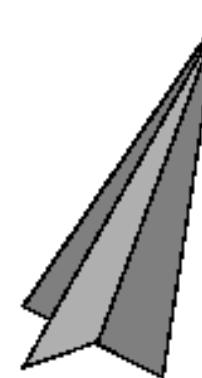
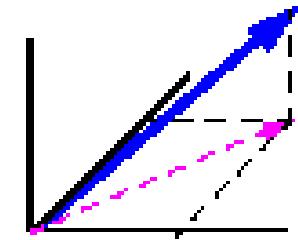
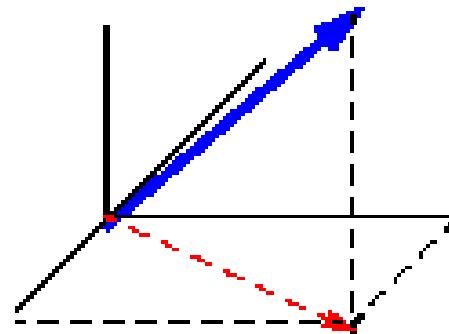


## ■ Following problems:

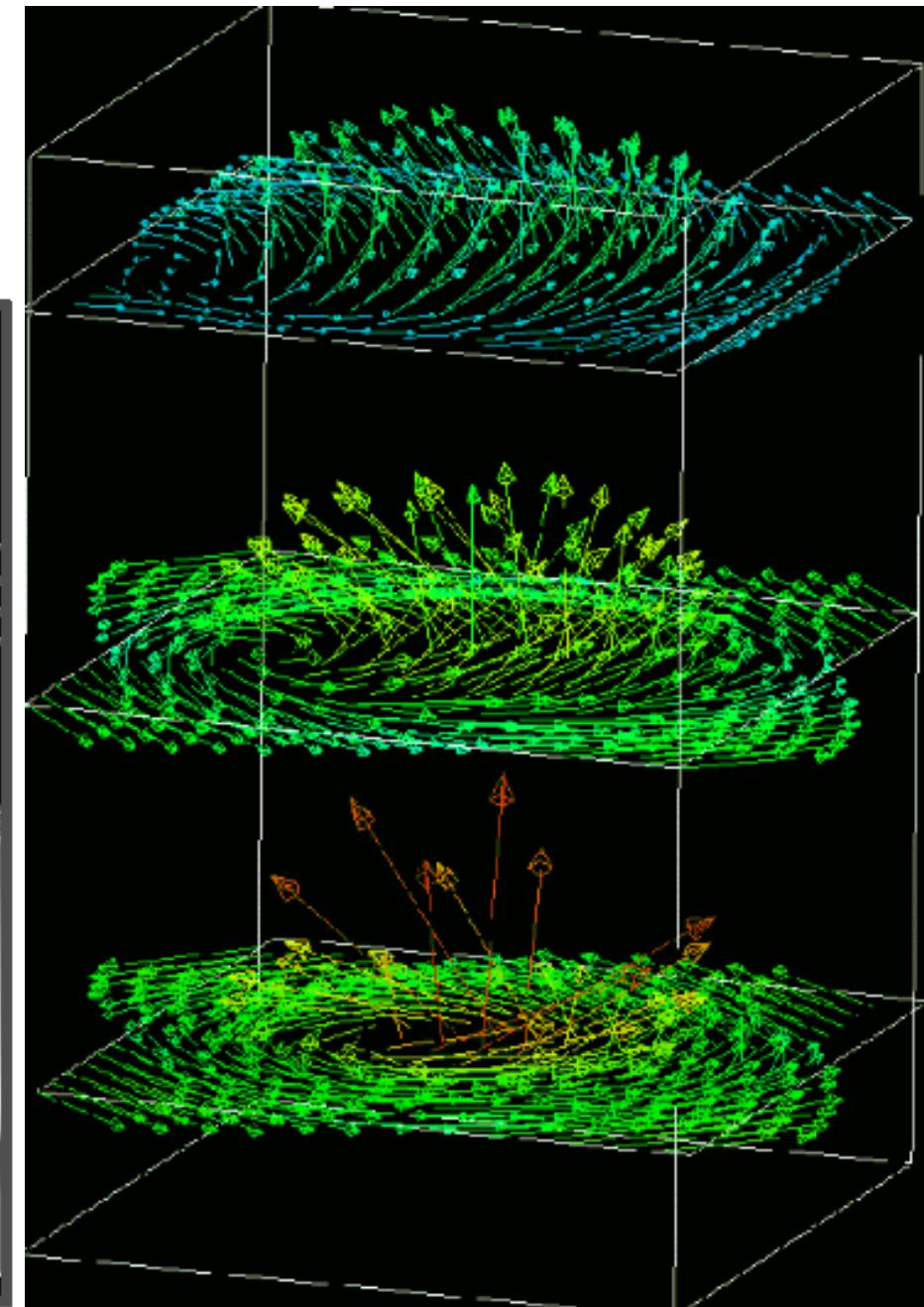
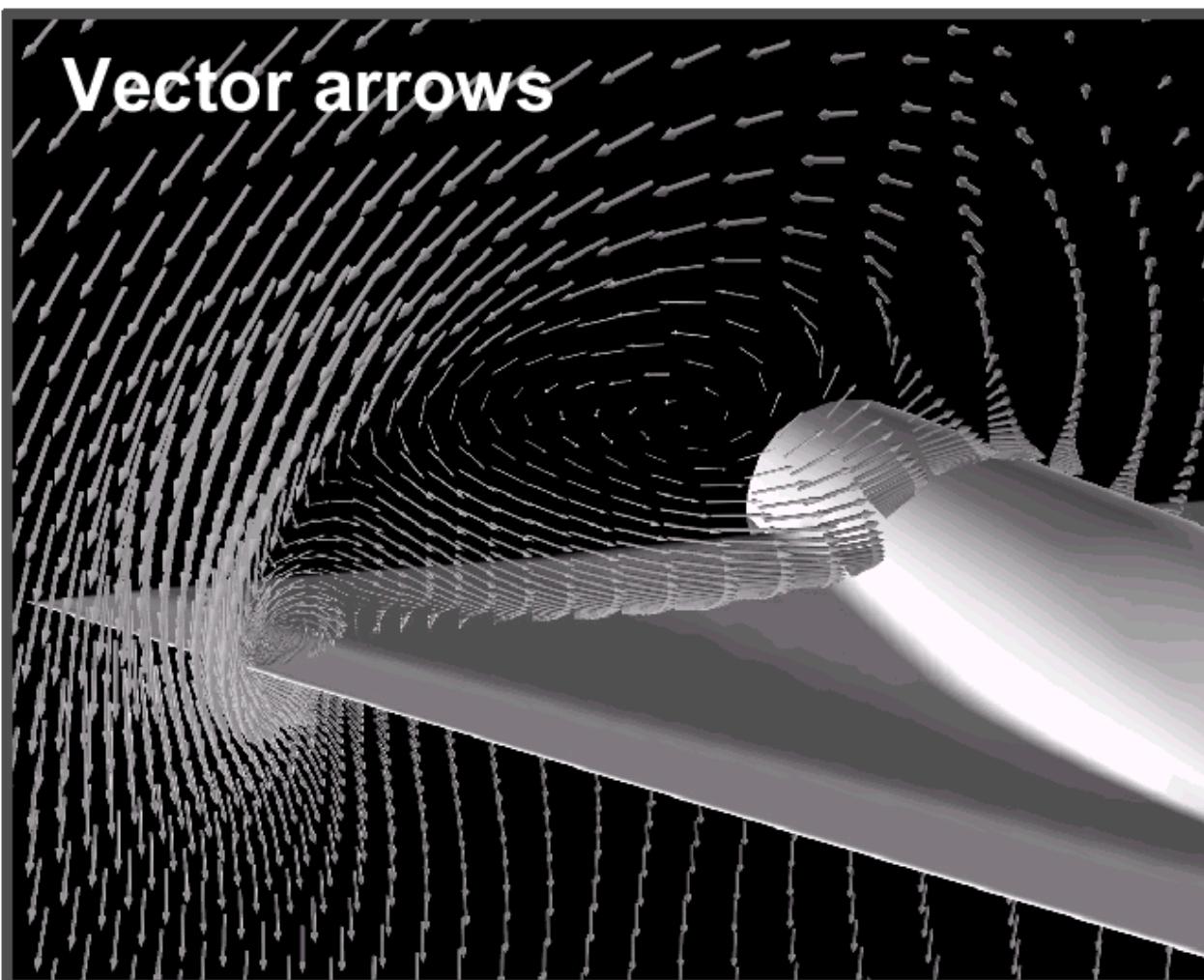
- ◆ Ambiguity
- ◆ Perspective Shortening
- ◆ 1D-objects in 3D:  
difficult spatial perception
- ◆ Visual clutter

## ■ Improvement:

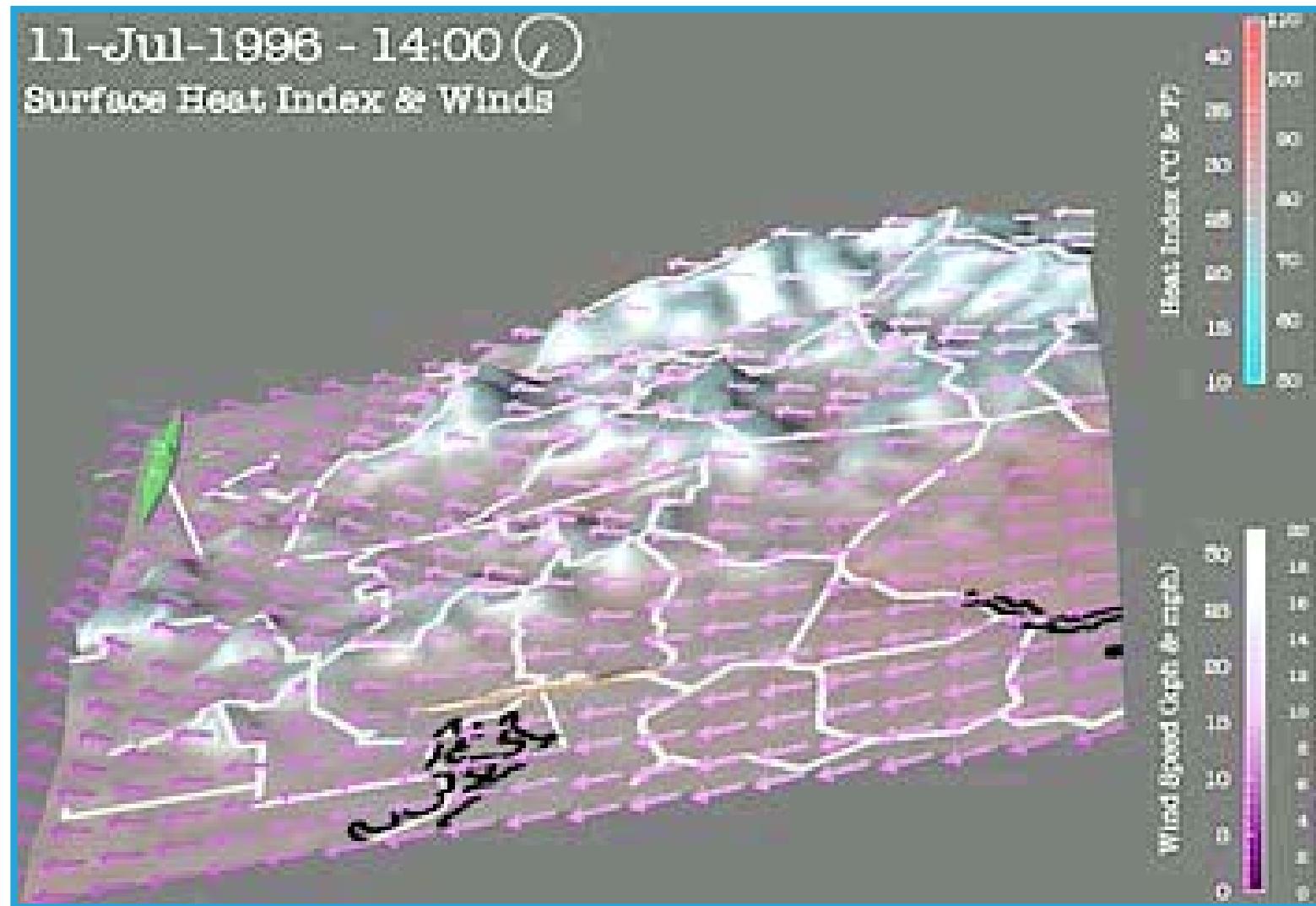
- ◆ 3D-arrows (help to a certain extent)



- Compromise:  
Arrows only in slices



- Well integrable within “real” 3D:



# Integration of Streamlines

Numerical Integration

# Streamlines – Theory

## ■ Correlations:

- flow data  $\mathbf{v}$ : derivative information
- $d\mathbf{x}/dt = \mathbf{v}(\mathbf{x})$ ;  
spatial points  $\mathbf{x} \in \mathbb{R}^n$ , time  $t \in \mathbb{R}$ , flow vectors  $\mathbf{v} \in \mathbb{R}^n$
- streamline  $\mathbf{s}$ : integration over time,  
also called trajectory, solution, curve
- $\mathbf{s}(t) = \mathbf{s}_0 + \int_{0 \leq u \leq t} \mathbf{v}(\mathbf{s}(u)) du$ ;  
seed point  $\mathbf{s}_0$ , integration variable  $u$
- difficulty: result  $\mathbf{s}$  also in the integral  $\Rightarrow$  analytical solution usually impossible!

# Streamlines – Practice

## ■ Basic approach:

- theory:  $\mathbf{s}(t) = \mathbf{s}_0 + \int_{0 \leq u \leq t} \mathbf{v}(\mathbf{s}(u)) du$
- practice: numerical integration
- idea:  
(very) locally, the solution is (approx.) linear
- Euler integration:  
follow the current flow vector  $\mathbf{v}(\mathbf{s}_i)$  from the current streamline point  $\mathbf{s}_i$  for a very small time ( $dt$ ) and therefore distance
- Euler integration:  $\mathbf{s}_{i+1} = \mathbf{s}_i + dt \cdot \mathbf{v}(\mathbf{s}_i)$ ,  
integration of small steps ( $dt$  very small)

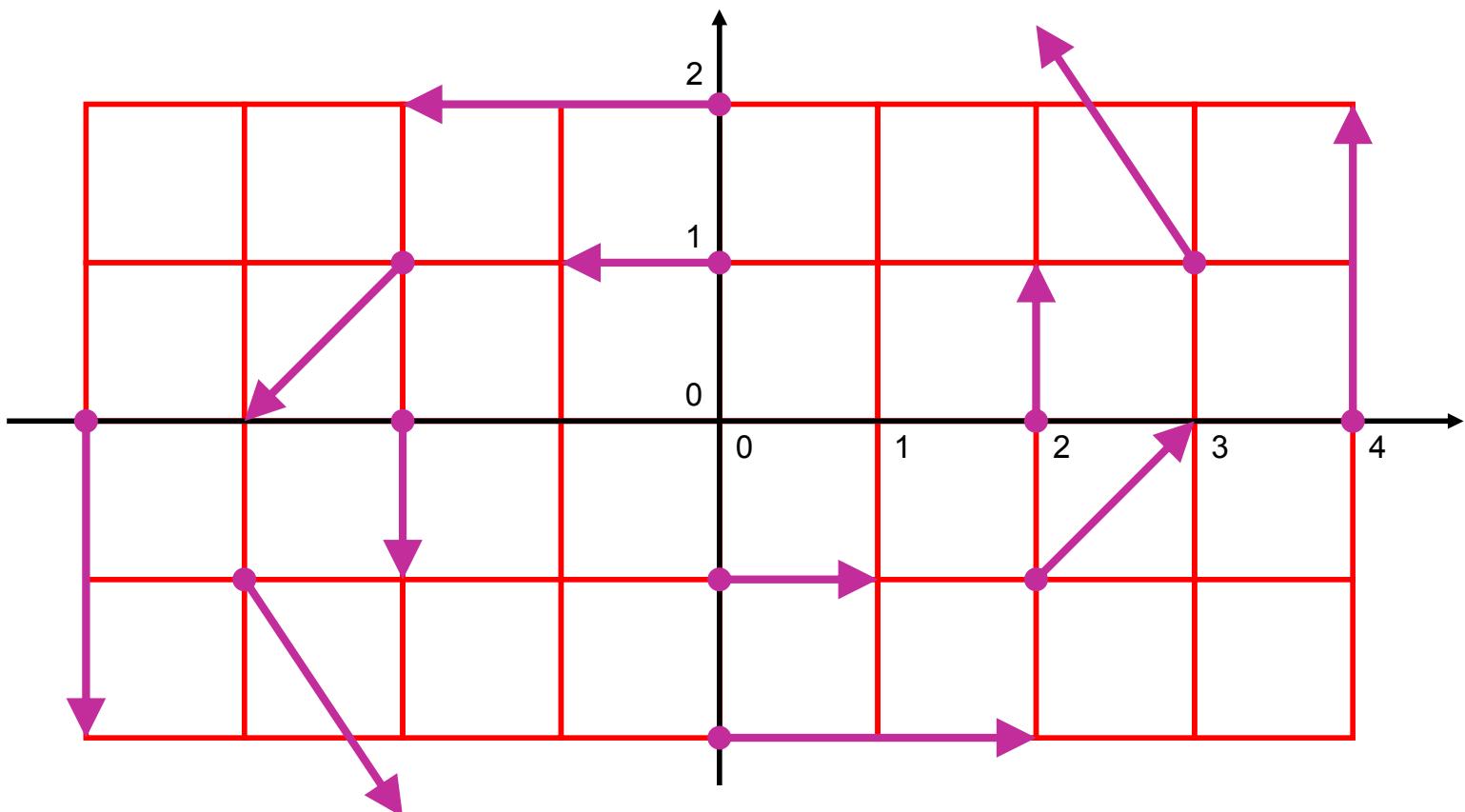
# Euler Integration – Example

- 2D model data:

$$v_x = \frac{dx}{dt} = -y$$

$$v_y = \frac{dy}{dt} = x/2$$

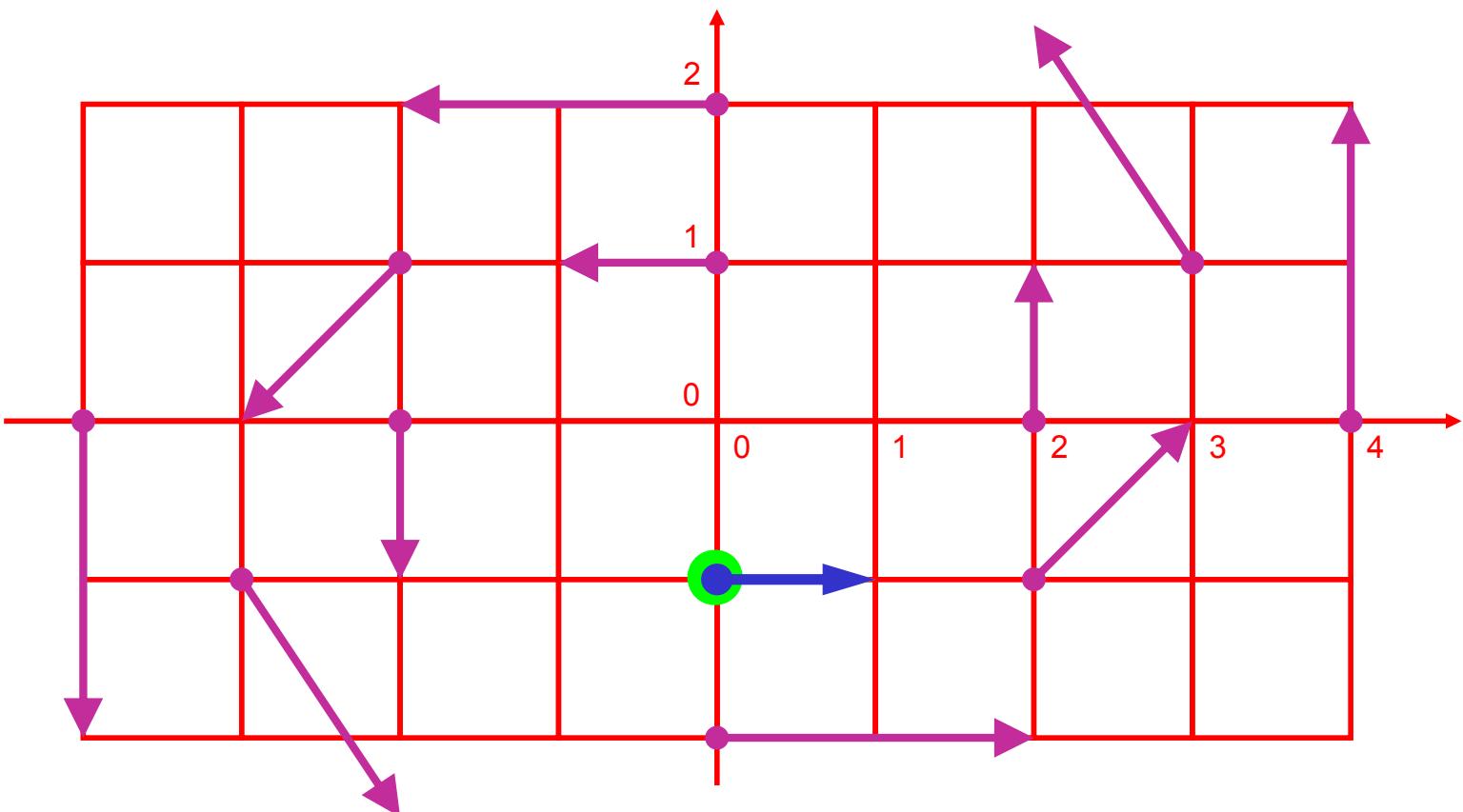
- Sample arrows:



- True solution: ellipses!

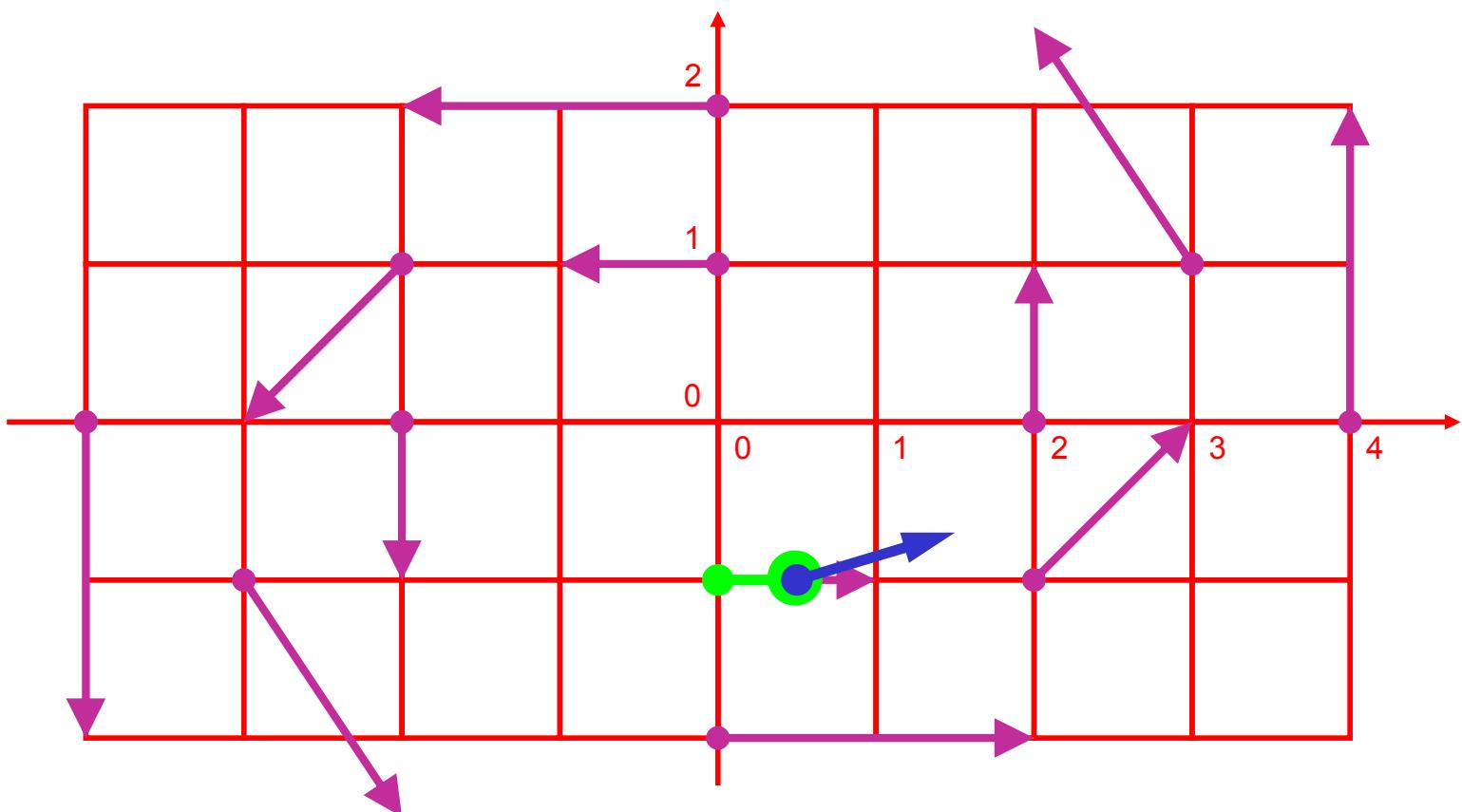
# Euler Integration – Example

- Seed point  $\mathbf{s}_0 = (0|-1)^T$ ;  
 current flow vector  $\mathbf{v}(\mathbf{s}_0) = (1|0)^T$ ;  
 $dt = 1/2$



