

Volume Visualization

Part 3 (out of 3)



Hardware-Volume Visualization

Faster with Hardware?!



Two Approaches



- 3D-textures:
 - ◆ Volume data stored in 3D-texture
 - ◆ Proxy geometry (slices) parallel to image plane, are interpolated tri-linearly
 - ◆ Back-to-front compositing
- 2D-textures:
 - ◆ 3 stacks of slices (x-, y- & z-axis), slices are interpolated bi-linearly
 - ◆ Select stack (most "parallel" to image plane)
 - ◆ Back-to-front compositing



Variation of View Point

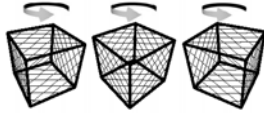


3D-textures:

- ◆ Number of slices arbitrary

2D-textures:

- ◆ Stack change: discontinuity



Viewport-Aligned Slices



Object-Aligned Slices



Special Hardware



Hardware volume raycasting

- ◆ In vertex and fragment operations of modern graphics cards

Special Hardware

- ◆ VolumePro board:
 - Special card for PC
 - Calculates shear-warp factorization, incl. compositing
 - Warp-step with "regular" graphics card (OpenGL)



Marching Cubes (MC)

Iso-Surface-Display



Repetition: Volume vs. Surface Rendering



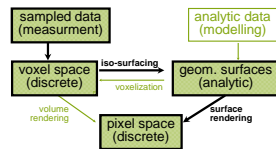
- **Volume rendering:**
 - ◆ Direct volume visualization
 - ◆ Usage of transfer functions
 - ◆ Pros: look on the interior, semi-transparency
- **Surface rendering:** ←
 - ◆ Indirect volume visualization
 - ◆ Intermediate representation: Iso-surface, "3D"
 - ◆ Pros: shading → shape!, hardware rendering



Concepts and Terms



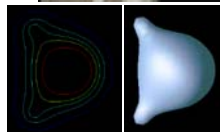
- **Example 1:**
 - ◆ CT measurement
 - ◆ Iso-stack-conversion
 - ◆ Iso-surface-calculation (marching cubes)
 - ◆ Surface rendering (OpenGL)



Iso-Surfaces



- **Intermediate representation**
- **Aspects:**
 - ◆ **Preconditions:**
 - expressive Iso-value, Iso-value separates materials
 - Interest: in transitions
 - ◆ Very selective (binary selection / omission)
 - ◆ Uses traditional hardware
 - ◆ shading ⇒ 3D-impression!

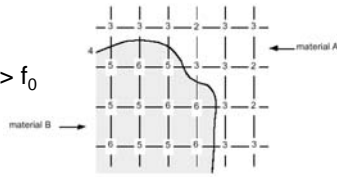


Volume Data \leftrightarrow Iso-Surfaces



■ Iso-Surface:

- ◆ Iso-value f_0
- ◆ separates values $> f_0$ from values $\leq f_0$
- ◆ Often not known \rightarrow
- ◆ Can only be approximated from samples!
- ◆ Shape / position dependent on type of reconstruction



Approximation of Iso-Surface

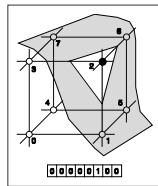
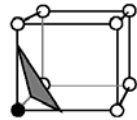


■ Approach:

- ◆ Iso-Surface intersects data volume = set of all cells

■ Idea:

- ◆ Parts of iso-surface represented on a(n intersected) cell basis
- ◆ As simple as possible:
Usage of triangles



Marching Cubes

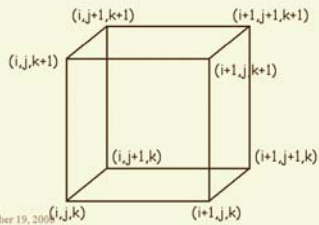
✓ Cell consists of 4(8) pixel (voxel) values:
($i+[01]$, $j+[01]$, $k+[01]$)

1. Consider a Cell
2. Classify each vertex as inside or outside
3. Build an index
4. Get edge list from table[index]
5. Interpolate the edge location
6. Go to next cell



MC 1: Create a Cube

✓ Consider a Cube defined by eight data values:

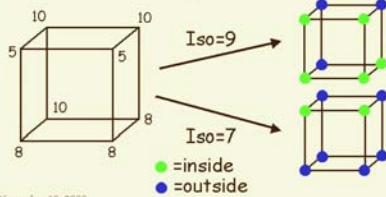


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MC 2: Classify Each Voxel

✓ Classify each voxel according to whether it lies outside the surface (value > iso-surface value) inside the surface (value <= iso-surface value)

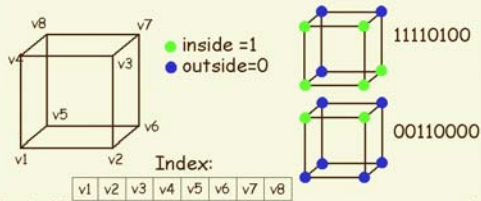


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MC 3: Build An Index

✓ Use the binary labeling of each voxel to create an index

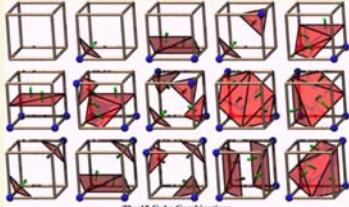


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MC 4: Lookup Edge List

- ✓ For a given index, access an array storing a list of edges



The 15 Cube Combinations

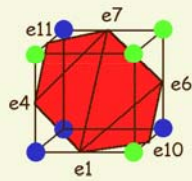
- ✓ all 256 cases can be derived from 15 base cases

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MC 5: Example

- ✓ Index = 10110001
- ✓ triangle 1 = e4, e7, e11
- ✓ triangle 2 = e1, e7, e4
- ✓ triangle 3 = e1, e6, e7
- ✓ triangle 4 = e1, e10, e6



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MC 6: Interp. Triangle Vertex

- ✓ For each triangle edge, find the vertex location along the edge using linear interpolation of the voxel values



$$T=5 \quad x = i + \left(\frac{T - v[i]}{v[i+1] - v[i]} \right)$$

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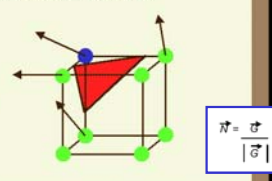
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MC 7: Compute Normals

- ✓ Calculate the normal at each cube vertex

$$G_x = V_{x-1,y,z} - V_{x+1,y,z}$$

$$G_y = V_{x,y-1,z} - V_{x,y+1,z}$$

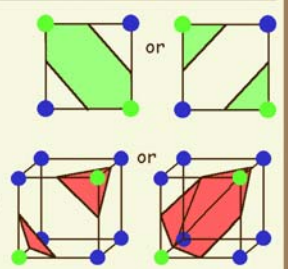
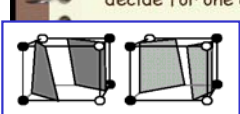
$$G_z = V_{x,y,z-1} - V_{x,y,z+1}$$


- ✓ Use linear interpolation to compute the polygon vertex normal

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MC 8: Ambiguous Cases

- ✓ Ambiguous cases: 3, 6, 7, 10, 12, 13
- ✓ Adjacent vertices: different states
- ✓ Diagonal vertices: same state
- ✓ Resolution: decide for one case

Danger: Holes!

Wrong vs. correct classification!

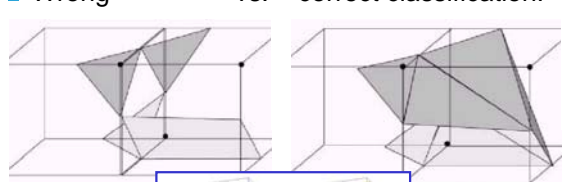
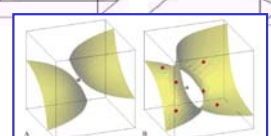
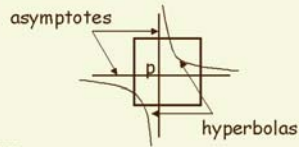