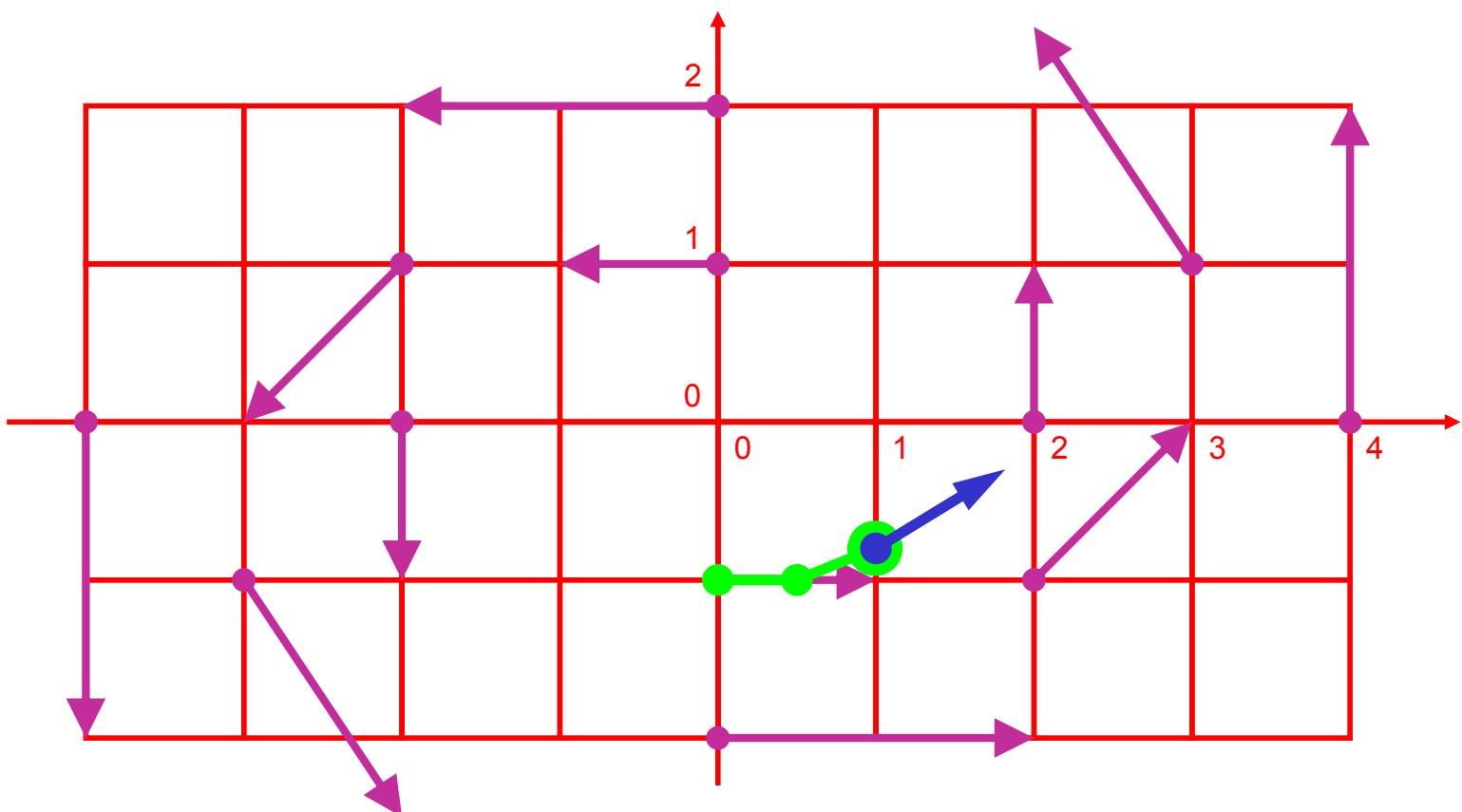
# Euler Integration – Example

- New point  $\mathbf{s}_1 = \mathbf{s}_0 + \mathbf{v}(\mathbf{s}_0) \cdot dt = (1/2 | -1)^T$ ;  
 current flow vector  $\mathbf{v}(\mathbf{s}_1) = (1 | 1/4)^T$ ;



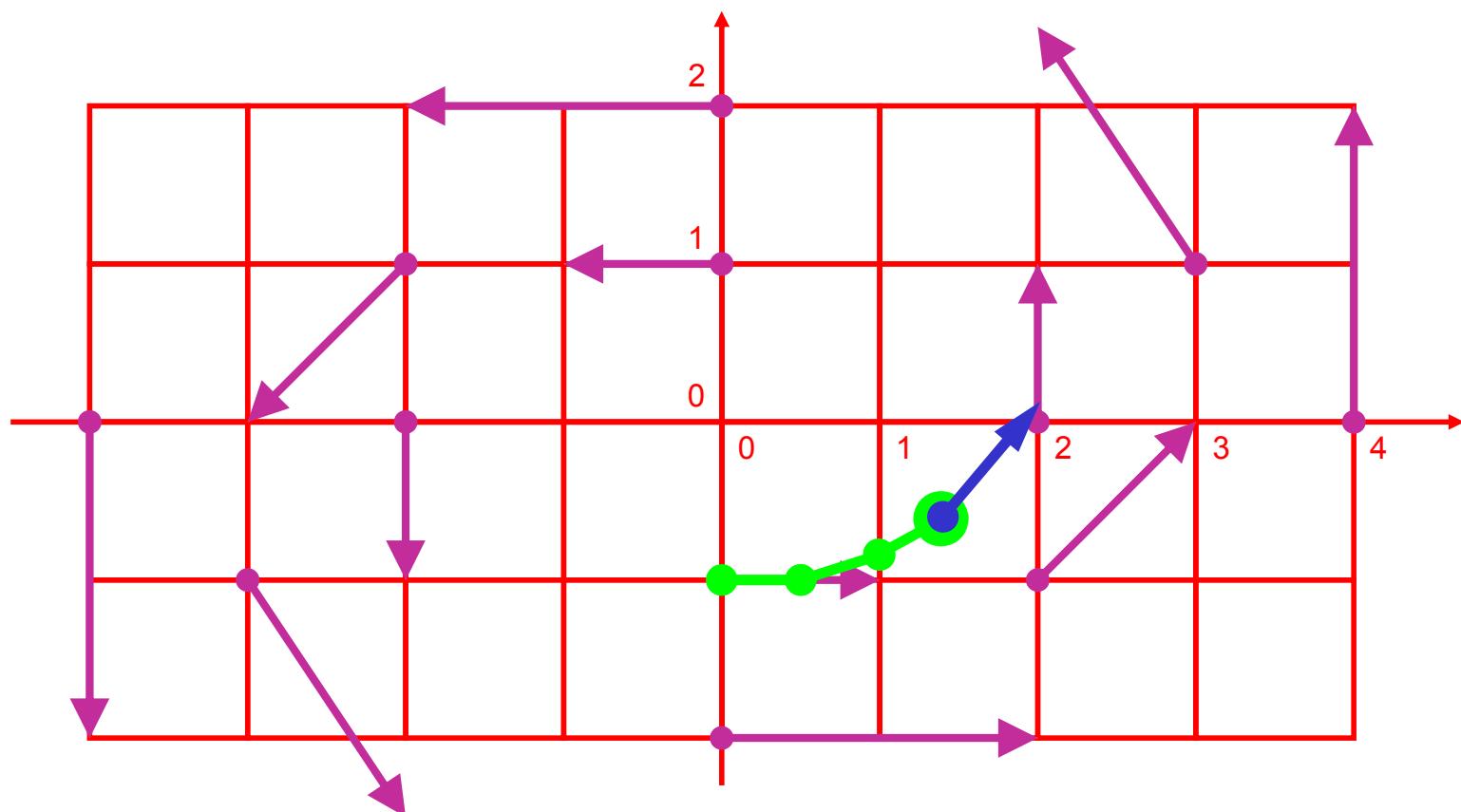
# Euler Integration – Example

- New point  $\mathbf{s}_2 = \mathbf{s}_1 + \mathbf{v}(\mathbf{s}_1) \cdot dt = (1 | -7/8)^T$ ;  
 current flow vector  $\mathbf{v}(\mathbf{s}_2) = (7/8 | 1/2)^T$ ;



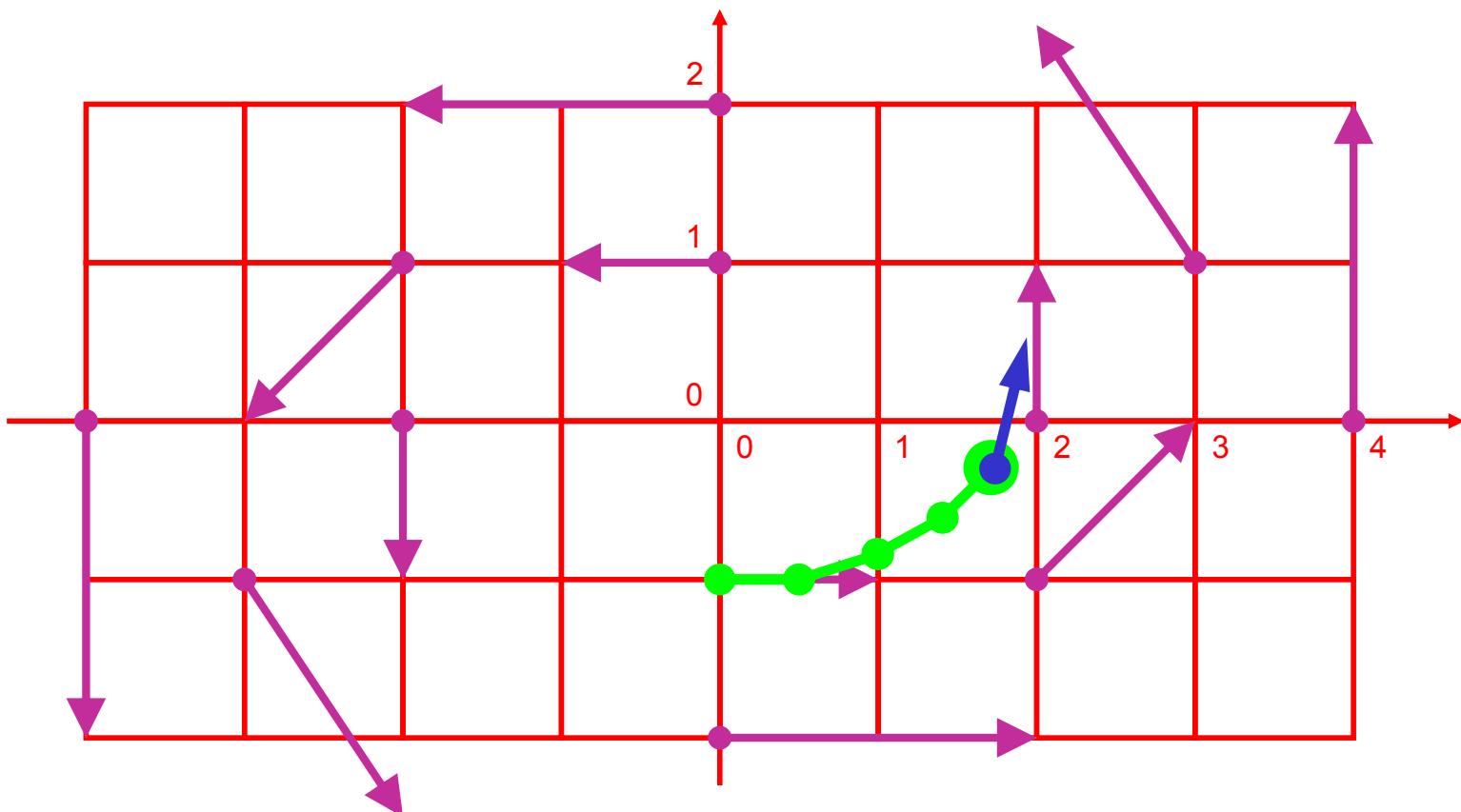
# Euler Integration – Example

- $\mathbf{s}_3 = (23/16 \mid -5/8)^T \approx (1.44 \mid -0.63)^T;$   
 $\mathbf{v}(\mathbf{s}_3) = (5/8 \mid 23/32)^T \approx (0.63 \mid 0.72)^T;$



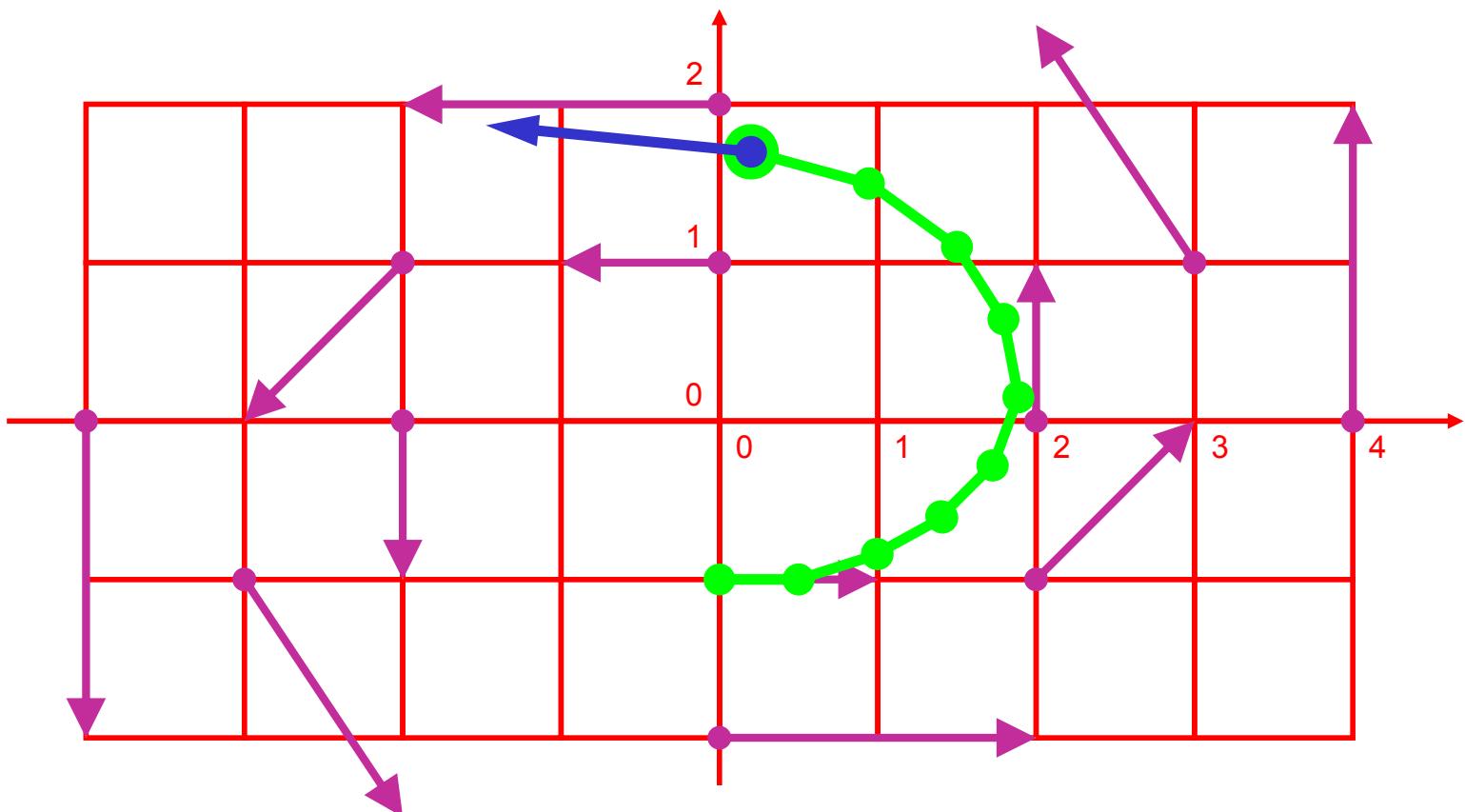
# Euler Integration – Example

- $\mathbf{s}_4 = \begin{pmatrix} 7/4 & -17/64 \end{pmatrix}^T \approx (1.75 \mid -0.27)^T;$   
 $\mathbf{v}(\mathbf{s}_4) = \begin{pmatrix} 17/64 & 7/8 \end{pmatrix}^T \approx (0.27 \mid 0.88)^T;$



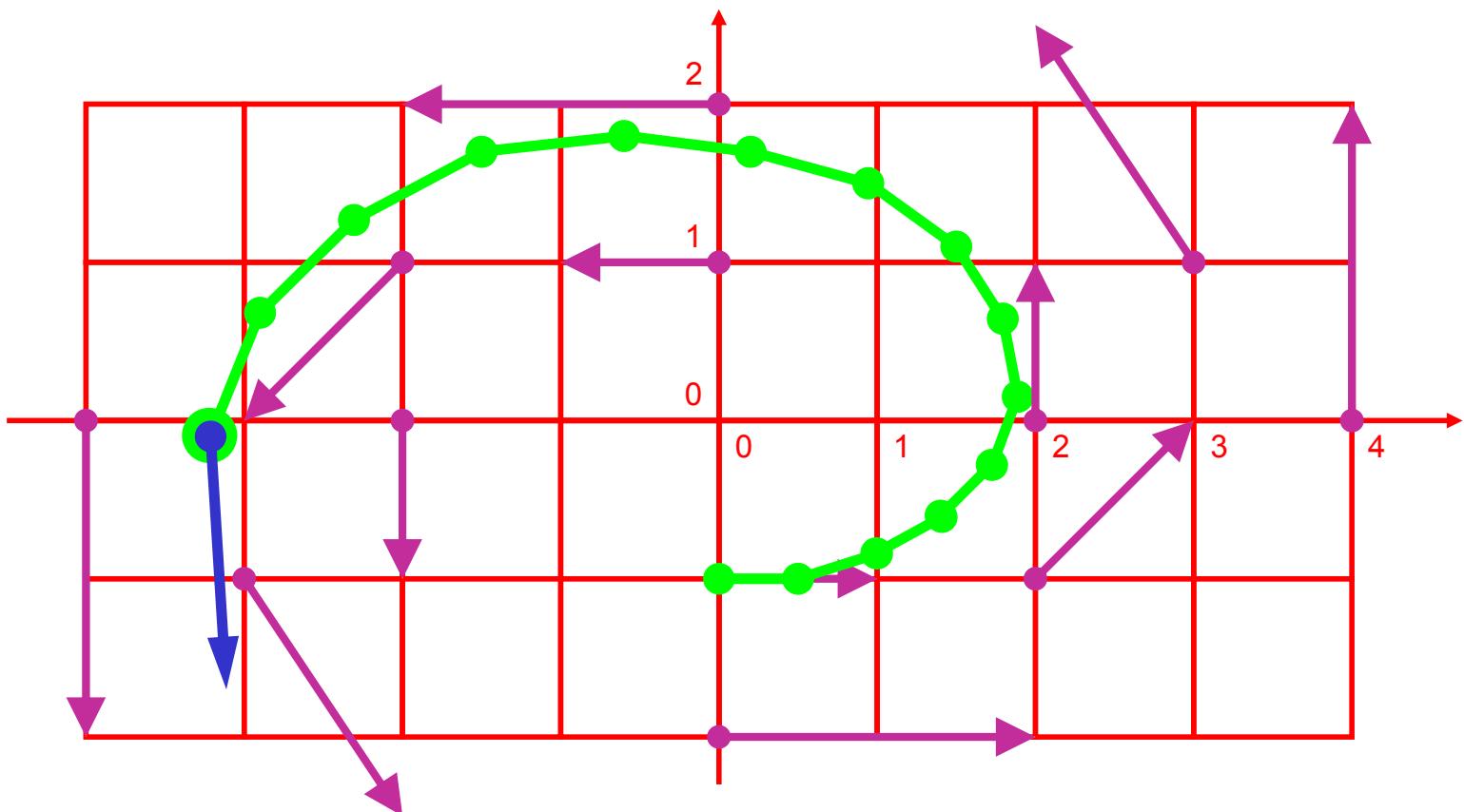
# Euler Integration – Example

- $s_9$   $\approx (0.20|1.69)^T;$   
 $v(s_9) \approx (-1.69|0.10)^T;$



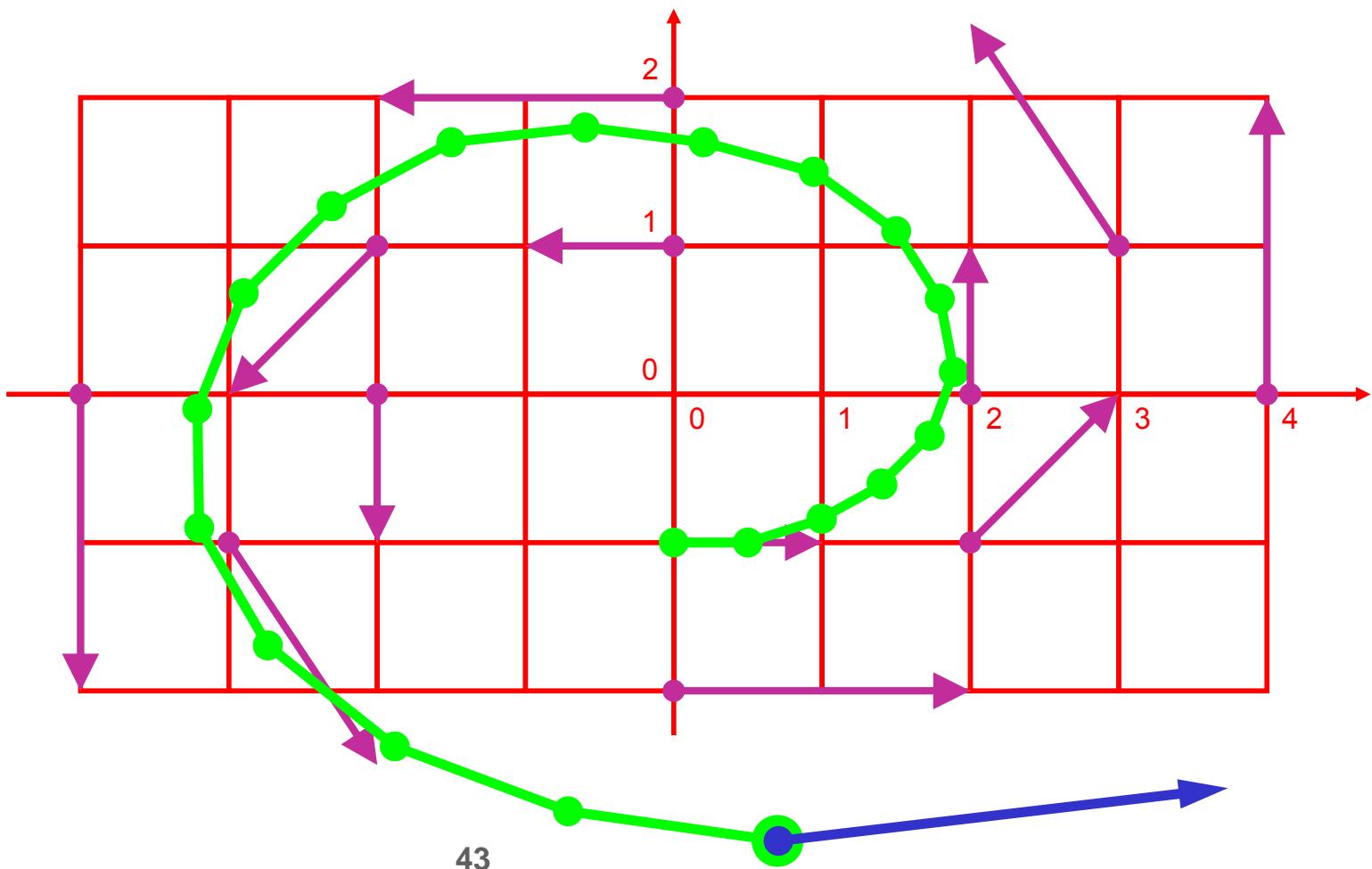
# Euler Integration – Example

- $s_{14}$   $\approx (-3.22 \mid -0.10)^T$ ;  
 $v(s_{14}) \approx (0.10 \mid -1.61)^T$ ;



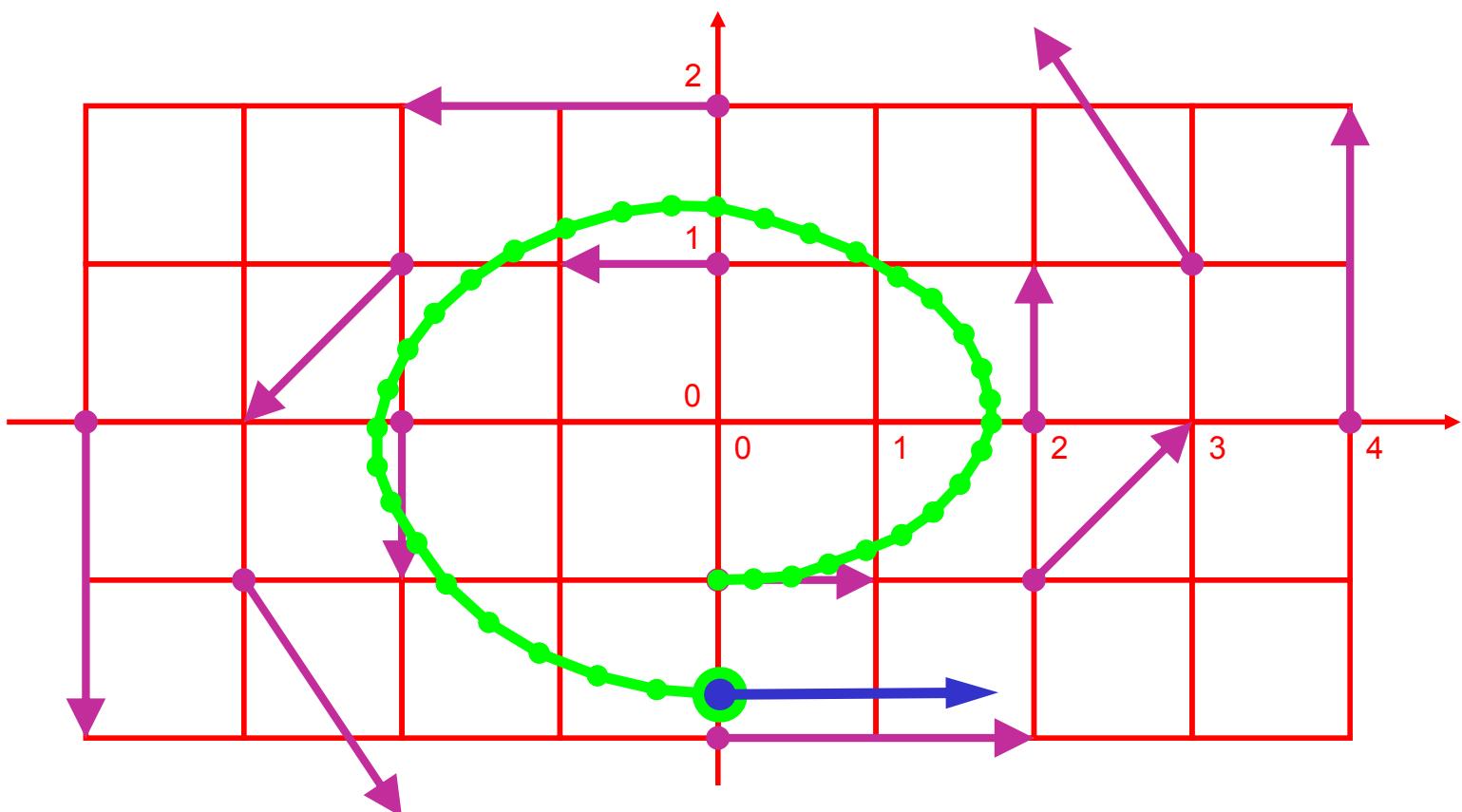
# Euler Integration – Example

- $\mathbf{s}_{19} \approx (0.75|-3.02)^T$ ;  $\mathbf{v}(\mathbf{s}_{19}) \approx (3.02|0.37)^T$ ;  
clearly: large integration error,  $dt$  too large!  
19 steps



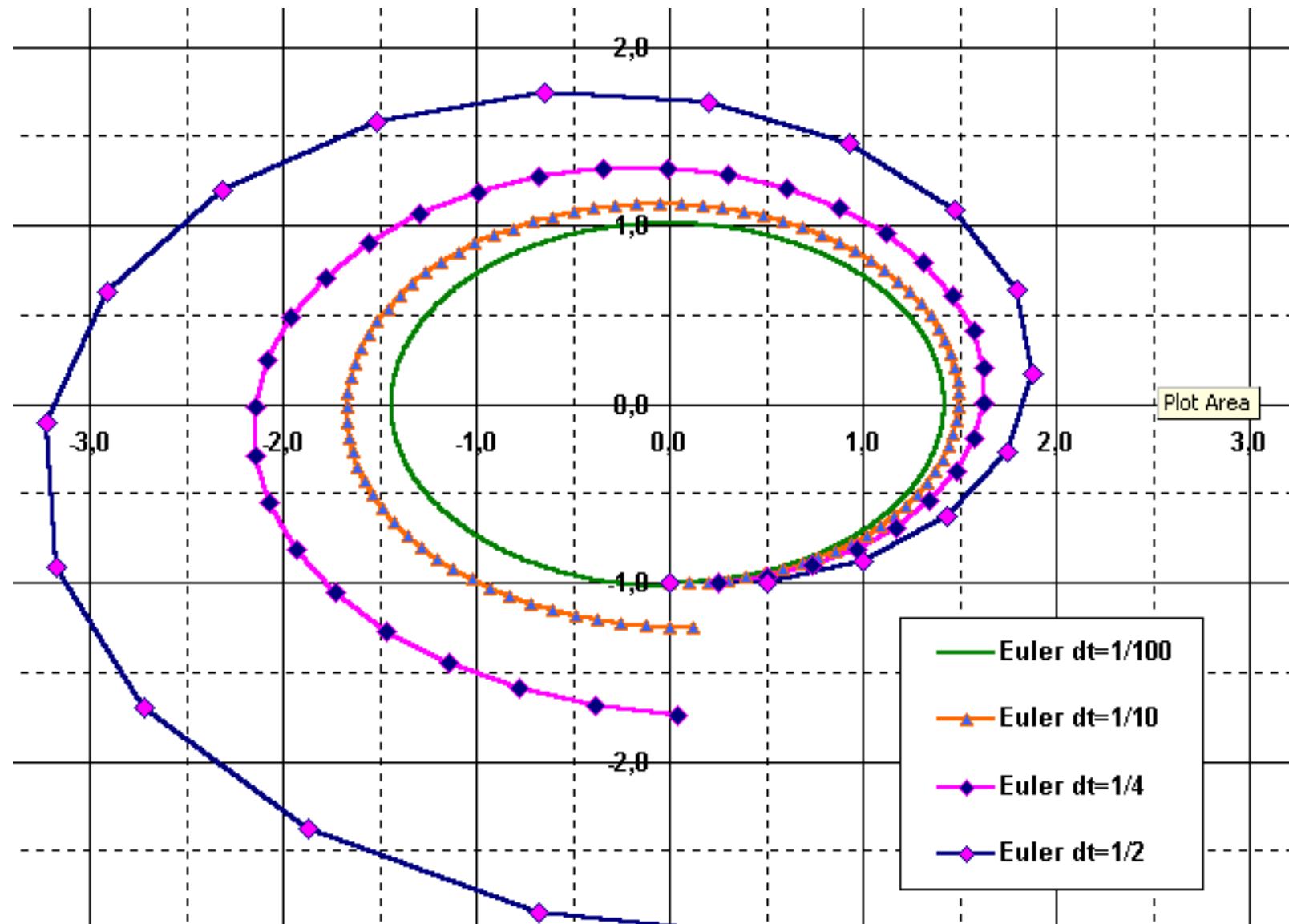
# Euler Integration – Example

- $dt$  smaller ( $1/4$ ): more steps, more exact!  
 $\mathbf{s}_{36} \approx (0.04 \mid -1.74)^T$ ;  $\mathbf{v}(\mathbf{s}_{36}) \approx (1.74 \mid 0.02)^T$ ;
- 36 steps



# Comparison Euler, Step Sizes

Euler  
is getting  
better  
proportionally  
to  $dt$



# Euler Example – Error Table

■	dt	#steps	error	
■	1/2	19	~200%	
■	1/4	36	~75%	
■	1/10	89	~25%	
■	1/100	889	~2%	
■	1/1000	8889	~0.2%	✓

# Better than Euler Integr.: RK

## ■ Runge-Kutta Approach:

- theory:  $\mathbf{s}(t) = \mathbf{s}_0 + \int_{0 \leq u \leq t} \mathbf{v}(\mathbf{s}(u)) du$
- Euler:  $\mathbf{s}_i = \mathbf{s}_0 + \sum_{0 \leq u < i} \mathbf{v}(\mathbf{s}_u) \cdot dt$

## ■ Runge-Kutta integration:

- idea: cut short the curve arc

- RK-2 (second order RK):

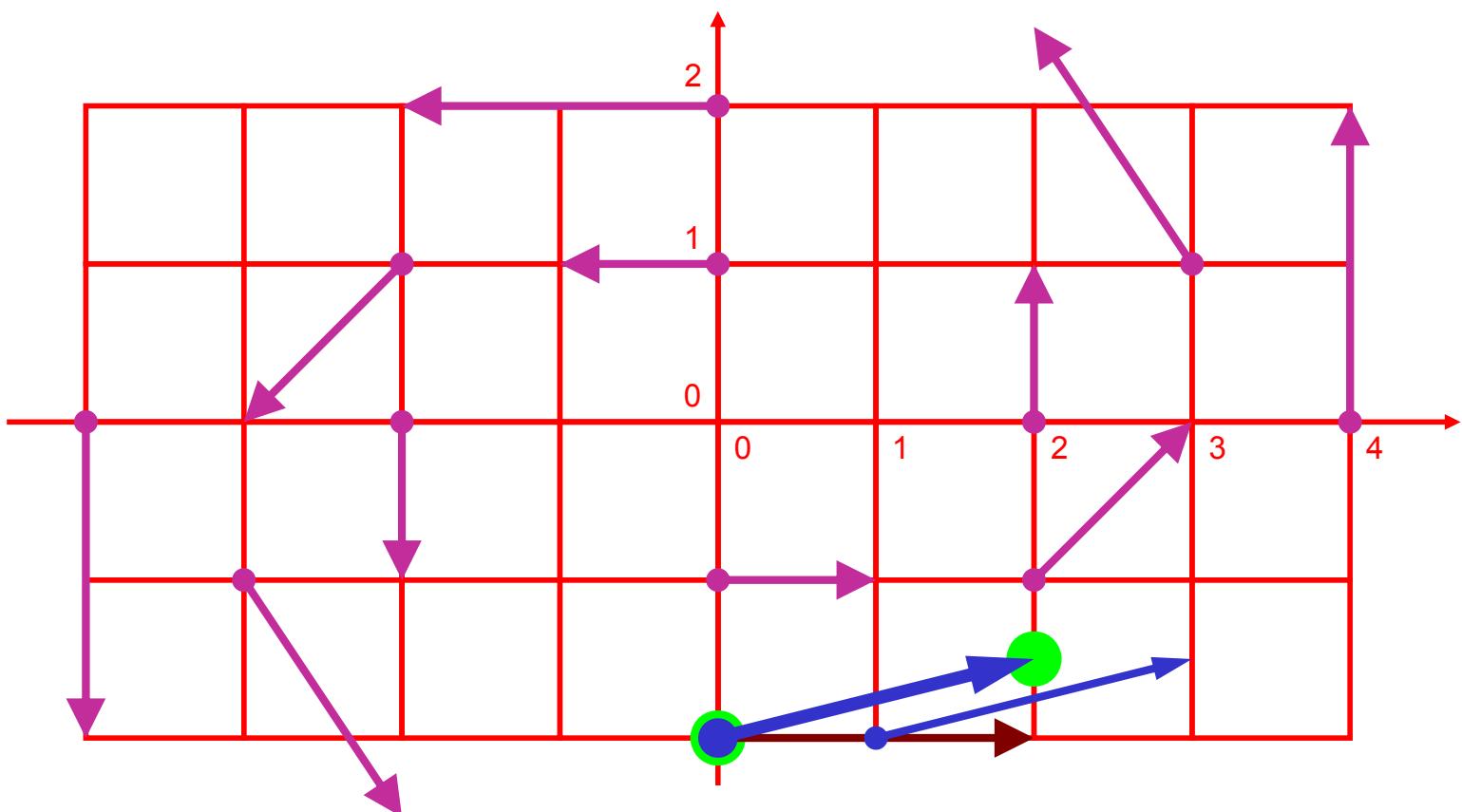
- 1.: do half a Euler step
- 2.: evaluate flow vector there
- 3.: use it in the origin

- RK-2 (two evaluations of  $\mathbf{v}$  per step):

$$\mathbf{s}_{i+1} = \mathbf{s}_i + \mathbf{v}(\mathbf{s}_i + \mathbf{v}(\mathbf{s}_i) \cdot dt/2) \cdot dt$$

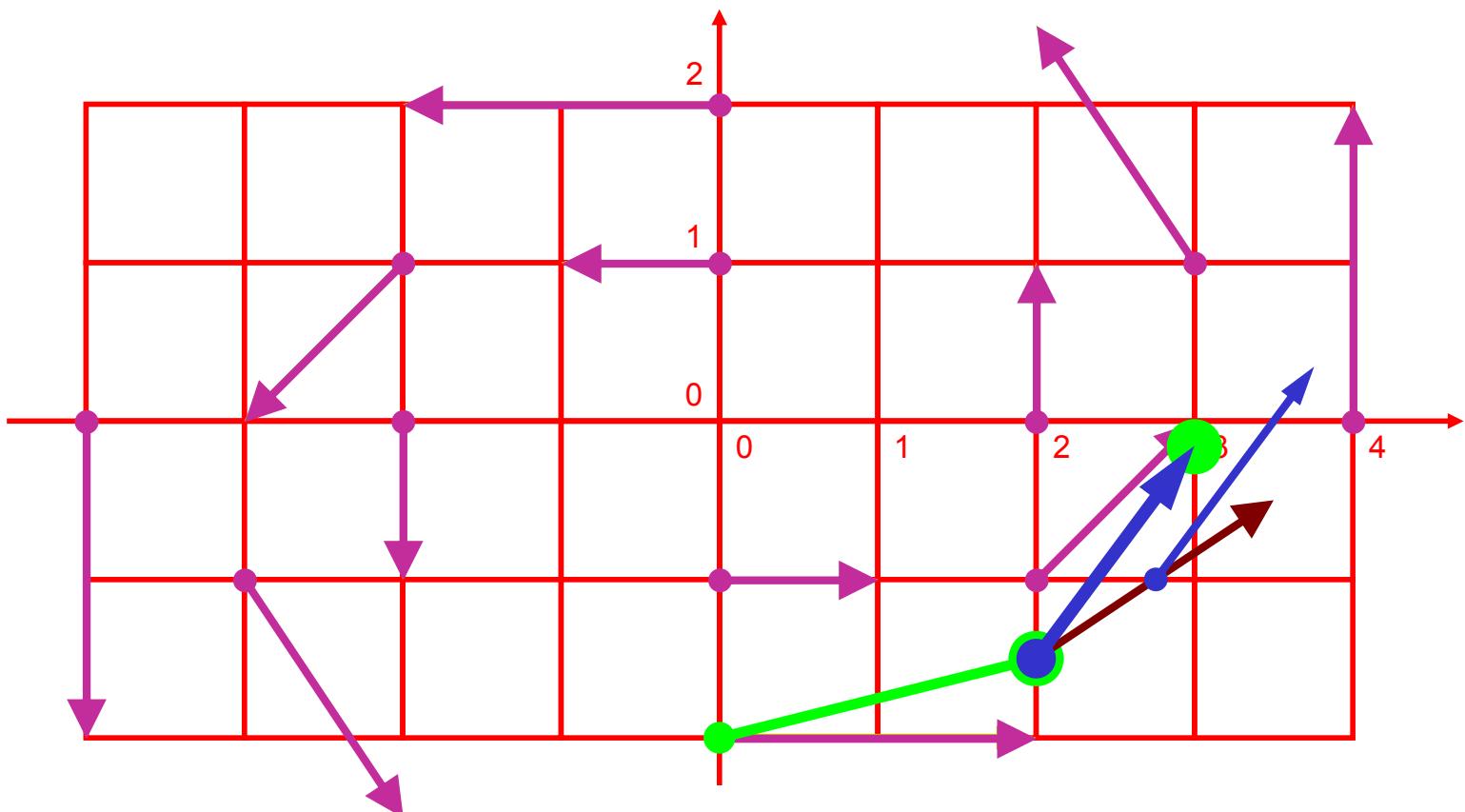
# RK-2 Integration – One Step

- Seed point  $s_0 = (0|-2)^T$ ;  
 current flow vector  $v(s_0) = (2|0)^T$ ;  
 preview vector  $v(s_0 + v(s_0) \cdot dt/2) = (2|0.5)^T$ ;  
 $dt = 1$



# RK-2 – One more step

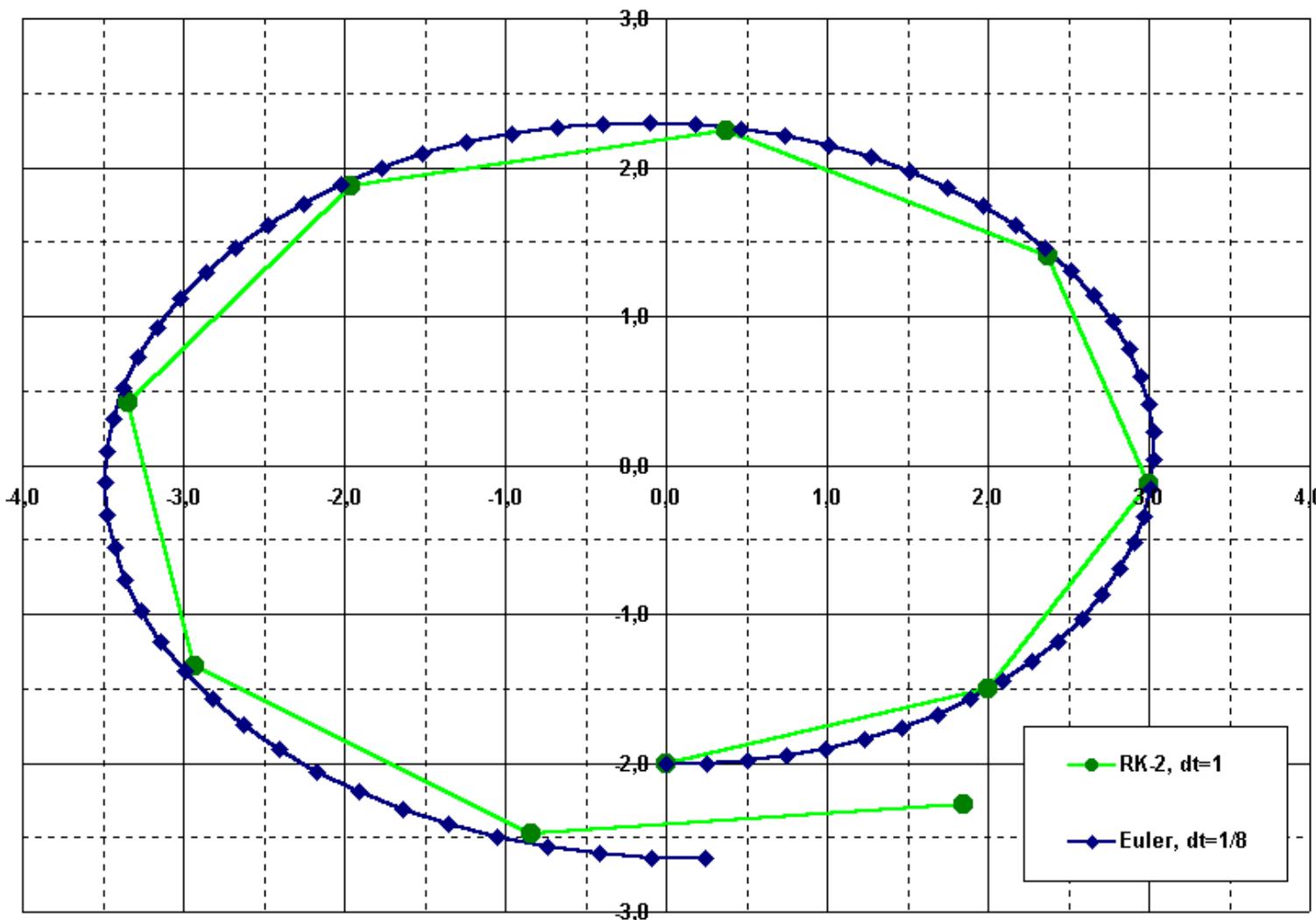
- Seed point  $s_1 = (2|-1.5)^T$ ;  
 current flow vector  $v(s_1) = (1.5|1)^T$ ;  
 preview vector  $v(s_1 + v(s_1) \cdot dt/2) \approx (1|1.4)^T$ ;  
 $dt = 1$



# RK-2 – A Quick Round

- RK-2: even with  $dt=1$  (9 steps)

better  
than Euler  
with  $dt=1/8$   
(72 steps)





# Integration, Conclusions

## ■ Summary:

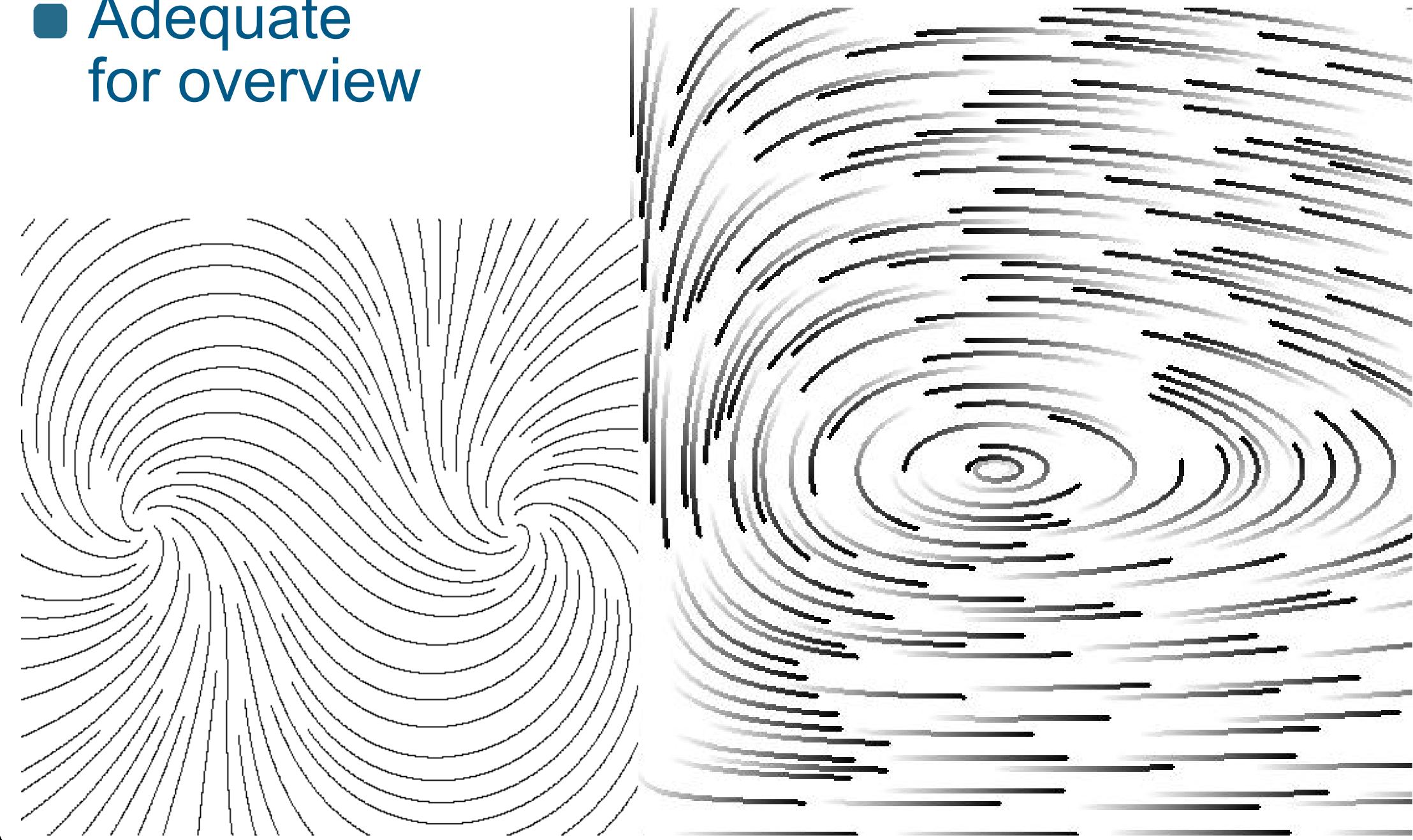
- analytic determination of streamlines  
usually not possible
- hence: numerical integration
- several methods available  
(Euler, Runge-Kutta, etc.)
- Euler: simple, imprecise, esp. with small  $dt$
- RK: more accurate in higher orders
- furthermore: adaptive methods, implicit methods, etc.

# Flow Visualization with Streamlines

Streamlines,  
Particle Paths, etc.

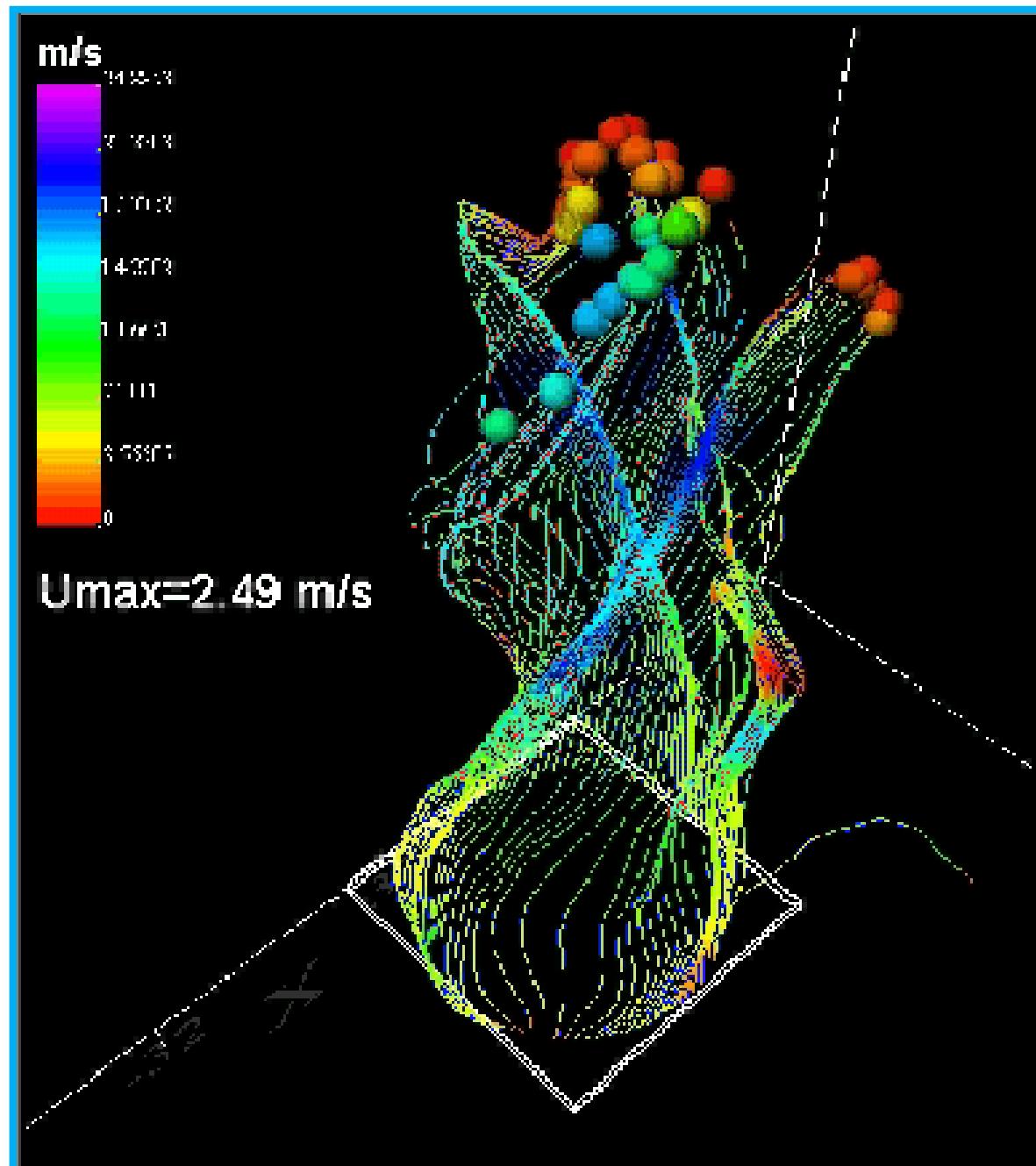
# Streamlines in 2D

- Adequate for overview



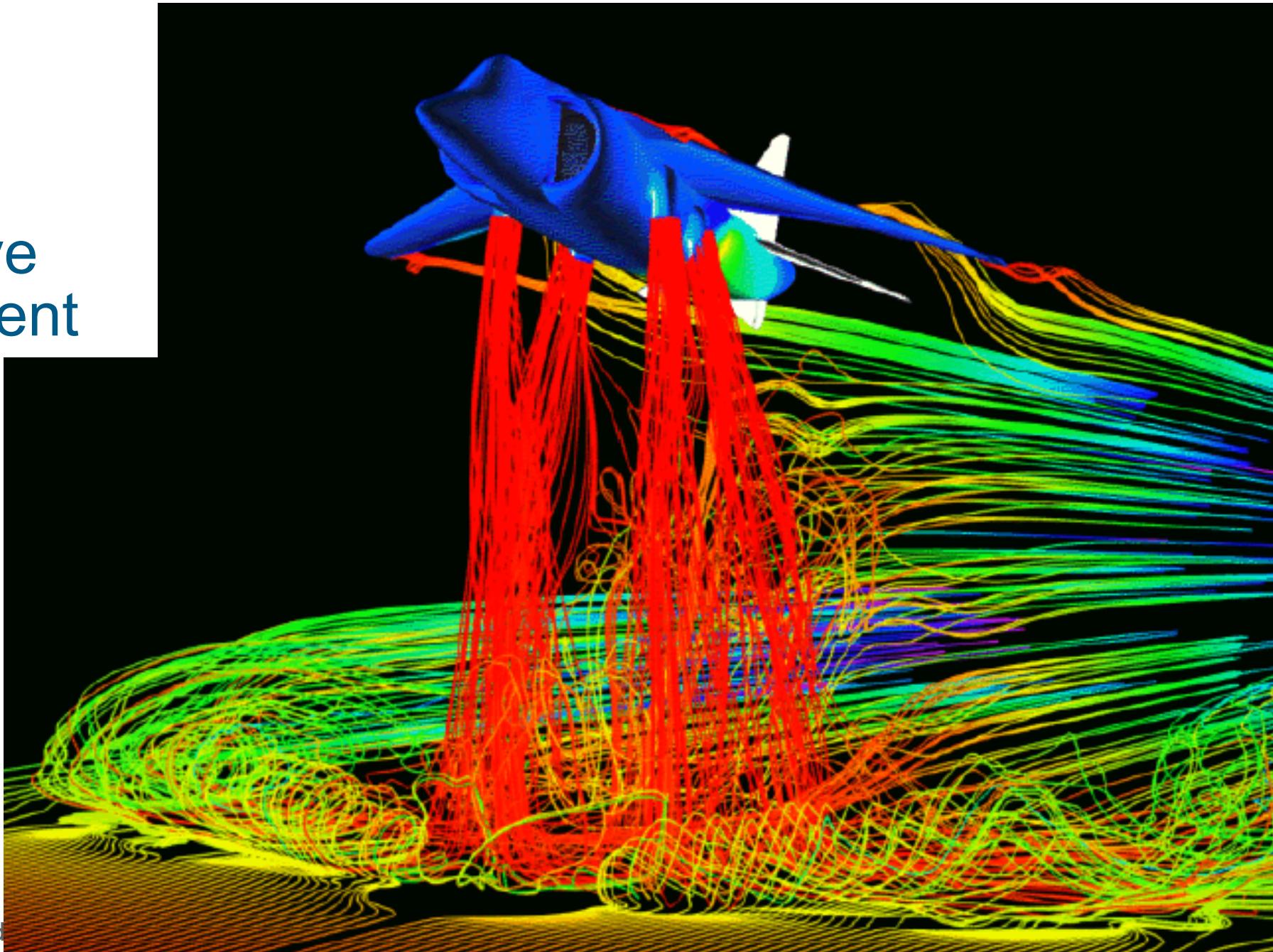
# Visualization with Particles

- Particle paths = streamlines (steady flows)
- Variants (time-dependent data):
  - **streak lines:** steadily new particles
  - **path lines:** long-term path of one particle