Figure 4: Two internal configurations for the Marching Cubes configuration 5

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MC 9: Asymptotic Decider

- ✓ Assume bilinear interpolation within a face
- ✓ hence iso-surface is a hyperbola
- ✓ compute the point p where the asymptotes meet
- ✓ sign of $S(p)$ decides the connectedness

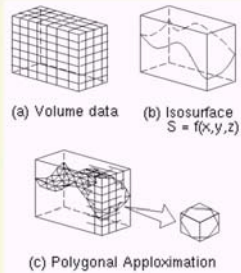


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Marching Cubes - Summary 1

- ✓ 256 Cases
- ✓ reduce to 15 cases by symmetry
- ✓ Complementary cases - (swap in- and outside)
- ✓ Ambiguity resides in cases 3, 6, 7, 10, 12, 13
- ✓ Causes holes if arbitrary choices are made.



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Marching Cubes - Summary 2

- ✓ Up to 4 triangles per cube
- ✓ Dataset of 512^3 voxels can result in several million triangles (many Mbytes!!!)
- ✓ Iso-surface does not represent an object!!!
- ✓ No depth information
- ✓ Semi-transparent representation --> sorting
- ✓ Optimization:
 - Reuse intermediate results
 - Prevent vertex replication
 - Mesh simplification




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MC Examples

1 Iso-surface




3 Iso-surfaces



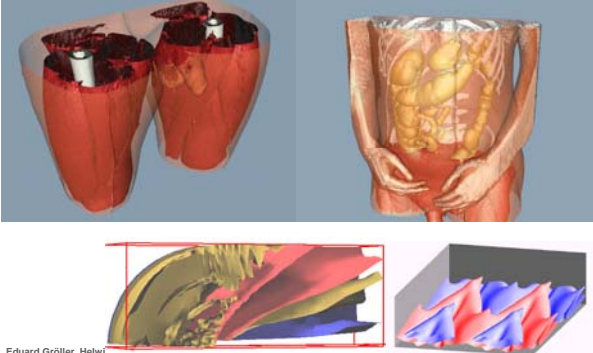


2 Iso-surfaces



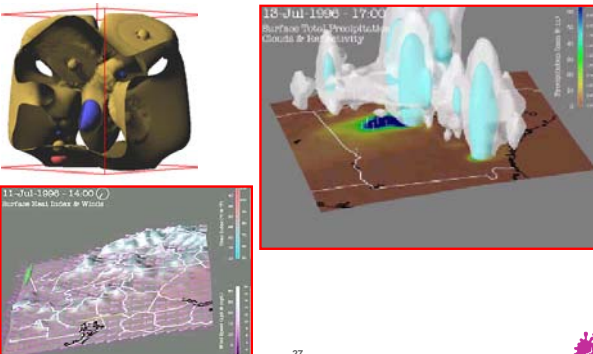
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Further Examples



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Even Further Examples



11-Jul-1996 - 14:00
Surface Wind Vectors & Wind

18 Jul 1996 - 17:00
Surface Wind, Precipitation
Clouds & Low Clouds

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Literature



■ Paper (more details):

- ◆ **W. Lorensen & H. Cline: "Marching Cubes: A High Resolution 3D Surface Construction Algorithm"** in *Proceedings of ACM SIGGRAPH '87 = Computer Graphics*, Vol. 21, No. 24, July 1987



Conclusion Volume Visualization General Remarks



Surface vs. Volume Rendering




■ Surface Rendering:

- ◆ Indirect representation / display
- ◆ Conveys surface impression
- ◆ Hardware supported rendering (fast?!)
- ◆ Iso-value-definition


■ Volume Rendering:


- ◆ direct representation / display
- ◆ Conveys volume impression
- ◆ Often realized in software (slow?!)
- ◆ Transfer functions



Conclusion VolVis 

- Introduction ⇐ data, simple methods
⇐ DVR vs. surf. fitting
- Direct volume visualization
 - ◆ Ray casting ⇐ types of combinations
 - ◆ Splatting ⇐ object-order vs. image-order
⇐ speed vs. quality
 - ◆ Shear-warp factorization
 - ◆ Hardware-based VolVis
- Indirect VolVis ⇐ iso-value selection
 - ◆ Marching cubes (iso-surface-visualization)
- Conclusion

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