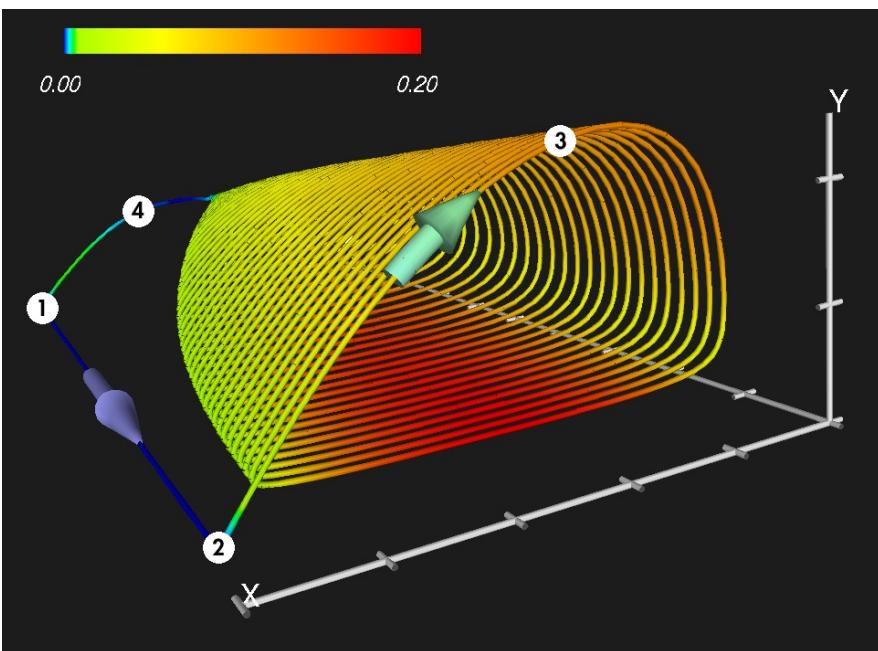
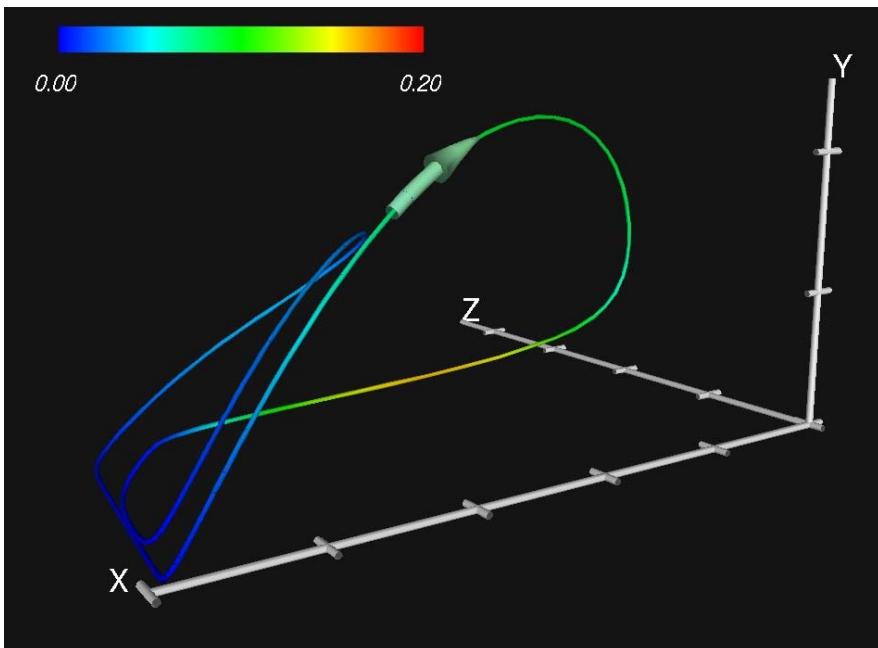
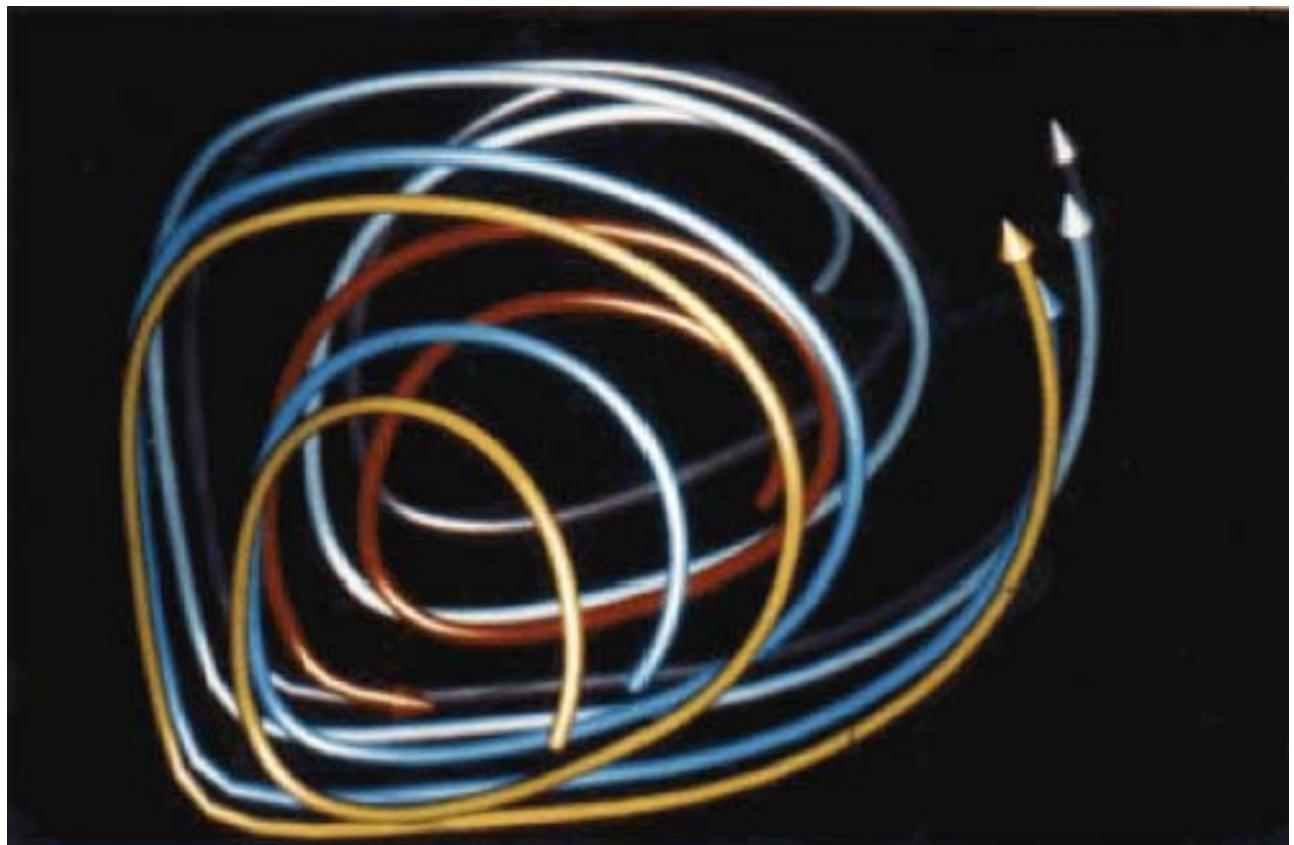
# Streamlines in 3D

- Color coding: Speed
- Selective Placement



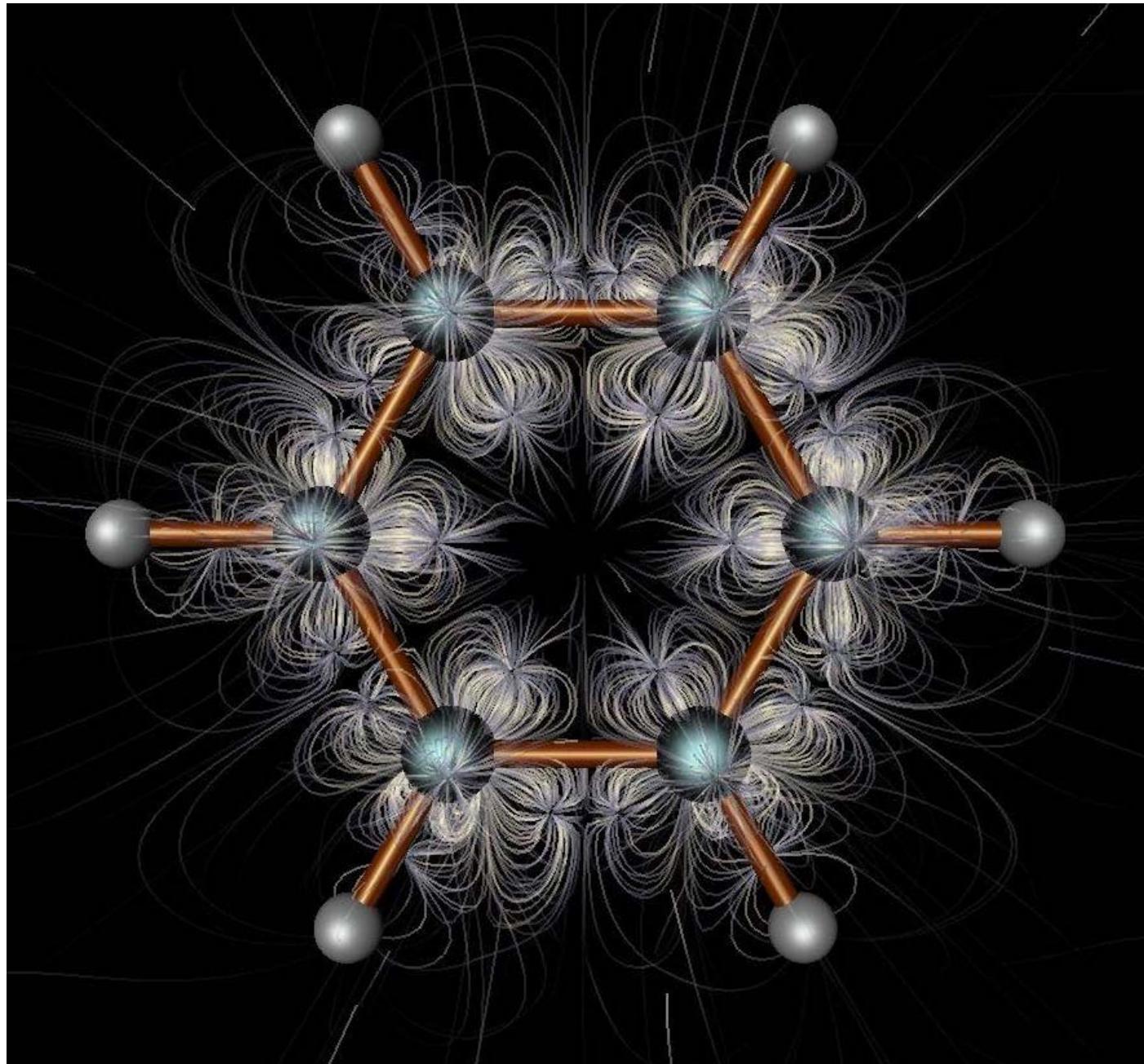
# 3D Streamlines with Sweeps

■ Sweeps:  
better spatial 3D  
perception



# Illuminated Streamlines

- Illuminated  
3D curves ⇒  
better 3D  
perception!

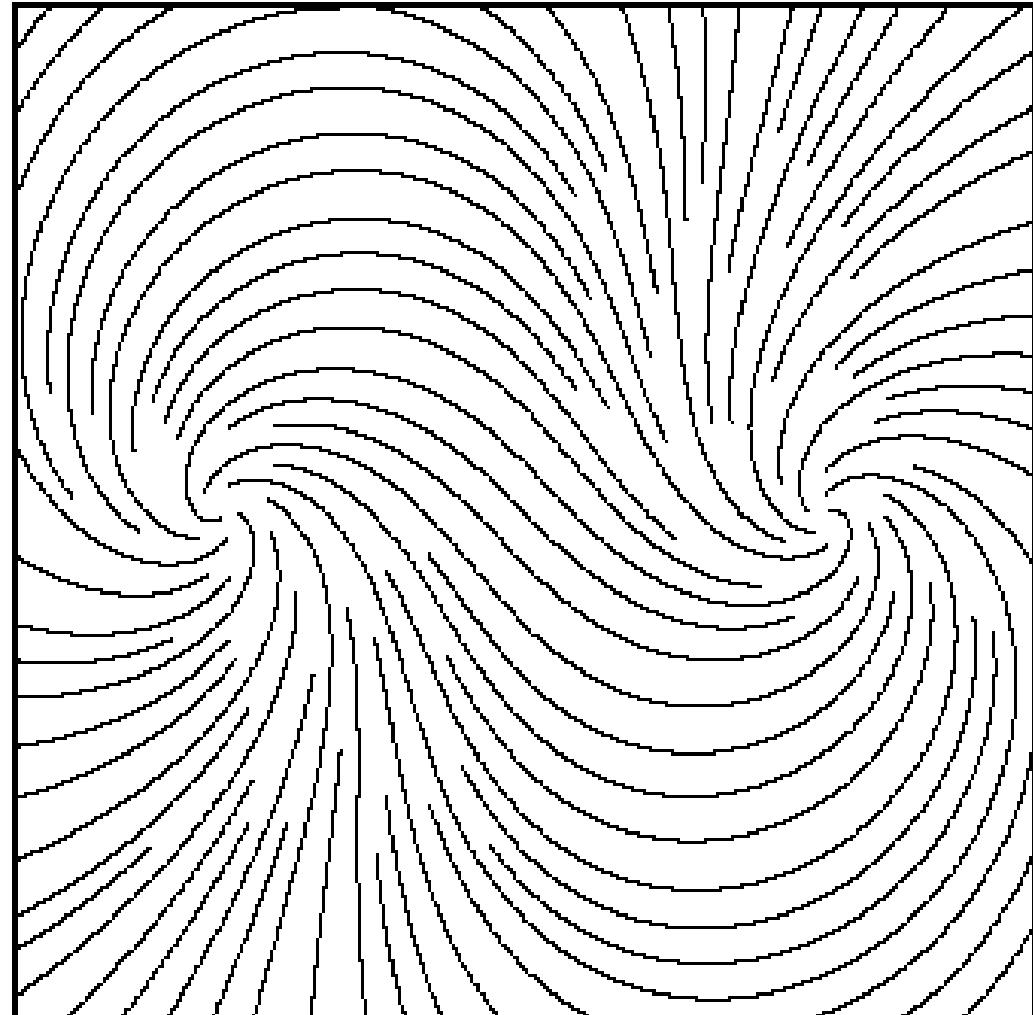
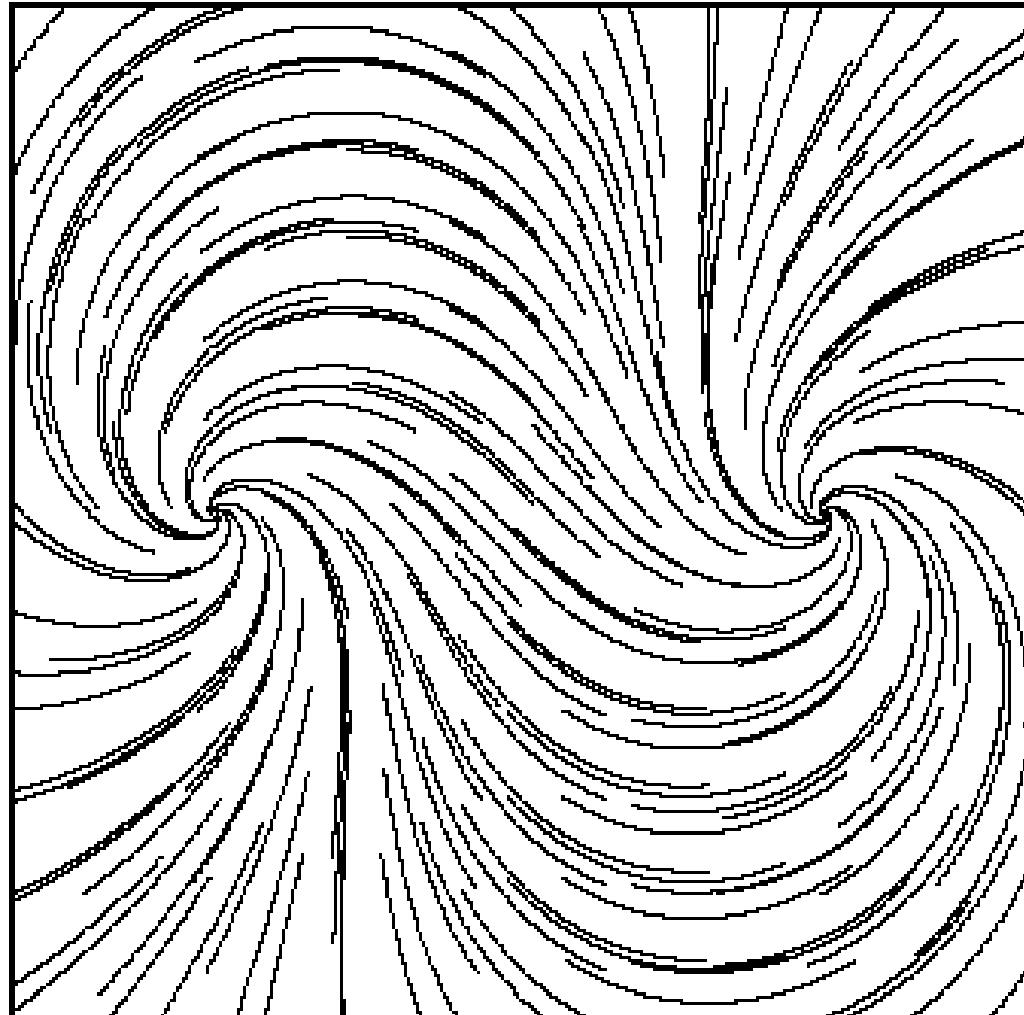


# Streamline Placement

in 2D

# Problem: Choice of Seed Points

- Streamline placement:
  - If regular grid used: very irregular result



# Overview of Algorithm

- Idea: streamlines should not get too close to each other
- Approach:
  - choose a seed point with distance  $d_{sep}$  from an already existing streamline
  - forward- and backward-integration until distance  $d_{test}$  is reached (or ...).
  - two parameters:
    - $d_{sep}$  ... start distance
    - $d_{test}$  ... minimum distance



# Algorithm – Pseudocode

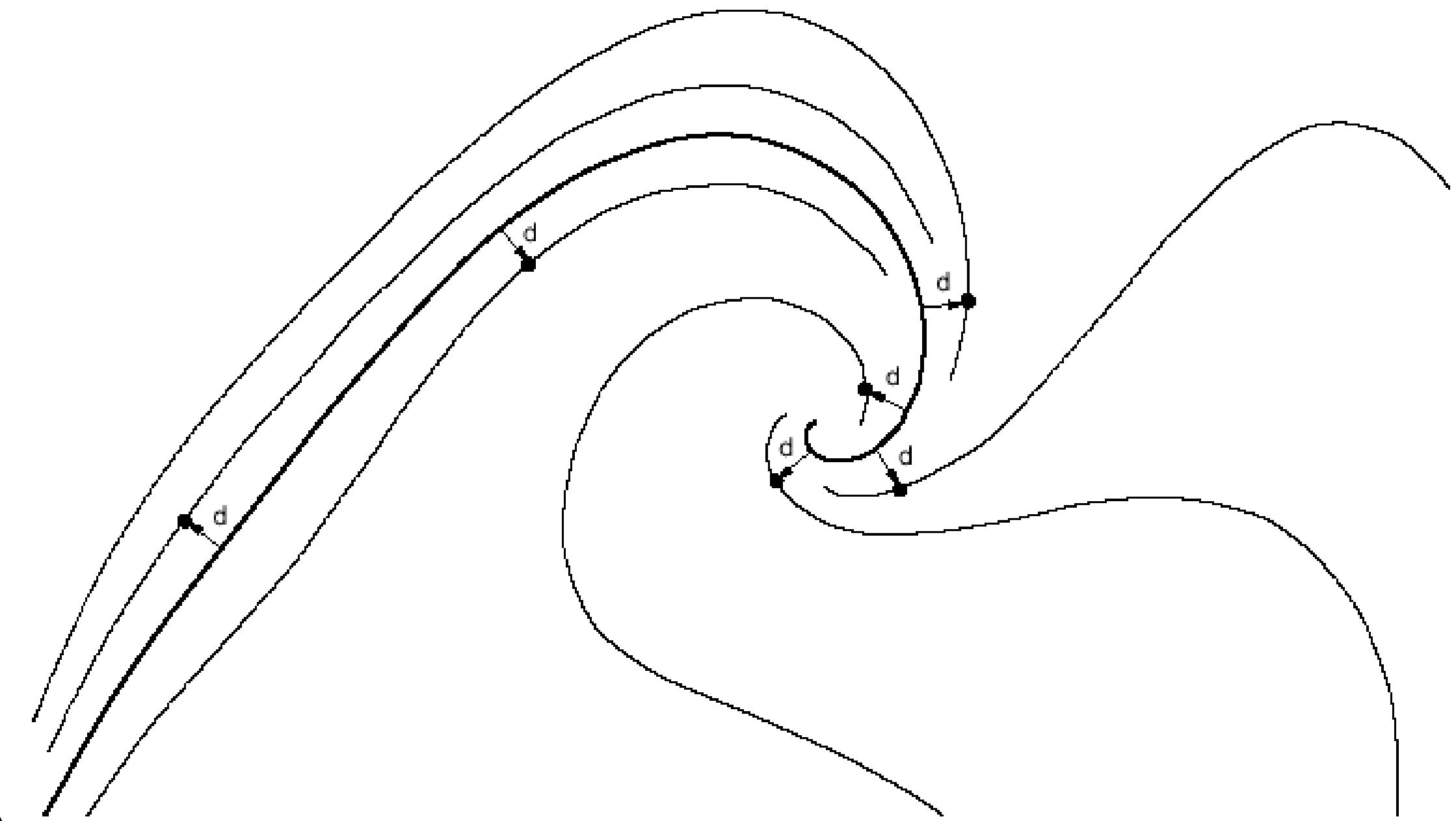
- Compute initial streamline, put it into a queue
- Initial streamline becomes current streamline
- WHILE not finished DO:
  - TRY: get new seed point which is  $d_{sep}$  away from current streamline
  - IF successful THEN compute new streamline and put to queue
  - ELSE IF no more streamline in queue THEN exit loop
  - ELSE next streamline in queue becomes current streamline



# Streamline Termination

- When to stop streamline integration:
  - when dist. to neighboring streamline  $\leq d_{\text{test}}$
  - when streamline leaves flow domain
  - when streamline runs into fixed point ( $v=0$ )
  - when streamline gets too near to itself
  - after a certain number of maximal steps

# New Streamlines



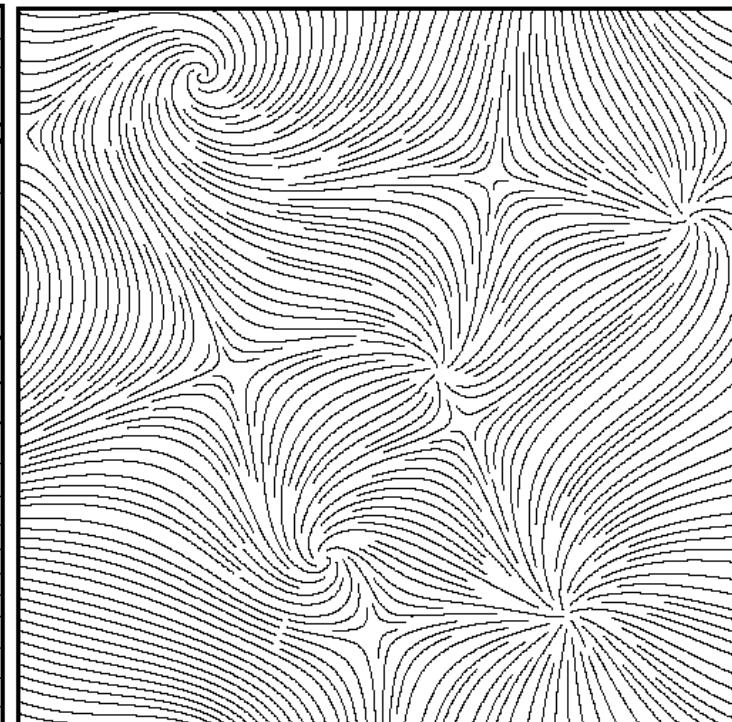
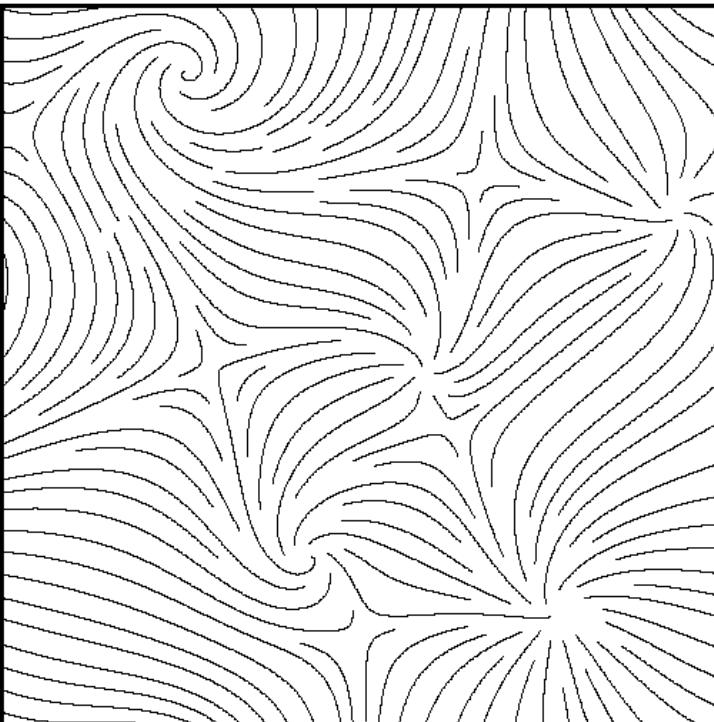
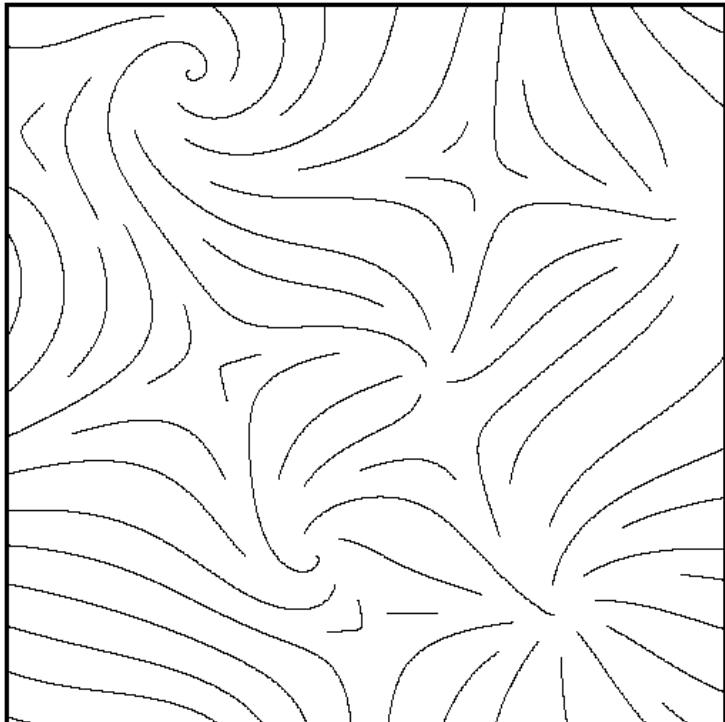
# Different Streamline Densities

- Variations of  $d_{sep}$  in rel. to image width:

6%

3%

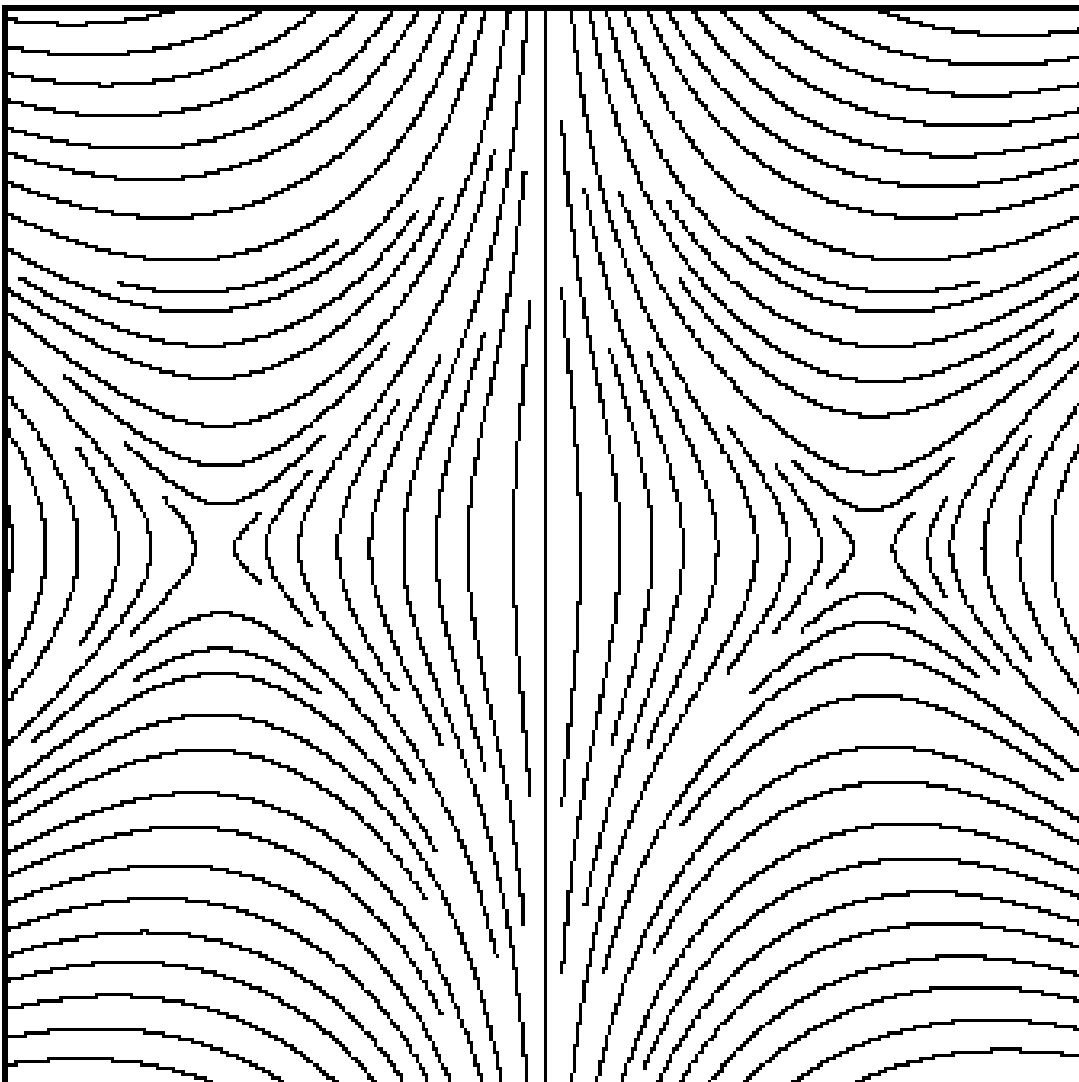
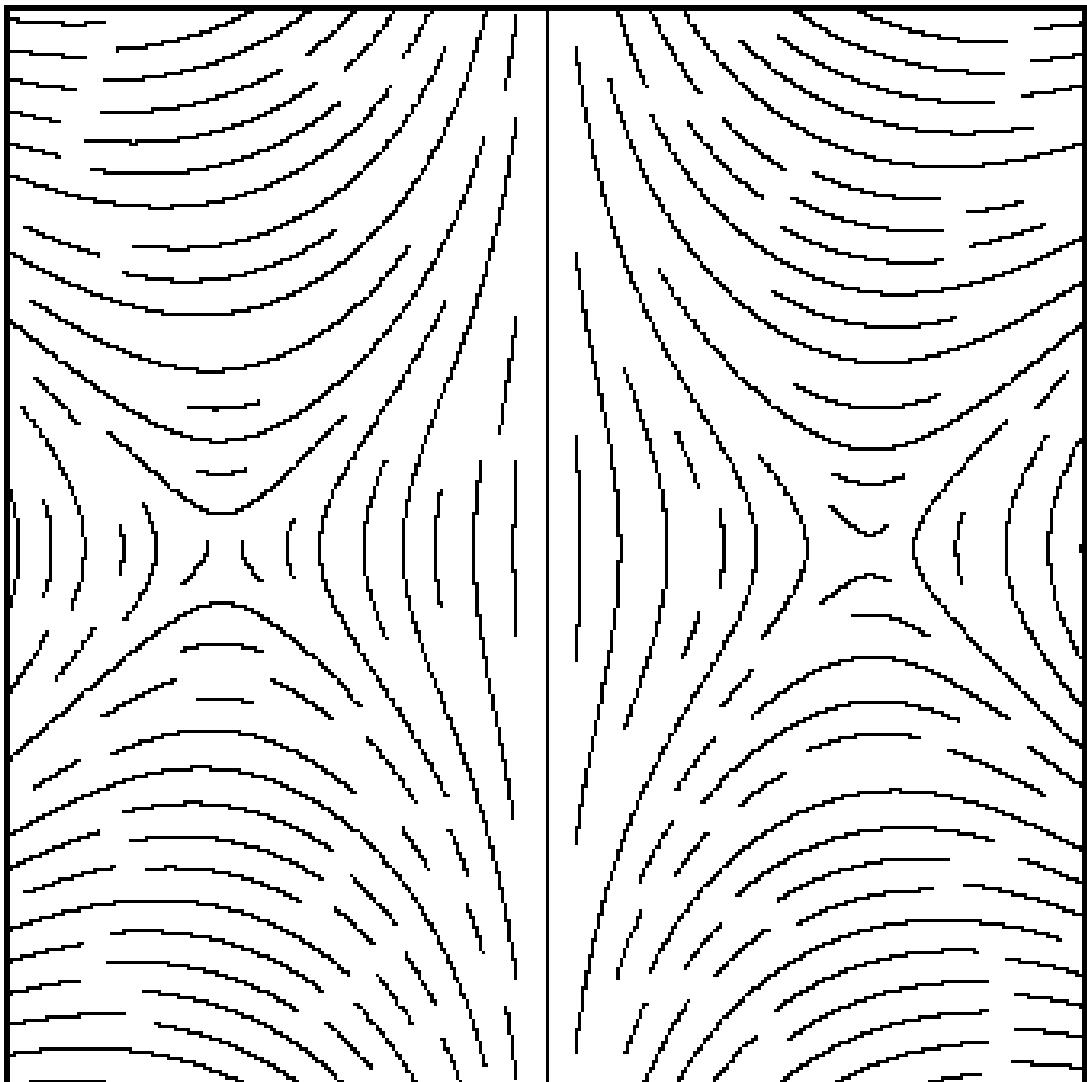
1.5%



# $d_{sep}$ vs. $d_{test}$

$$d_{test} = 0.9 \cdot d_{sep}$$

$$d_{test} = 0.5 \cdot d_{sep}$$



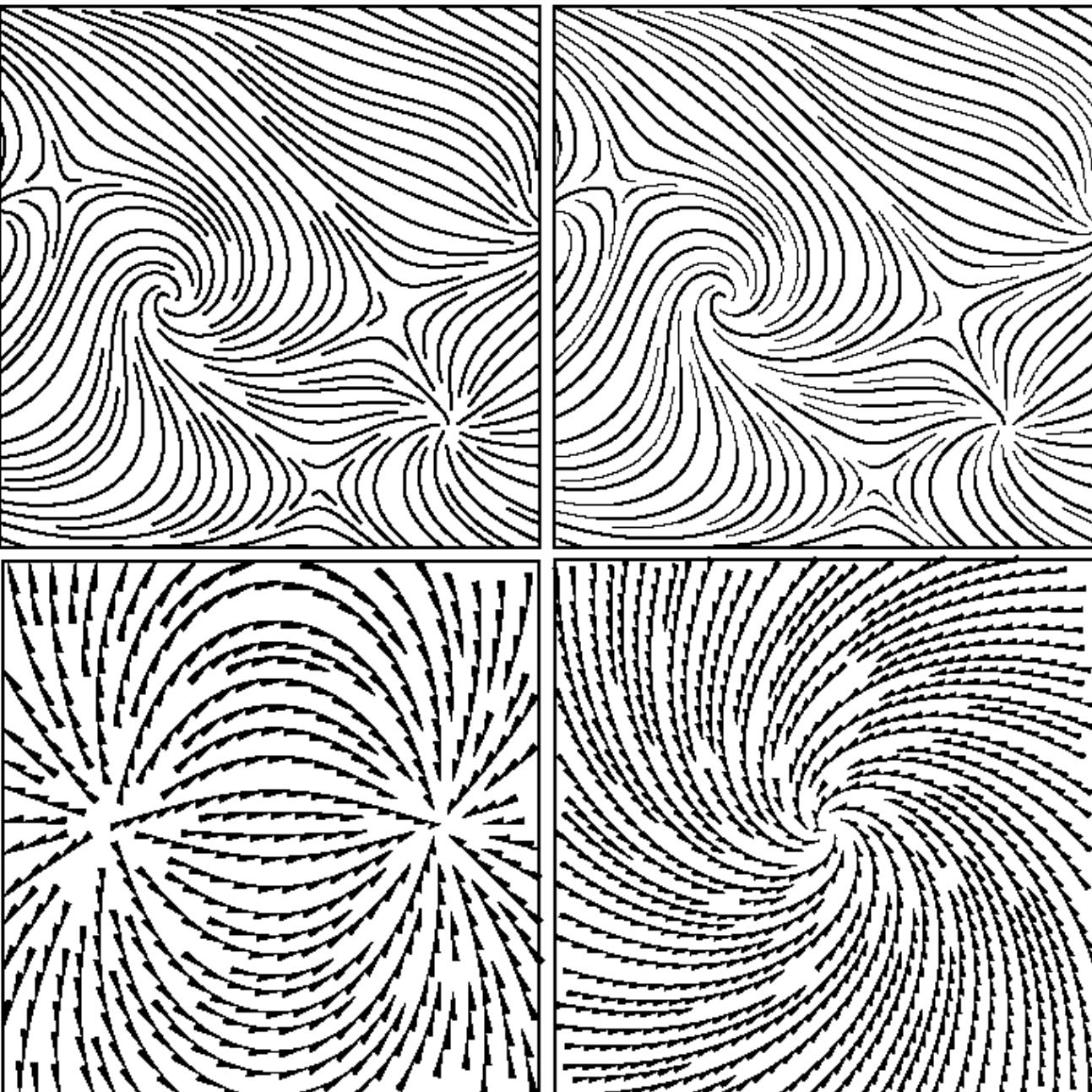
# Tapering and Glyphs

- Thickness in rel. to dist.

$$1.0 \quad \forall d \geq d_{sep}$$

$$\frac{d - d_{test}}{d_{sep} - d_{test}} \quad \forall d < d_{sep}$$

- Directional glyphs:

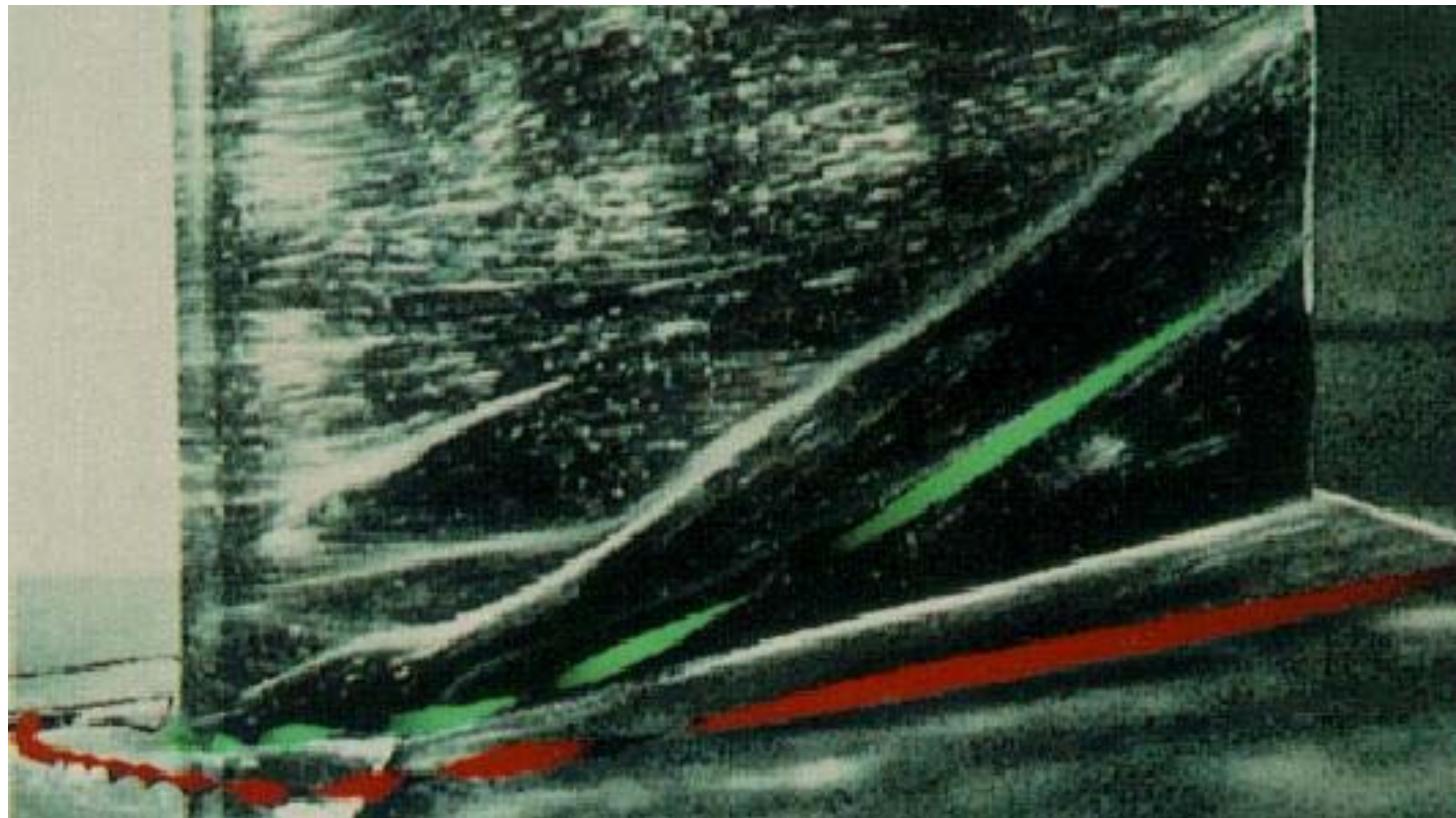
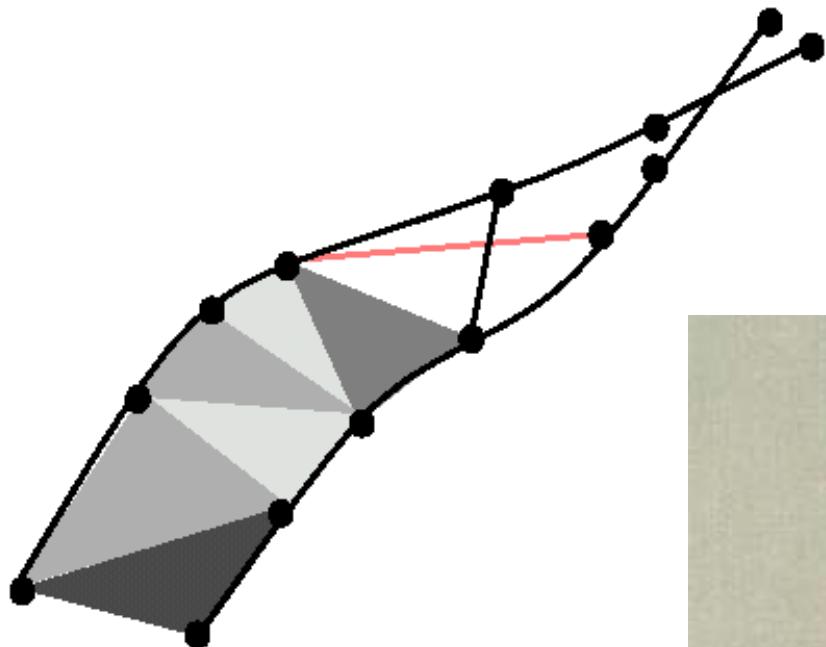


# Flow Visualization with Integral Objects

Streamribbons,  
Streamsurfaces,  
etc.

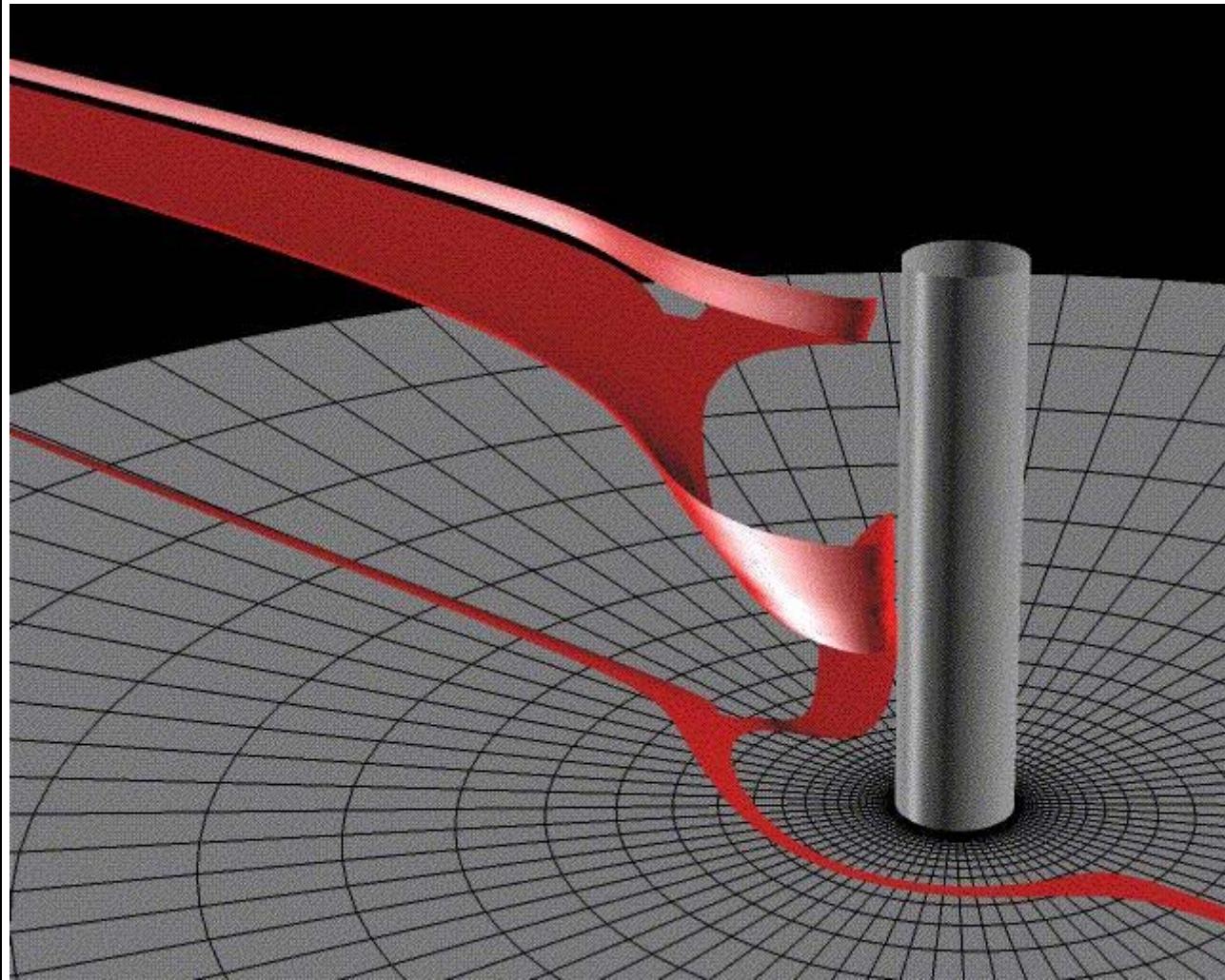
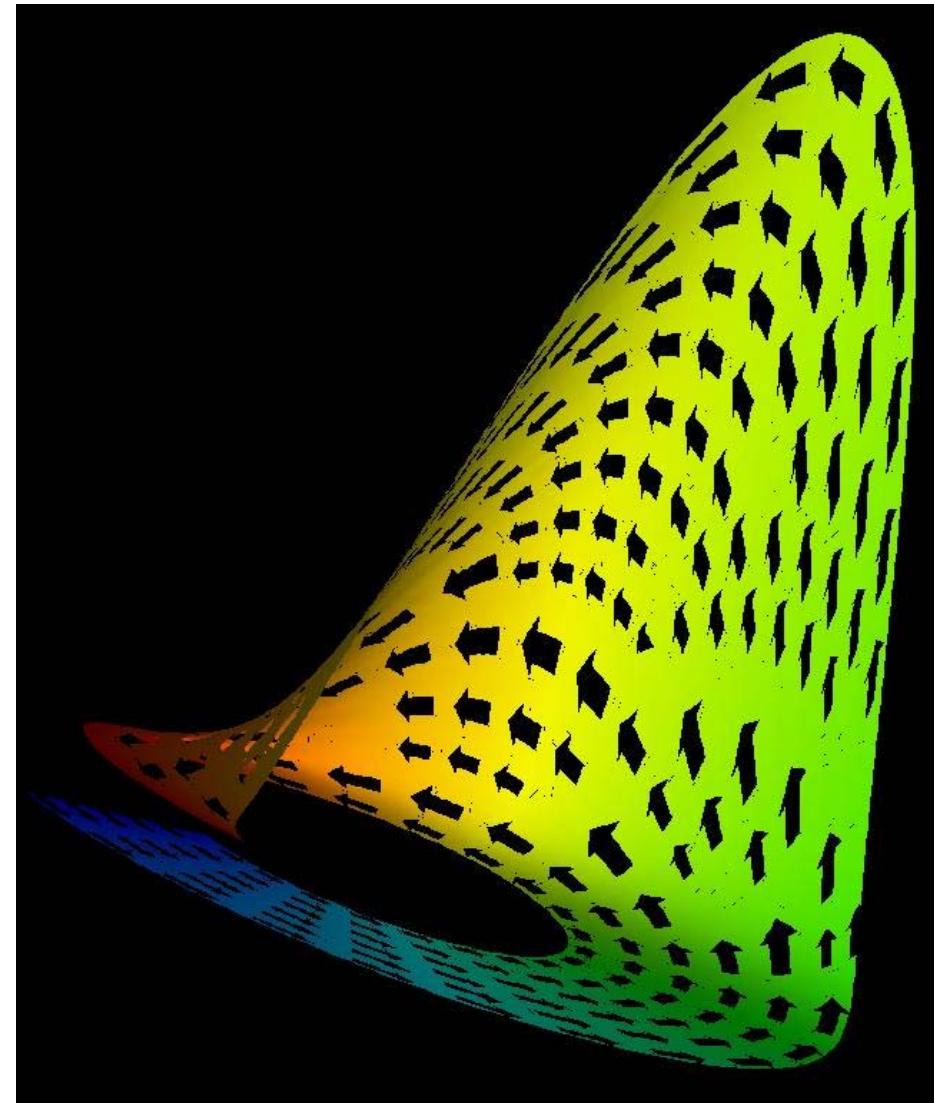
# Integral Objects in 3D 1/3

## ■ Streamribbons

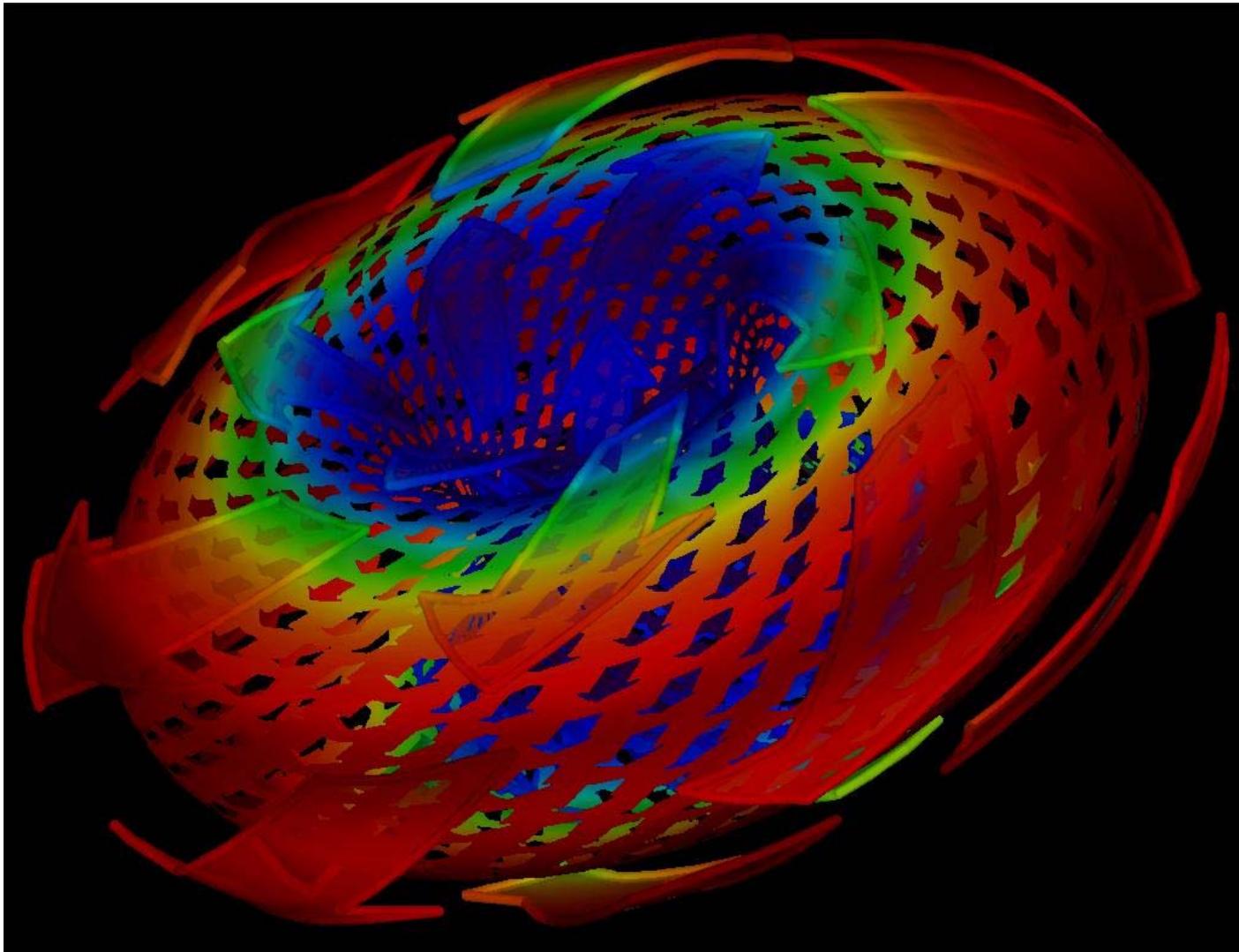
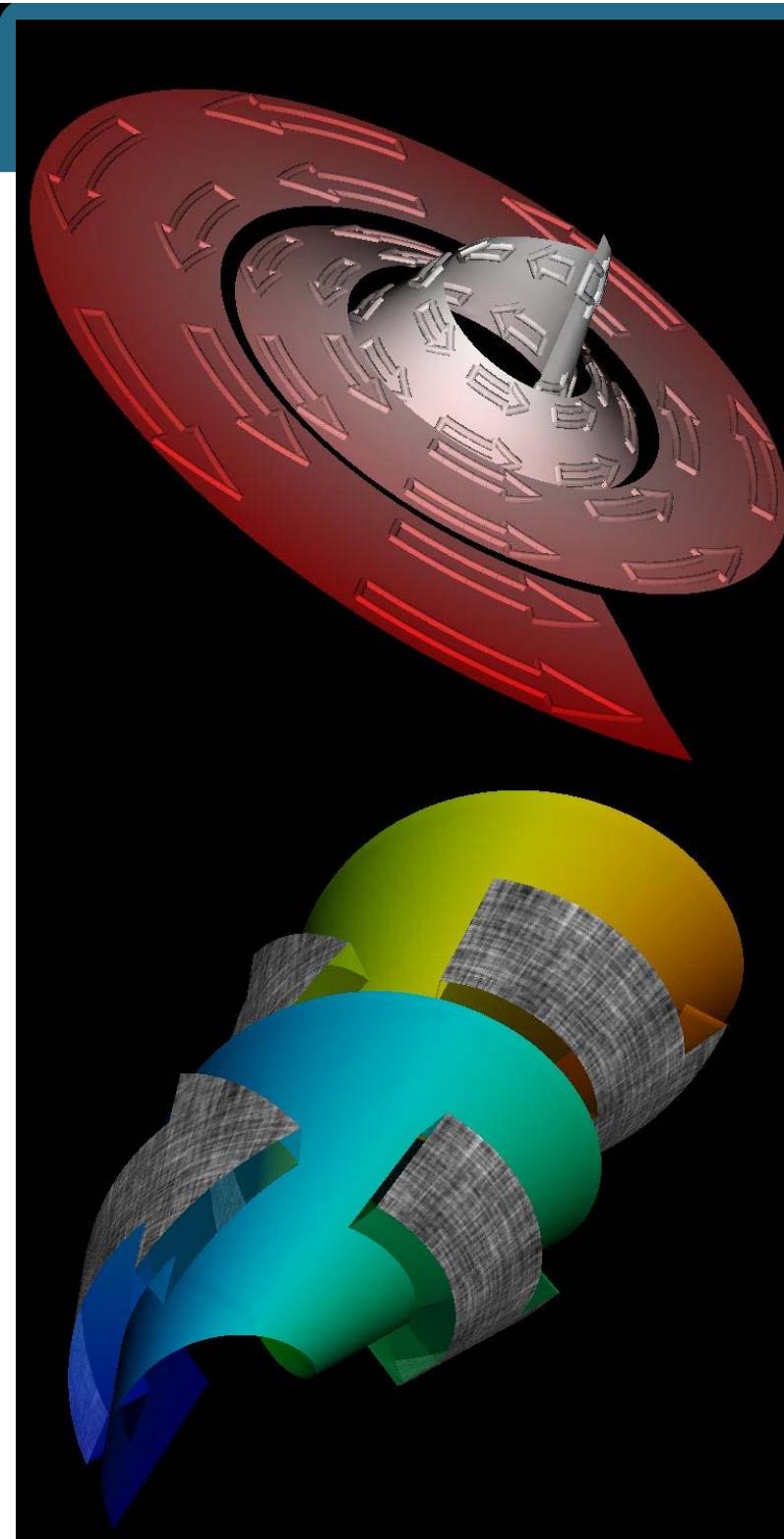


# Integral Objects in 3D 2/3

## ■ Streamsurfaces

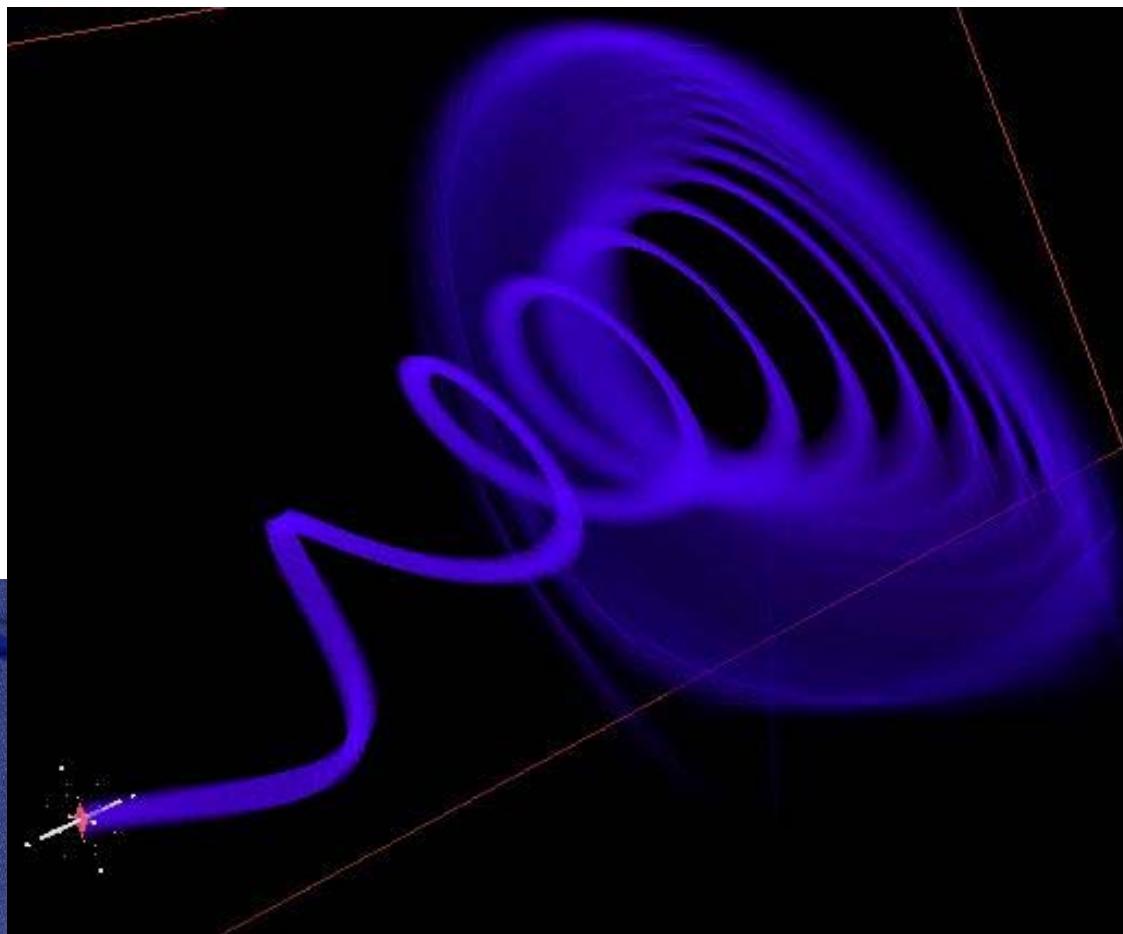


# Stream Arrows

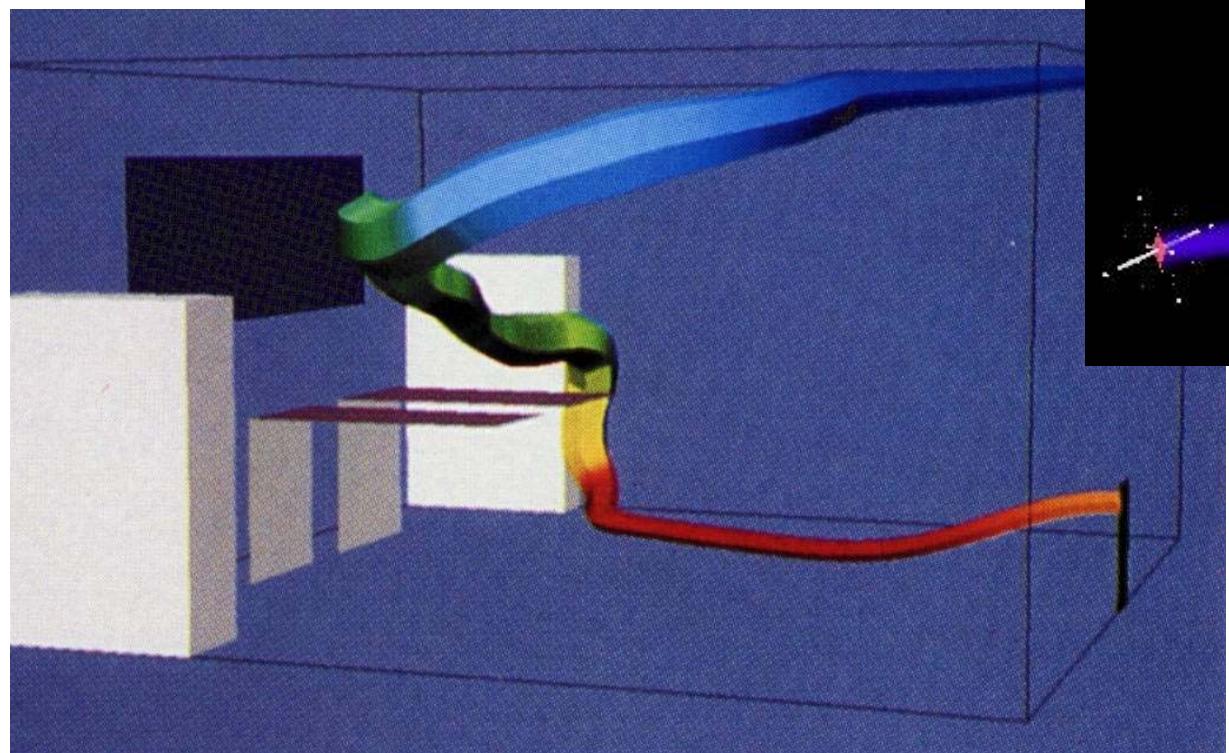


# Integral Objects in 3D 3/3

- Flow volumes ...



- vs. streamtubes  
(similar to streamribbon)



# Relation to Seed Objects

■ IntegralObj.	Dim.	SeedObj.	Dim.
Streamline, ...	1D	Point	0D
Streamribbon	1D++	Point+pt.	0D+0D
Streamtube	1D++	Pt.+cont.	0D+1D
Streamsurface	2D	Curve	1D
Flow volume	3D	Patch	2D

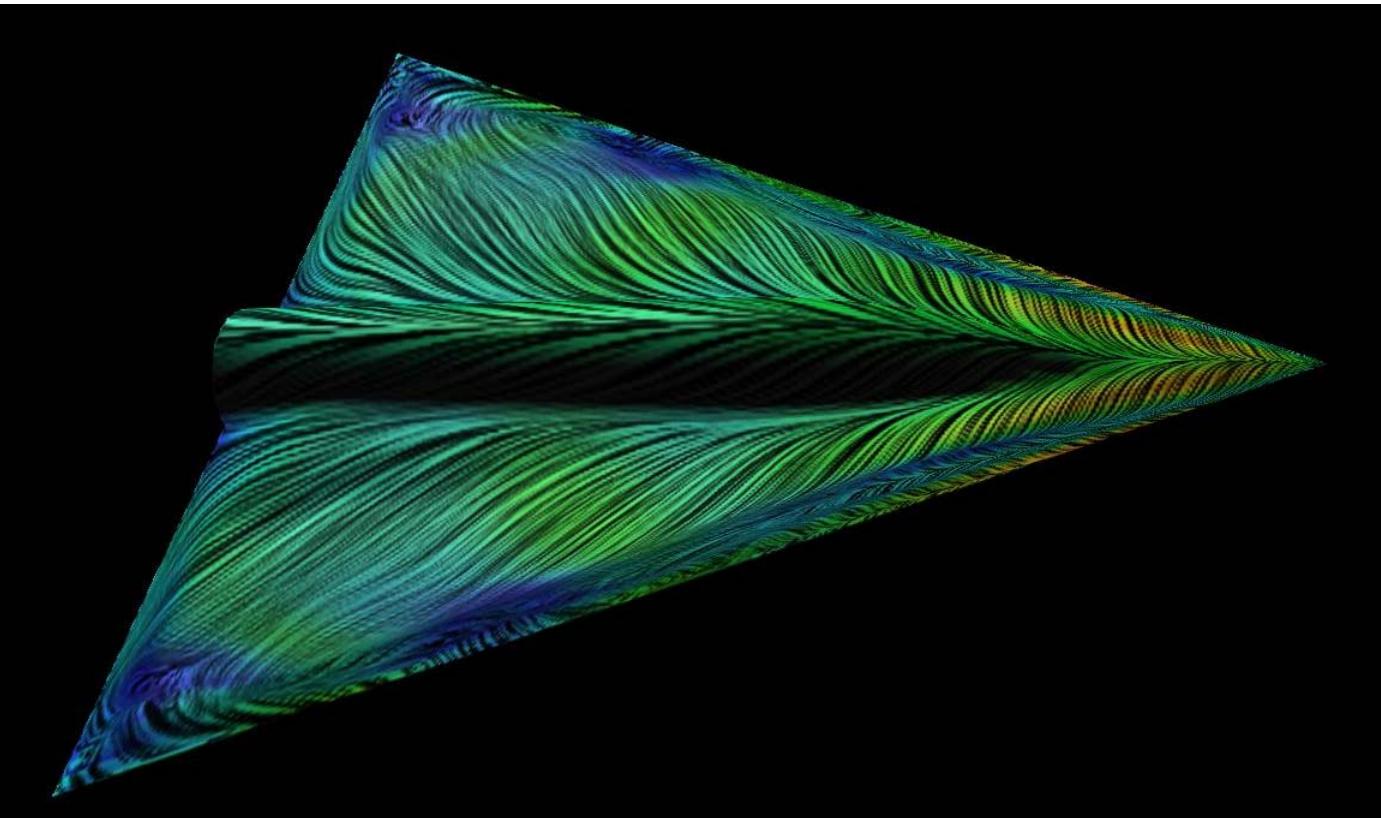
# Line Integral Convolution

Flow Visualization  
in 2D or on surfaces

# LIC – Introduction

## ■ Aspects:

- goal: general overview of flow
- Approach: usage of textures
- Idea: flow  $\Leftrightarrow$  visual correlation
- Example:



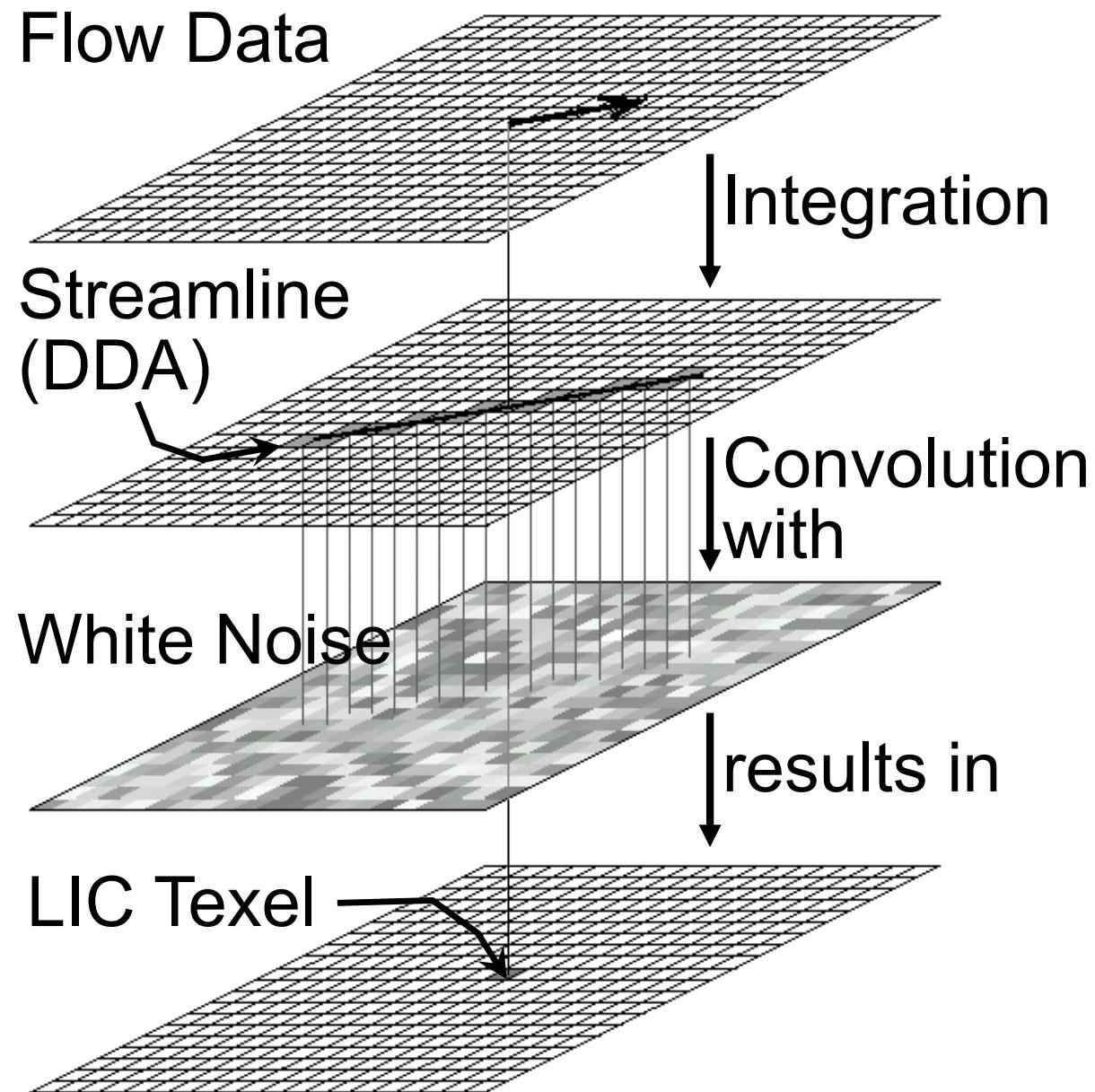
# LIC – Approach

- LIC idea:
  - for every texel: let the texture value...
    - ... correlate with neighboring texture values along the flow (in flow direction)
    - ... *not* correlate with neighboring texture values across the flow (normal to flow dir.)
  - result:  
along streamlines the texture values are correlated  $\Rightarrow$  visually coherent!
  - approach: “smudge” white noise (no a priori correlations) along flow

# LIC – Steps

## ■ Calculation of a texture value:

- look at streamline through point
- filter white noise along streamline



# LIC – Convolution with Noise

## ■ Calculation of LIC texture:

- input 1: flow data  $\mathbf{v}(\mathbf{x})$ :  $\mathbb{R}^n \rightarrow \mathbb{R}^n$ , analytically or interpolated
- input 2: white noise  $n(\mathbf{x})$ :  $\mathbb{R}^n \rightarrow \mathbb{R}^1$ , normally precomputed as texture
- streamline  $\mathbf{s}_x(u)$  through  $\mathbf{x}$ :  $\mathbb{R}^1 \rightarrow \mathbb{R}^n$ ,  
$$\mathbf{s}_x(u) = \mathbf{x} + \text{sgn}(u) \cdot \int_{0 \leq t \leq |u|} \mathbf{v}(\mathbf{s}_x(\text{sgn}(u) \cdot t)) dt$$
- input 3: filter  $h(t)$ :  $\mathbb{R}^1 \rightarrow \mathbb{R}^1$ , e.g., Gauss
- result: texture value  $\text{lic}(\mathbf{x})$ :  $\mathbb{R}^n \rightarrow \mathbb{R}^1$ ,  
$$\text{lic}(\mathbf{x}) = \text{lic}(\mathbf{s}_x(0)) = \int n(\mathbf{s}_x(u)) \cdot h(-u) du$$

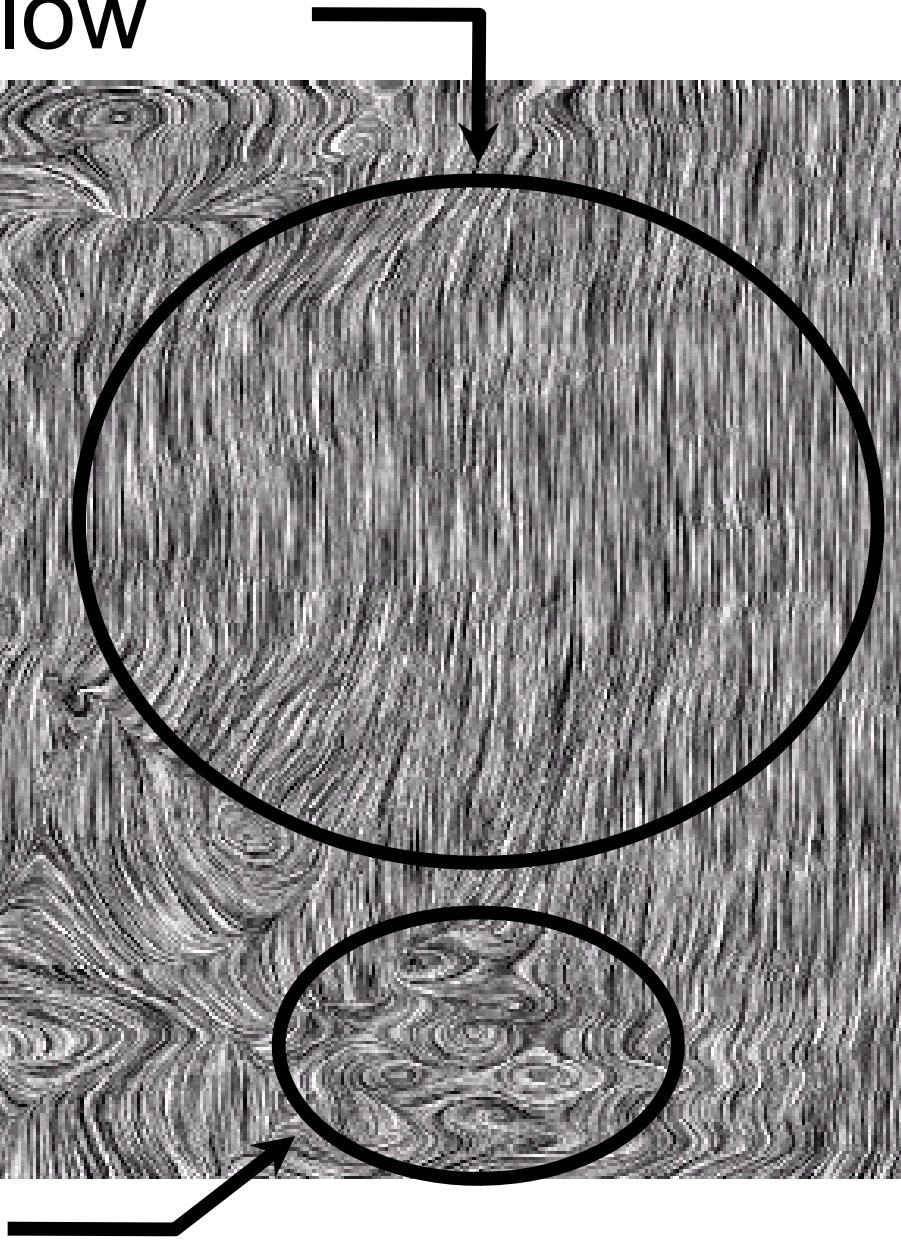


# More Explanation

- So:
  - LIC –  $\text{lic}(\mathbf{x})$  – is a convolution of
    - white noise  $n$  (or ...)
    - and a smoothing filter  $h$  (e.g. a Gaussian)
  - The noise texture values are picked up along streamlines  $\mathbf{s}_x$  through  $\mathbf{x}$

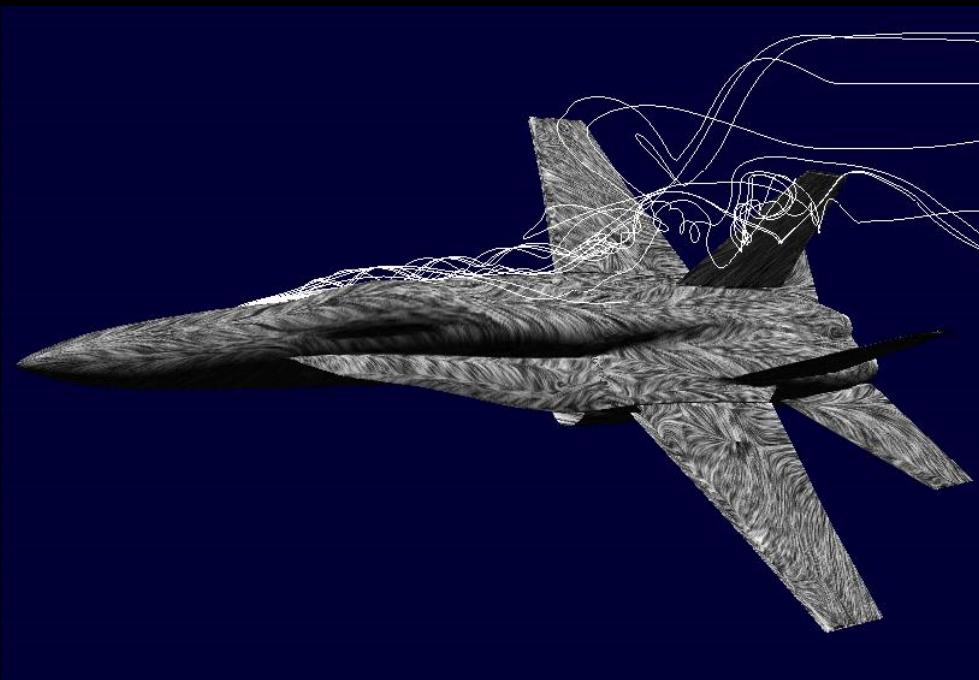
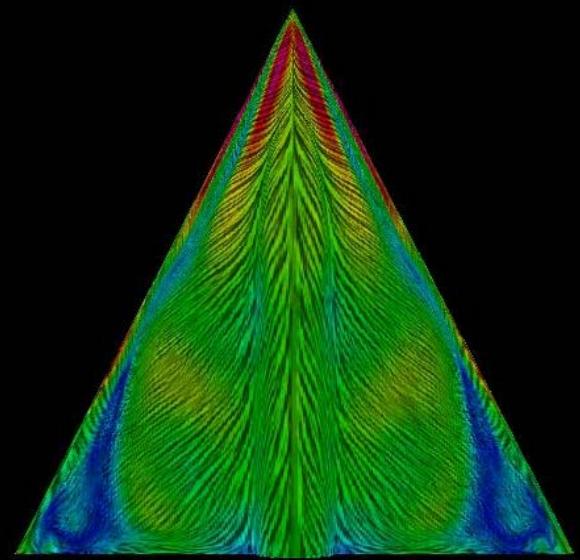
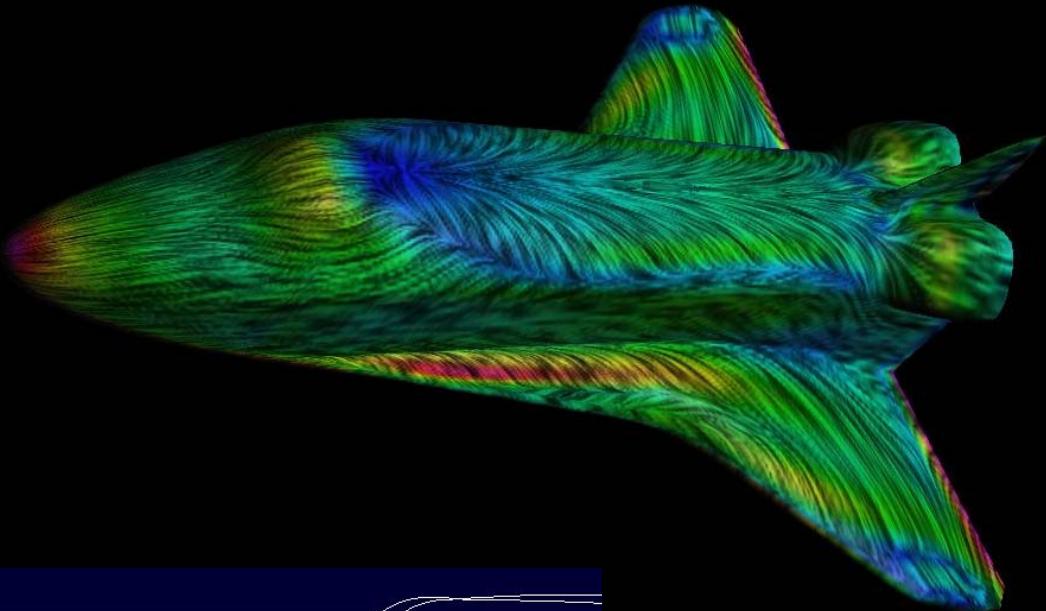
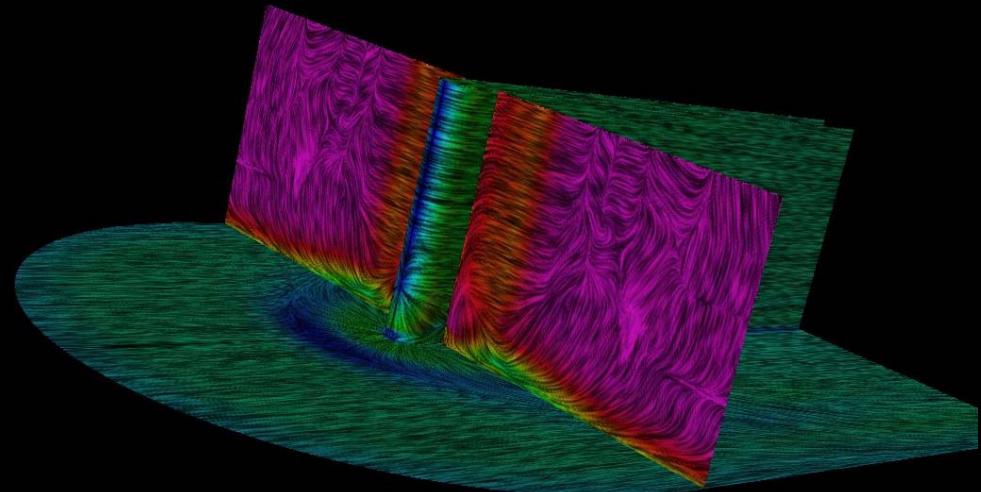
# LIC – Example in 2D

quite laminar flow



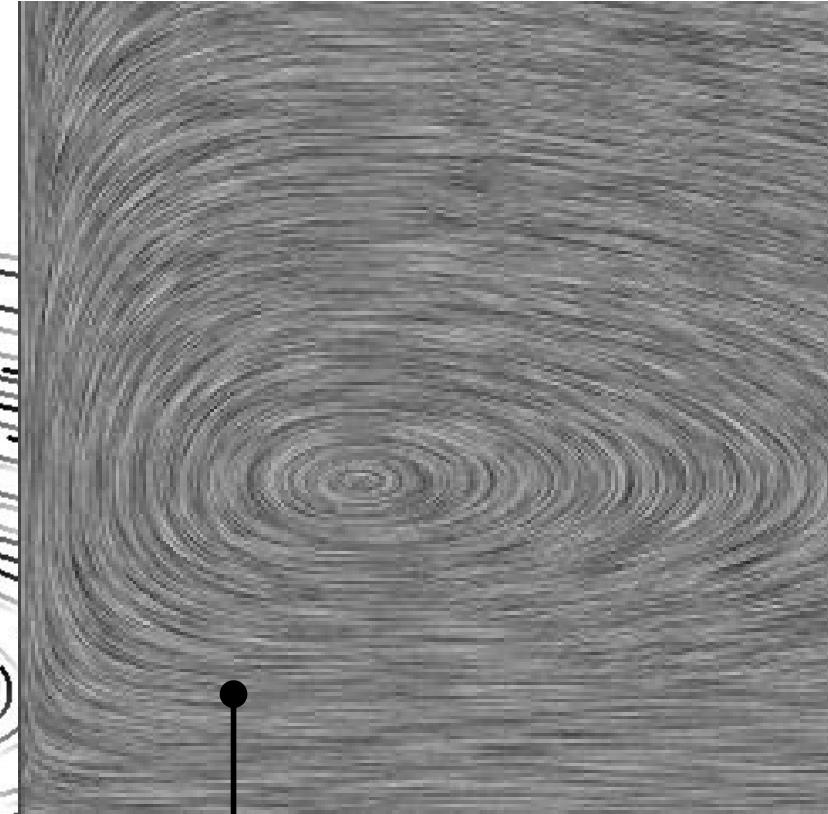
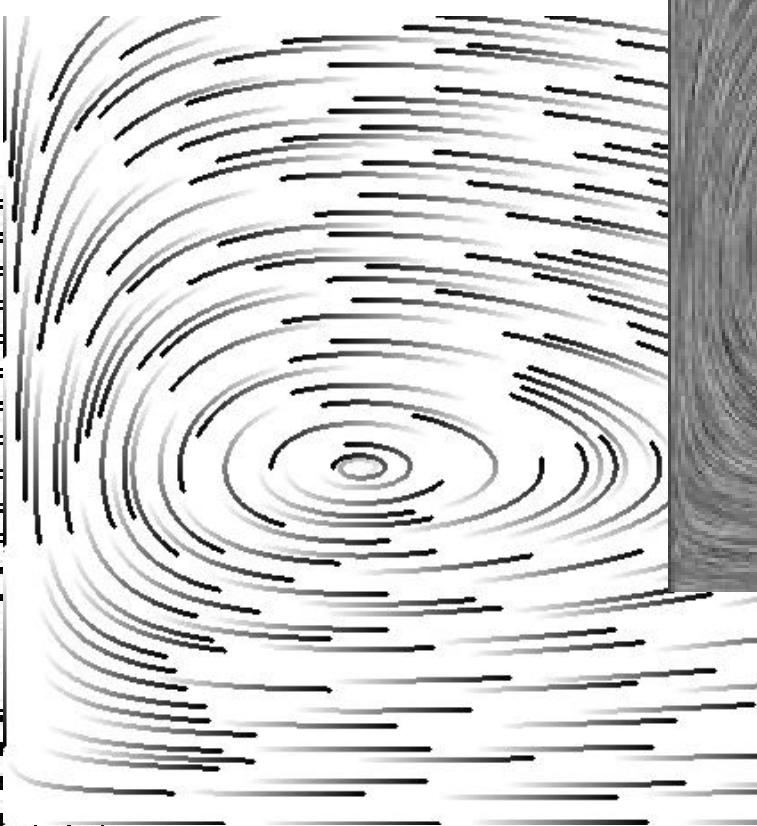
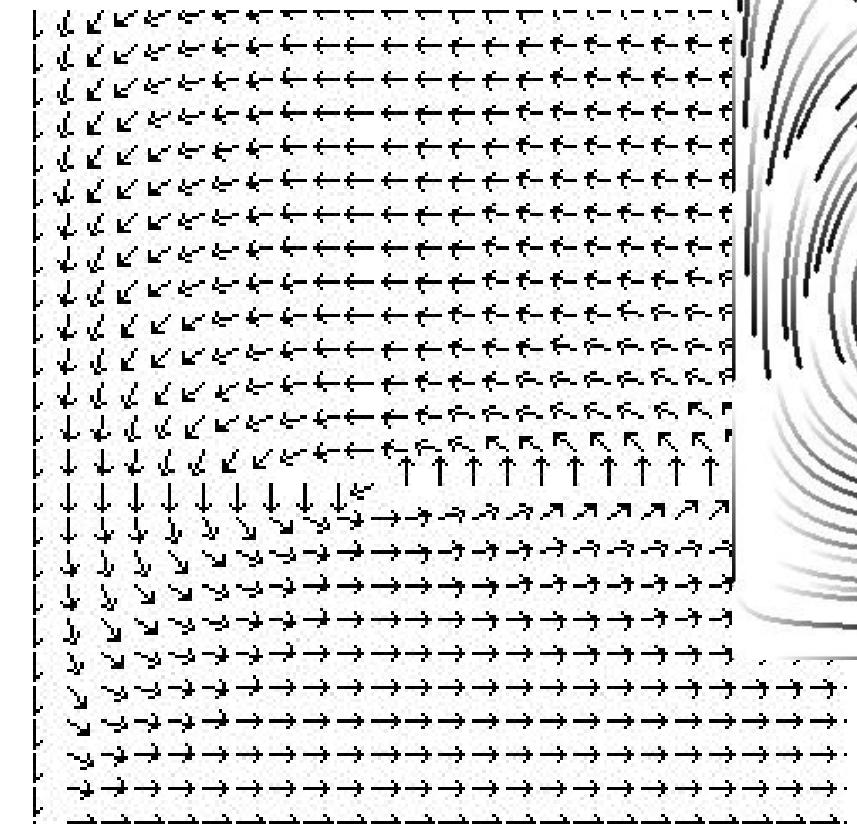
quite turbulent flow

# LIC – Examples on Surfaces



# Arrows vs. StrLines vs. Textures

- Streamlines: selective
- Arrows: well..

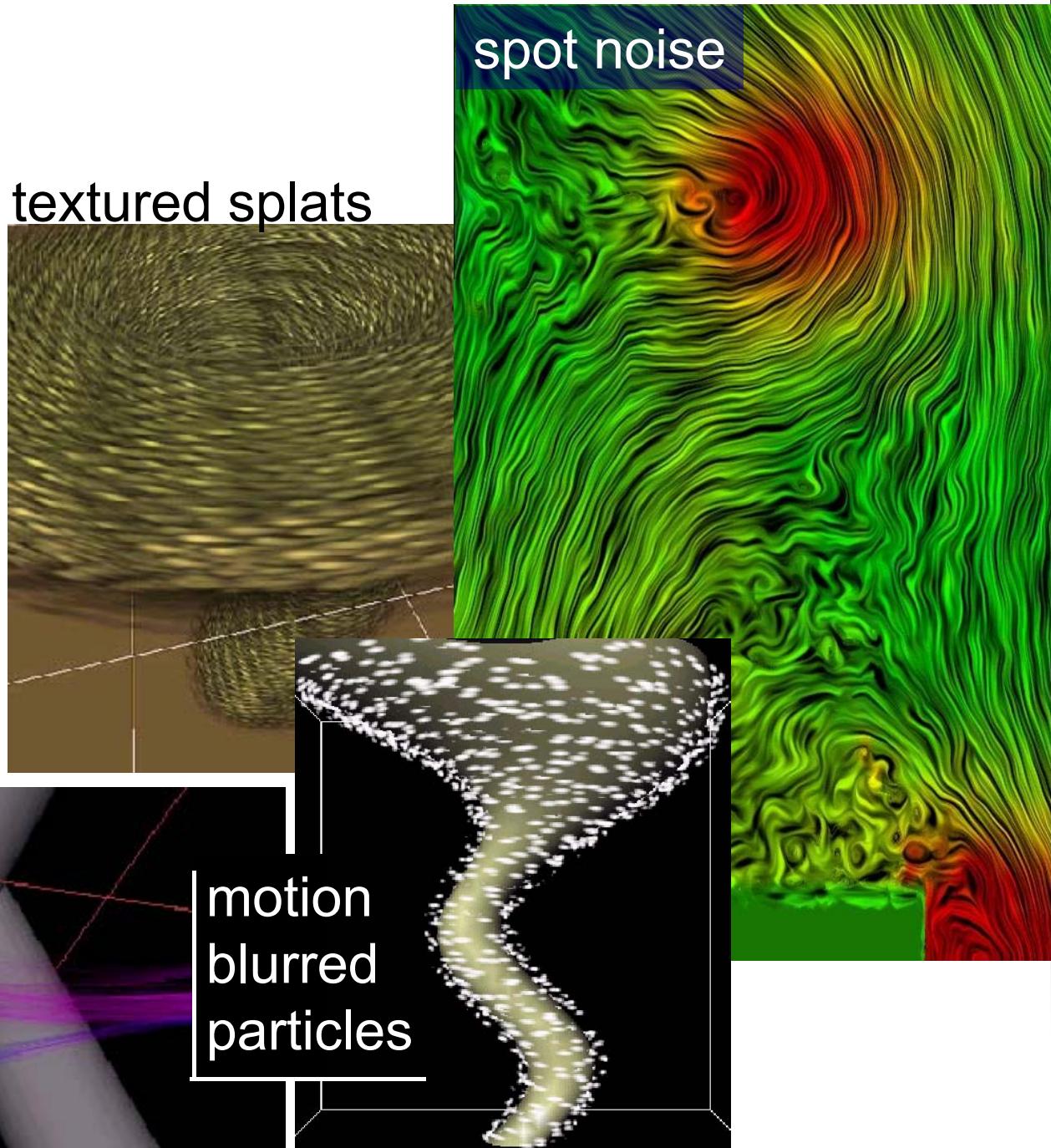


Textures:  
2D-filling

# Alternatives to LIC

## ■ Similar approaches:

- spot noise
- vector kernel
- line bundles/splats
- textured splats
- particle systems
- flow volumes
- texture advection

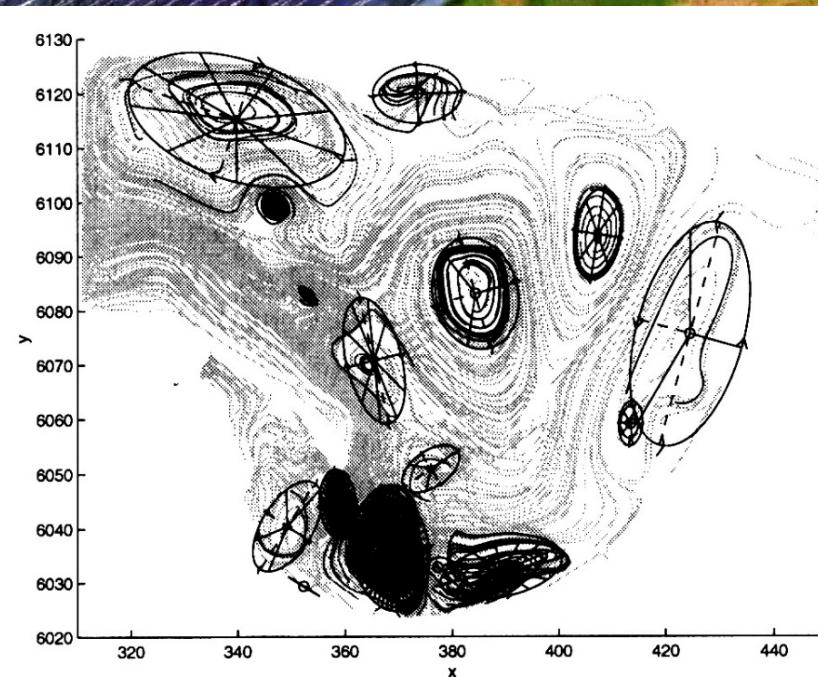
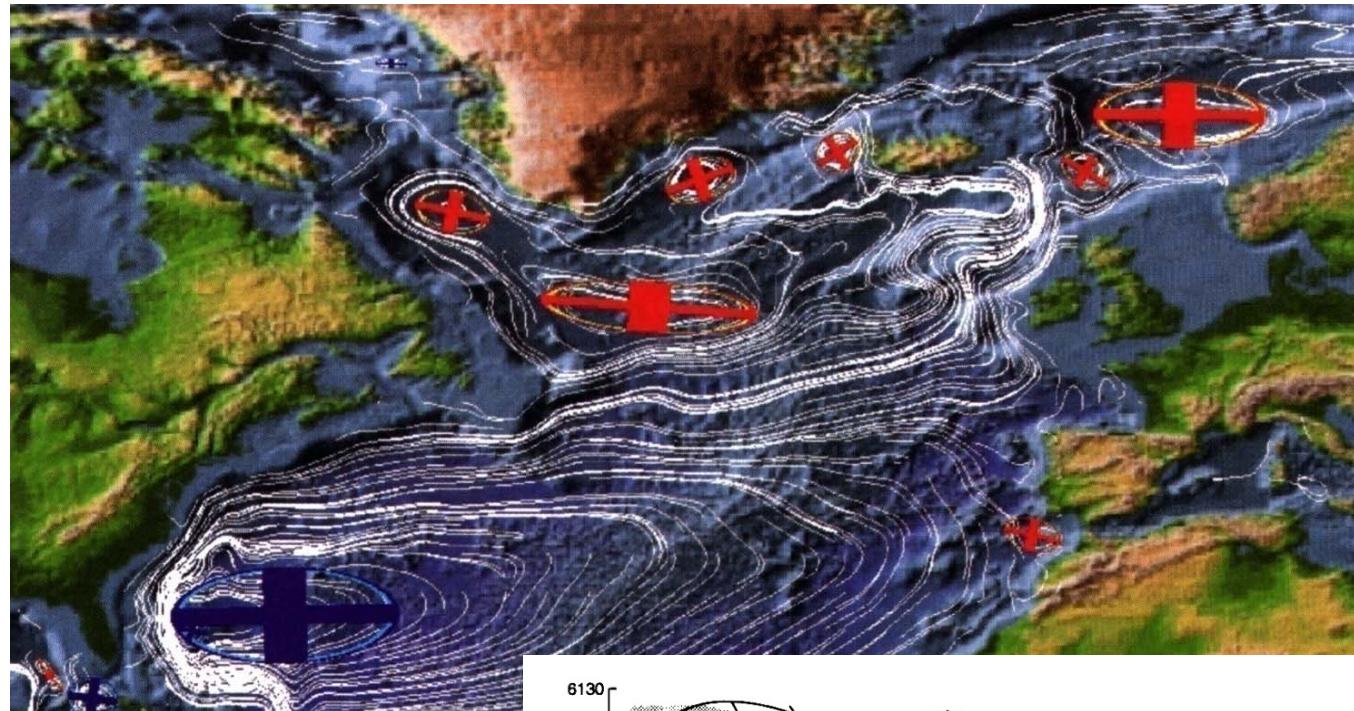
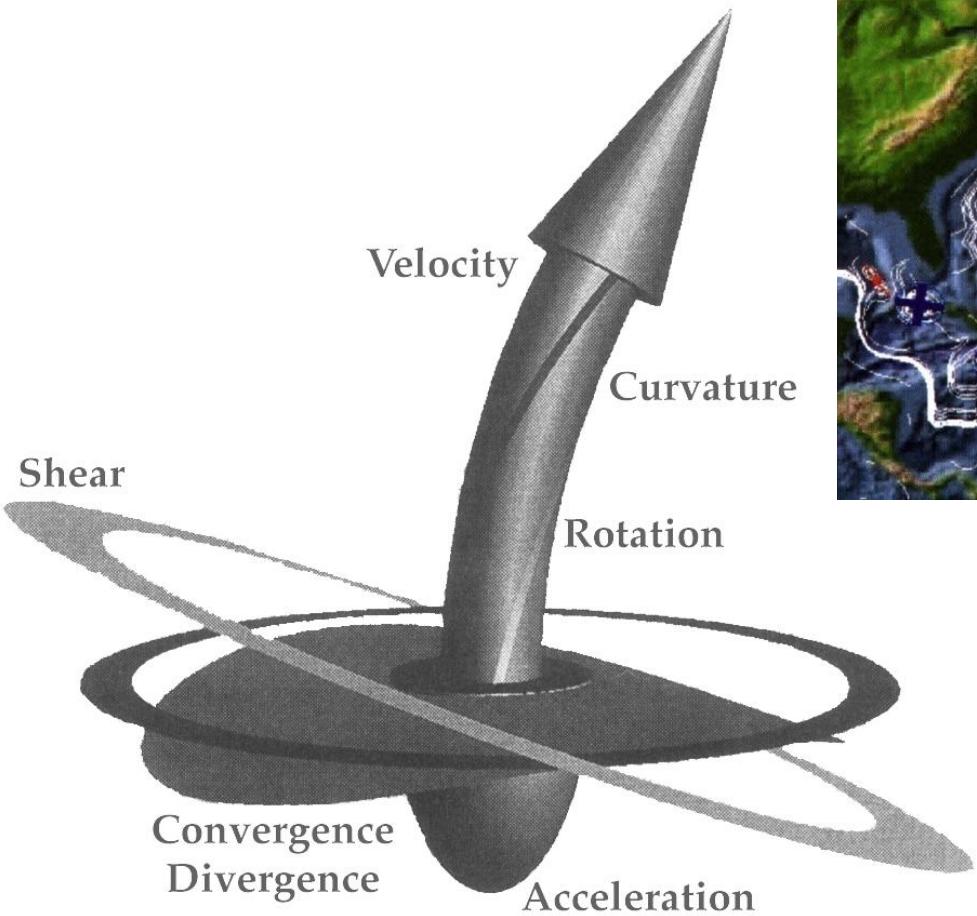


Flow Visualization  
dependent on local props.

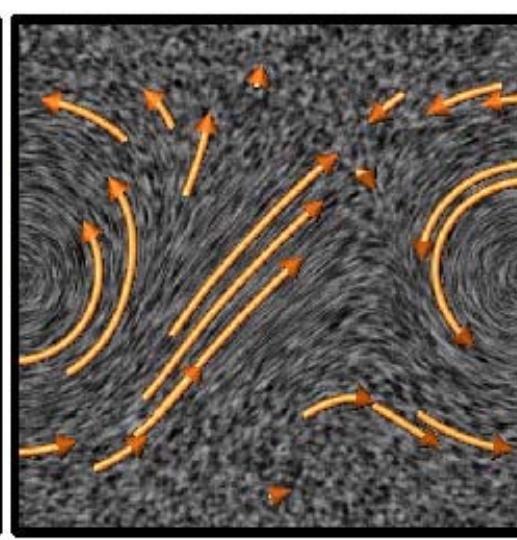
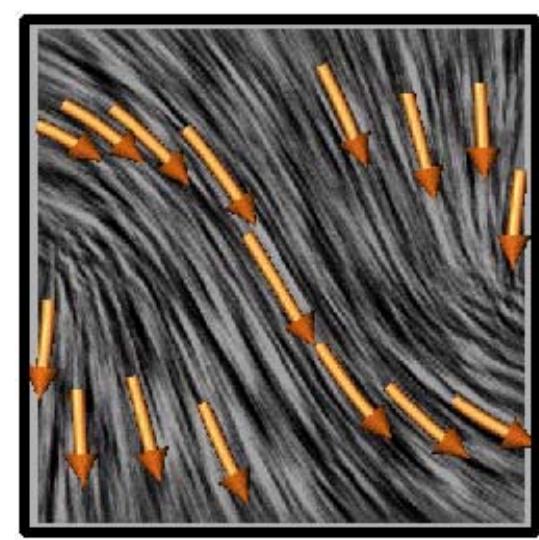
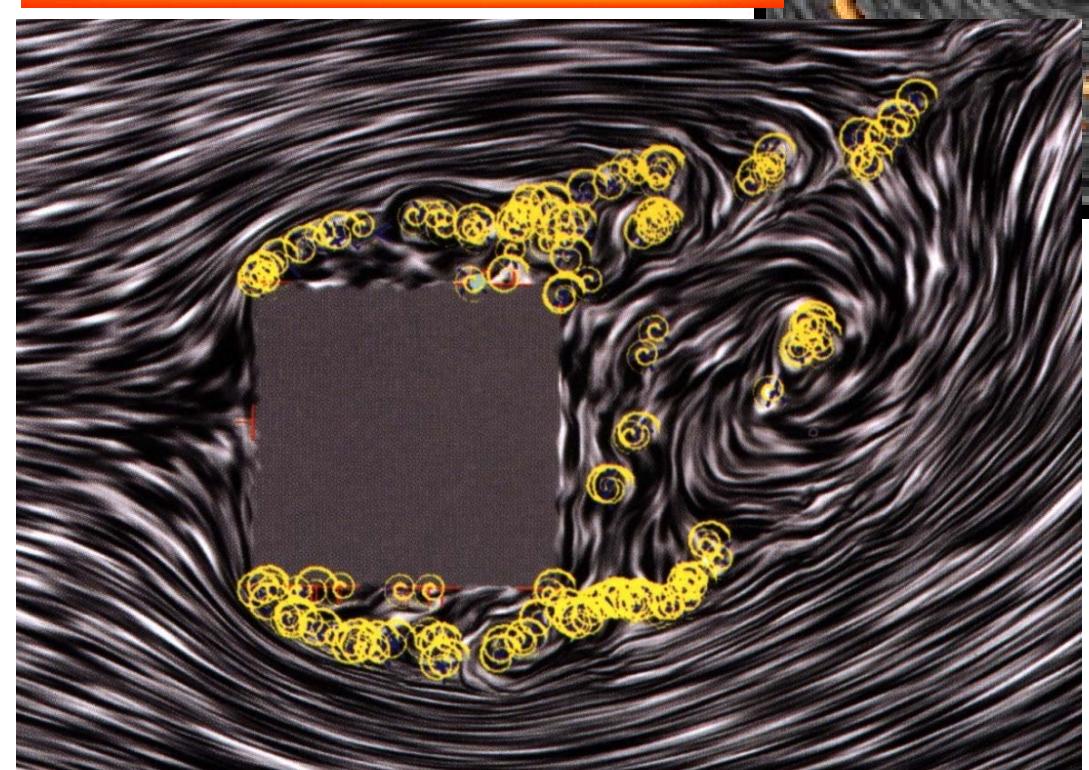
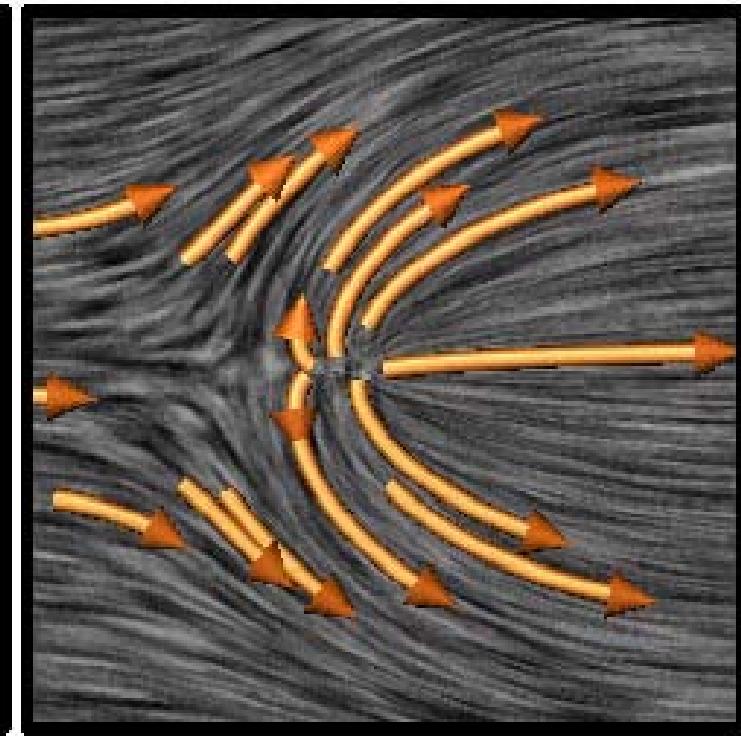
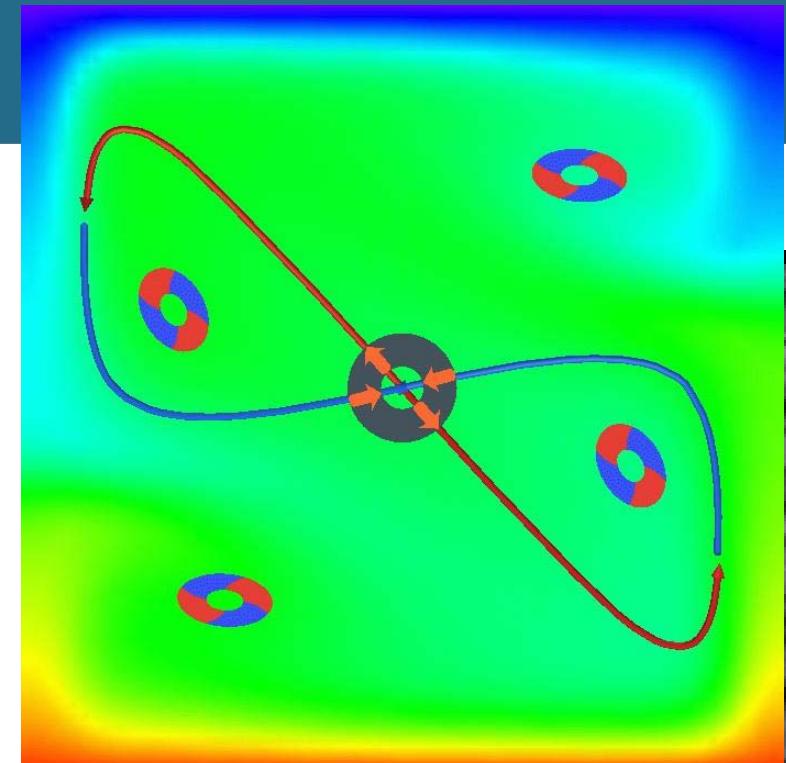
Visualization of  $\nabla v$

# Glyphs resp. Icons

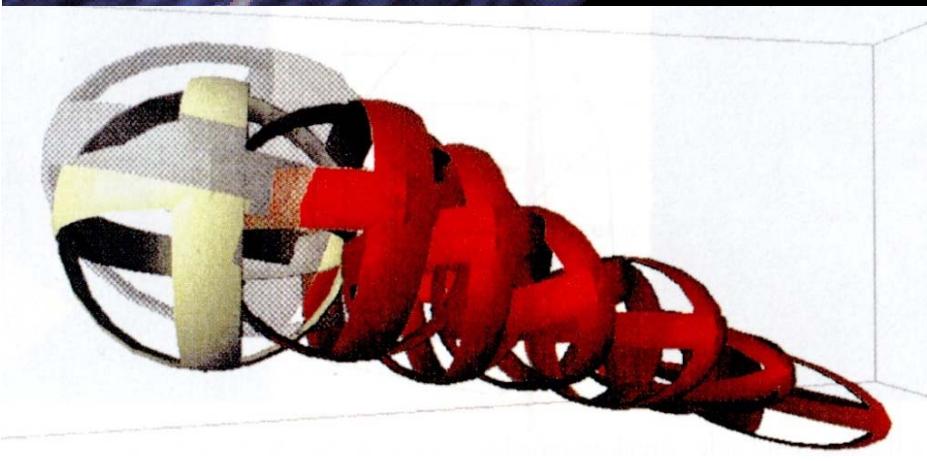
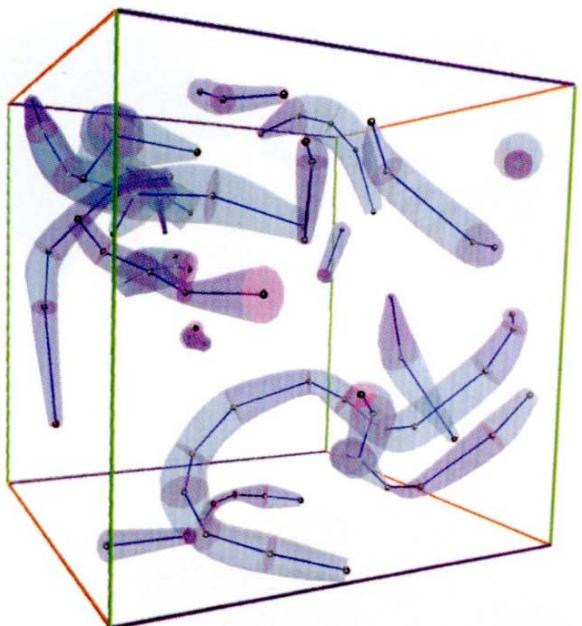
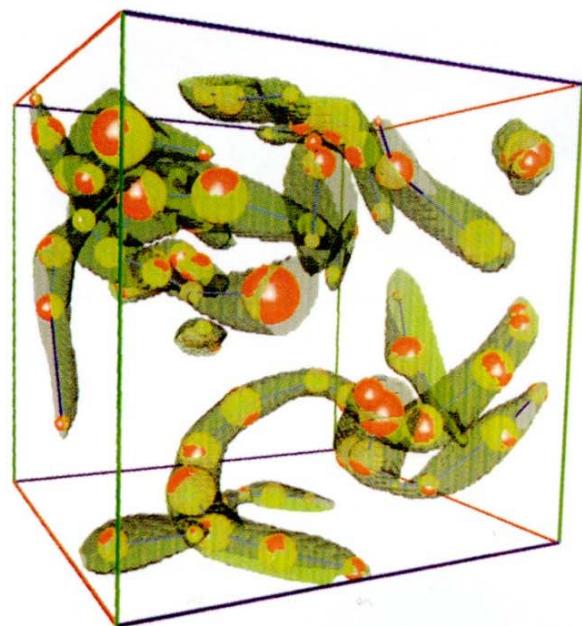
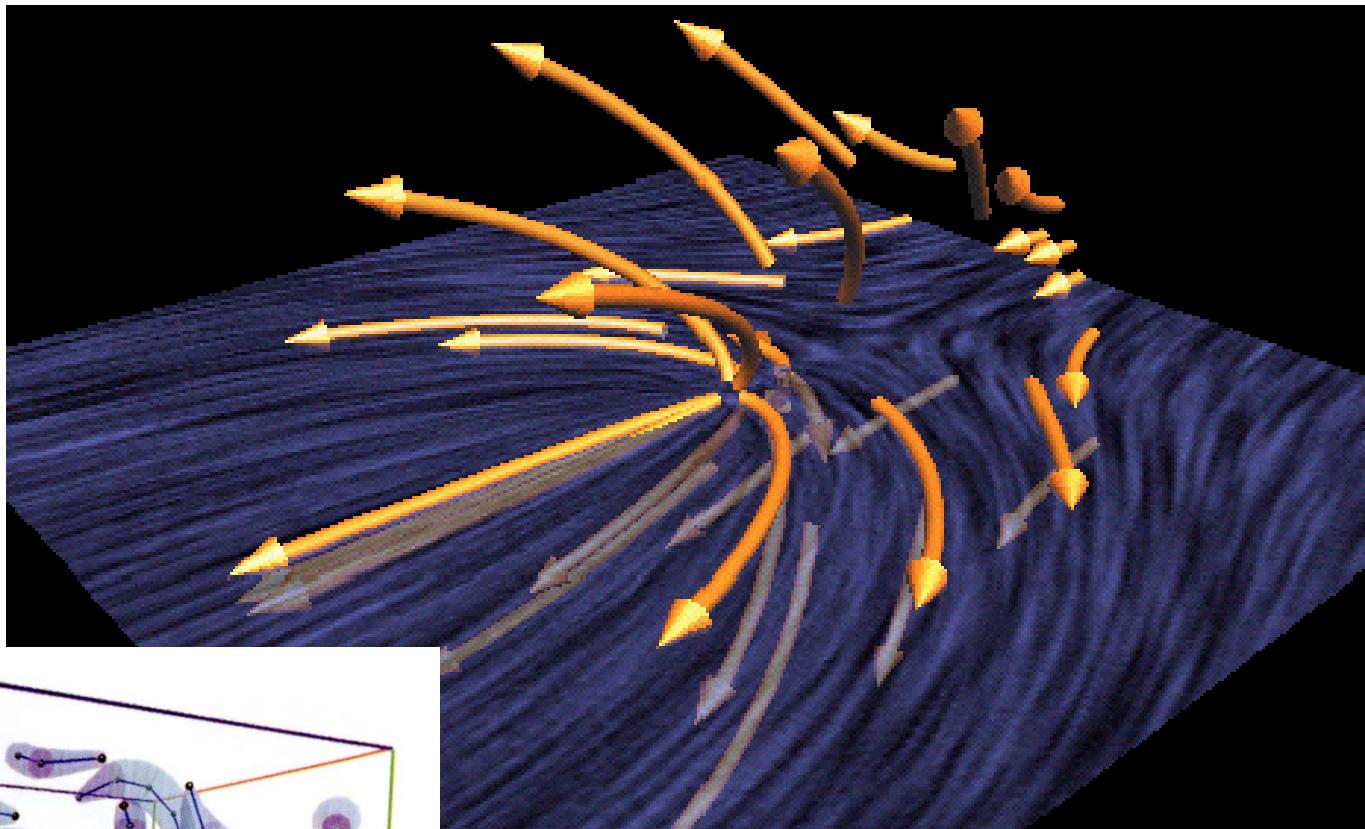
- Local / topological properties



# Icons in 2D



# Icons & Glyphs in 3D



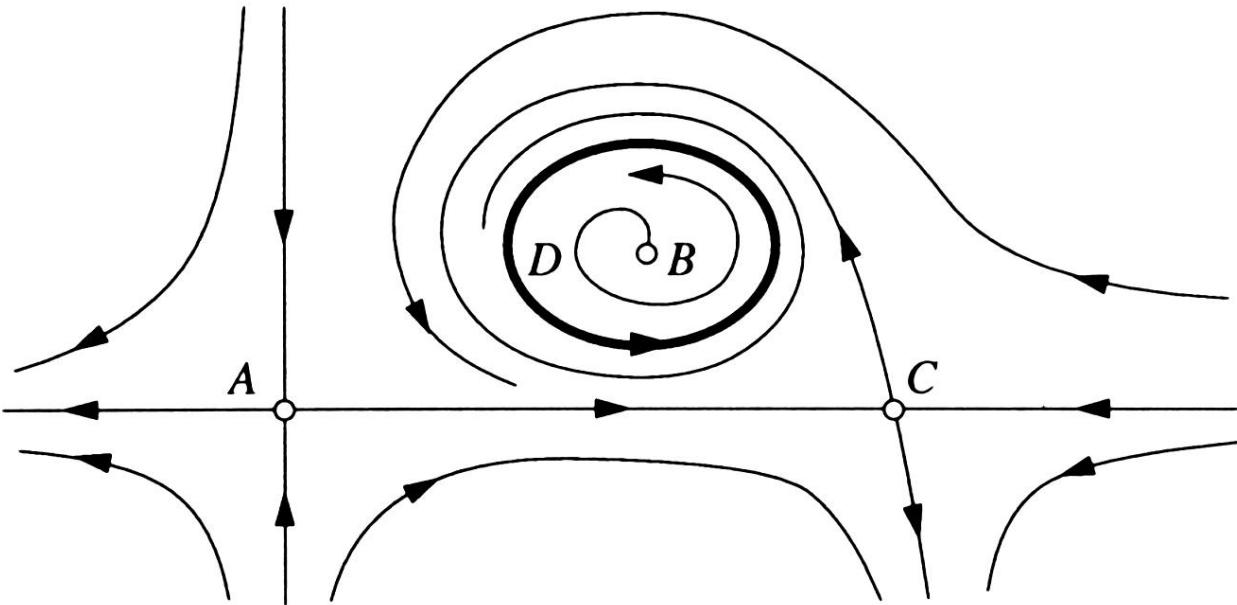
# Flow Topology

## Topology:

- abstract structure of a flow

- different elements, e.g.:

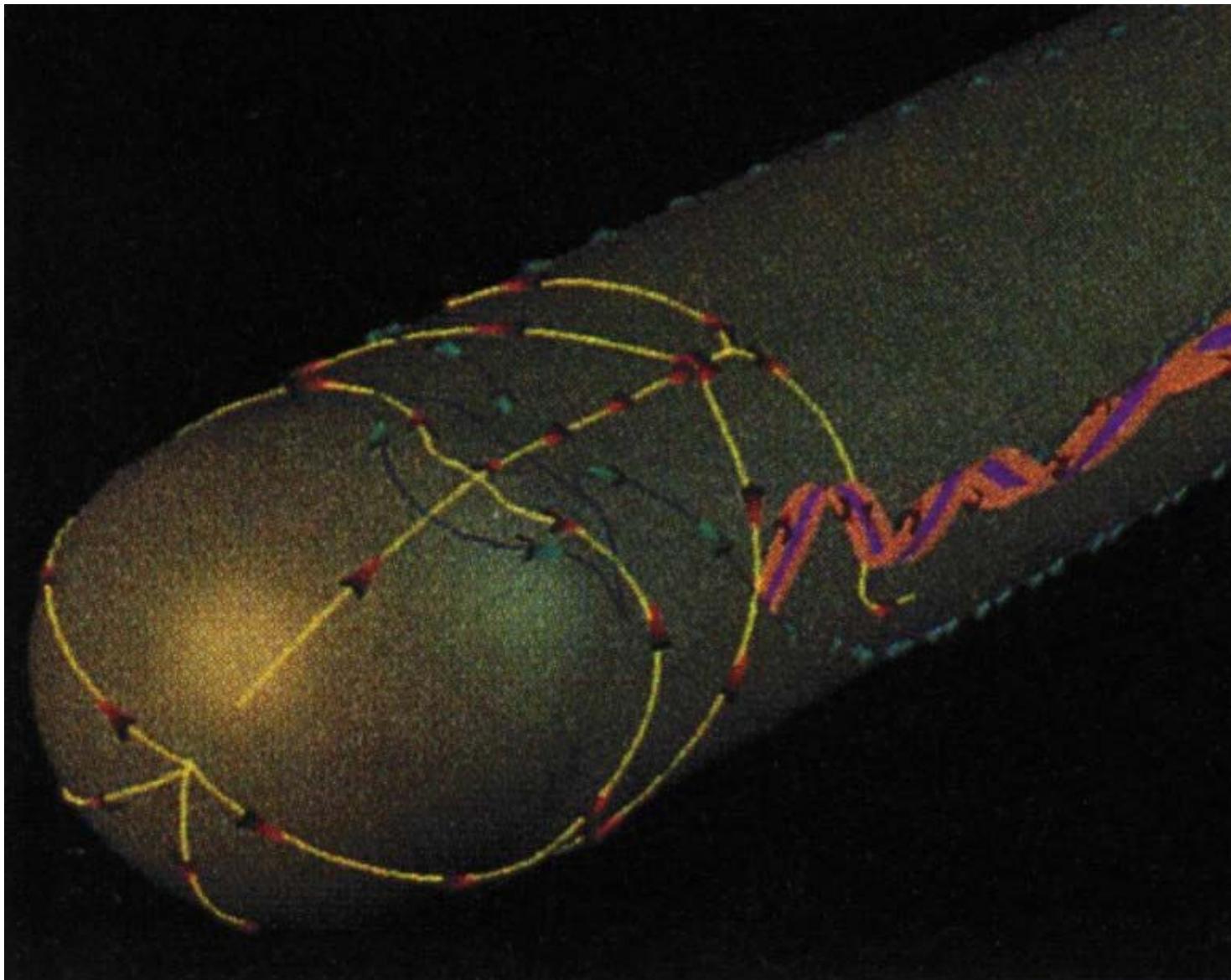
- checkpoints, defined through  $v(x)=0$
- cycles, defined through  $s_x(t+T)=s_x(t)$
- connecting structures (separatrices, etc.)



# Flow Topology in 3D

- Topology on surfaces:

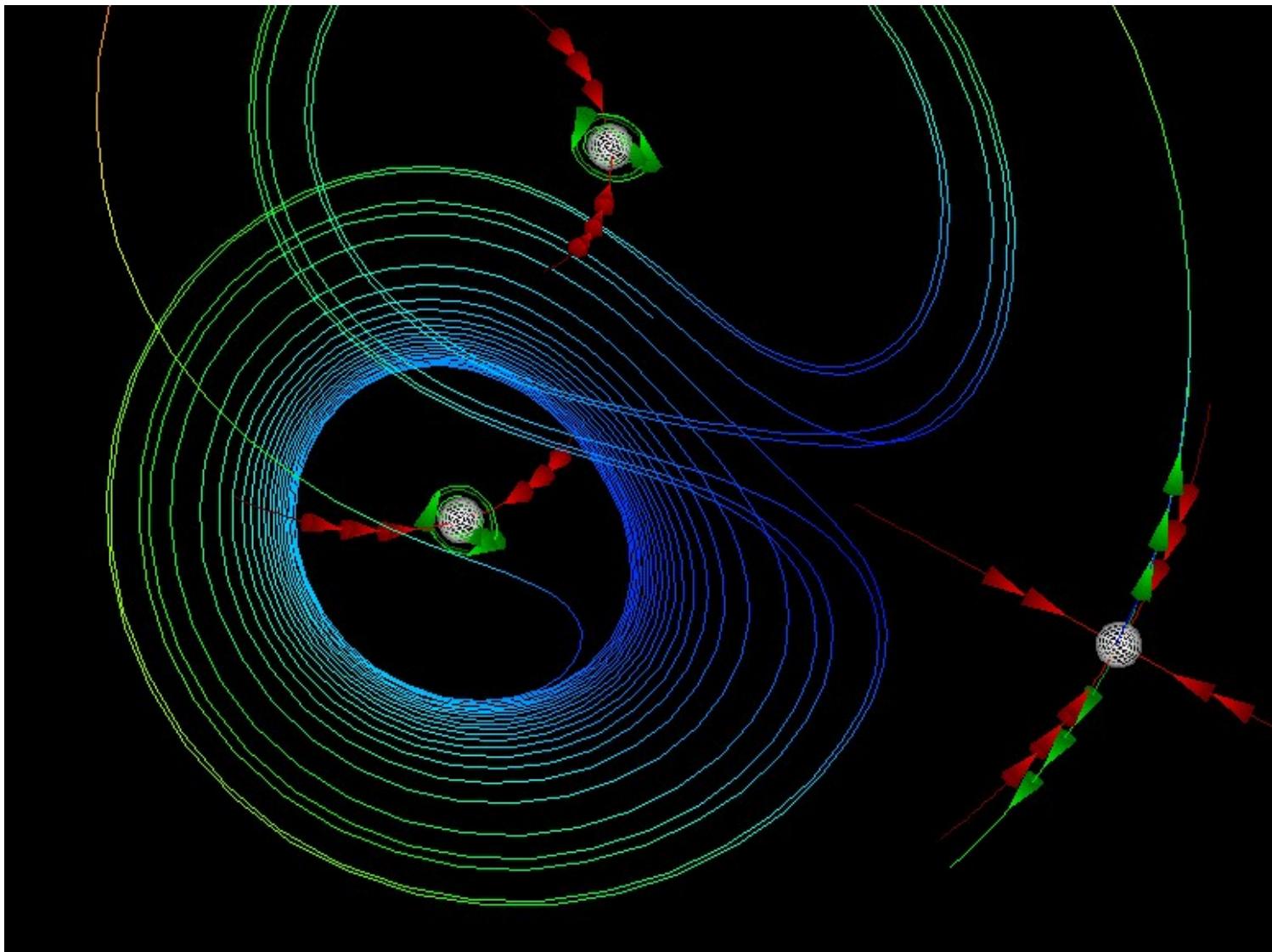
- fixed points
- separatrixes



# Flow Topology in 3D

## ■ Lorenz system:

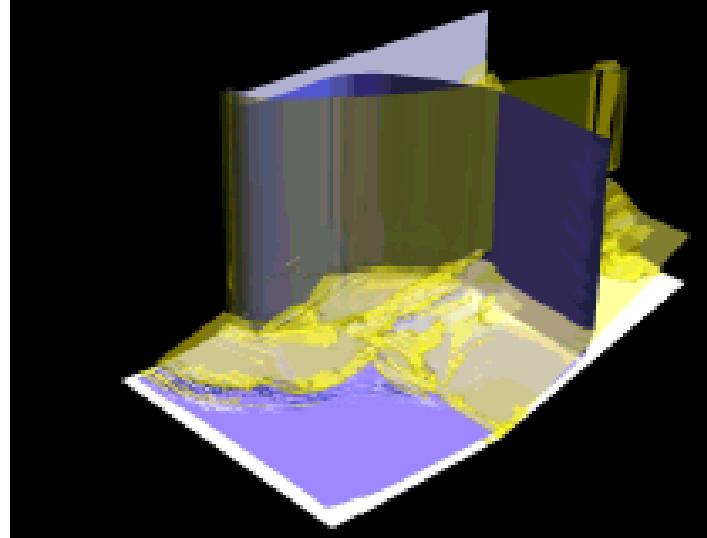
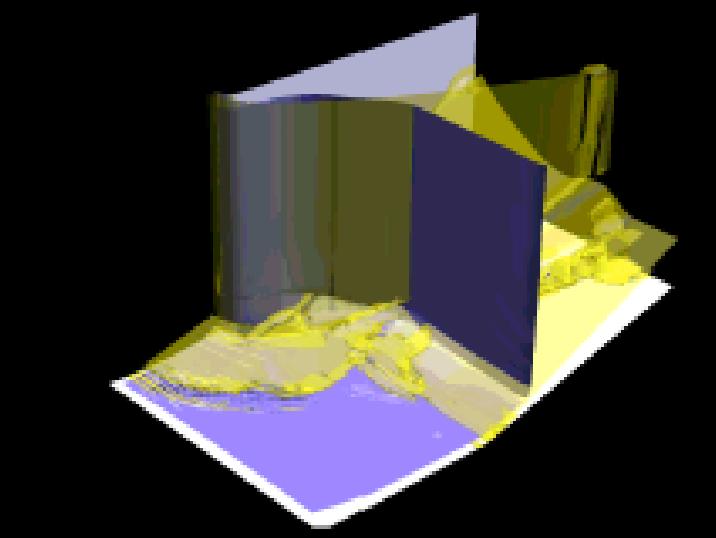
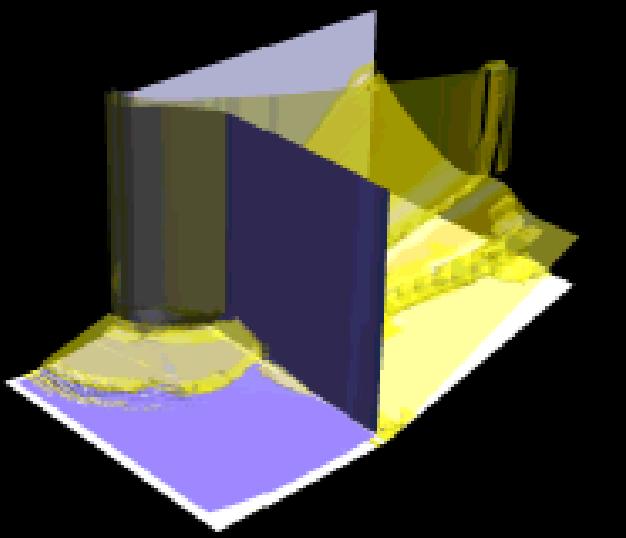
- 1 saddle
- 2 saddle foci
- 1 chaotic attractor



# Timesurfaces

## ■ Idea:

- start surface, e.g. part of a plane
- move whole surface along flow over time
- time surface: surface at one point in time



# Literature, References

- **B. Jobard & W. Lefer:** “**Creating Evenly-Spaced Streamlines of Arbitrary Density**” in *Proceedings of 8th Eurographics Workshop on Visualization in Scientific Computing*, April 1997, pp. 45-55
- **B. Cabral & L. Leedom:** “**Imaging Vector Fields Using Line Integral Convolution**” in *Proceedings of SIGGRAPH '93 = Computer Graphics* 27, 1993, pp. 263-270
- **D. Stalling & H.-C. Hege:** “**Fast and Resolution Independent Line Integral Convolution**” in *Proceedings of SIGGRAPH '95 = Computer Graphics* 29, 1995, pp. 249-256
- **Frits H. Post, Benjamin Vrolijk, Helwig Hauser, Robert S. Laramee, Helmut Doleisch:** **The State of the Art in Flow Visualization: Feature Extraction and Tracking.** Published in journal *Computer Graphics Forum* (Blackwell CGF) 22(4), pp. 775-792, 2003. [<http://wwwx.cs.unc.edu/~taylorr/Comp715/papers/j.1467-8659.2003.00723.x.pdf>]
- **Robert S. Laramee, Helwig Hauser, Helmut Doleisch, Benjamin Vrolijk, Frits H. Post, Daniel Weiskopf:** **The State of the Art in Flow Visualization: Dense and Texture-based Techniques.** Published in journal *Computer Graphics Forum* (Blackwell CGF) 23(2), pp. 203-222, 2004.  
[<http://wwwx.cs.unc.edu/~taylorr/Comp715/papers/j.1467-8659.2004.00753.x.pdf>]
- <http://www.winslam.com/rlaramee/swirl-tumble/>



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  - ◆ Helwig Hauser
  - ◆ Bruno Jobard
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  - ◆ Rüdiger Westermann
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