

Acquisition of 3D Data

Tomographic Techniques

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3D Data

- **Animation, film:** a sequence of images with *time* as the third coordinate:

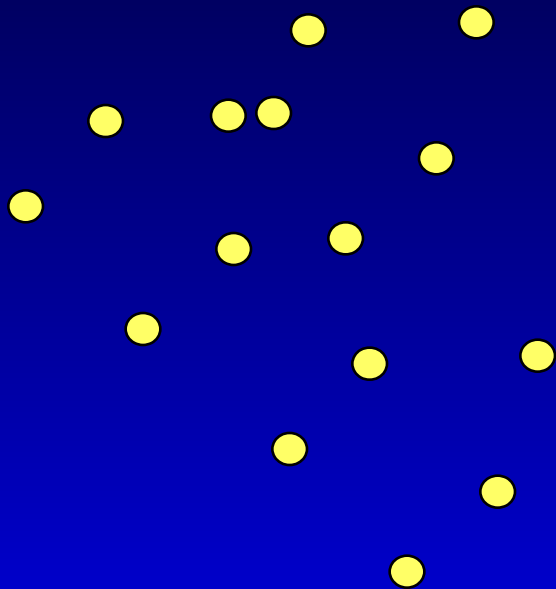
[x,y,t]

- **Volume data:** a sequence of images with *space* as the third coordinate:

[x,y,z]

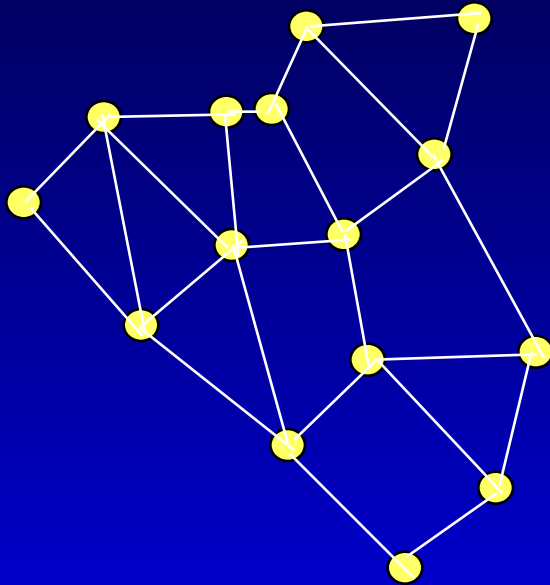
- **Volume data in general:** a set of data samples measured on a grid with certain properties

Scattered Points



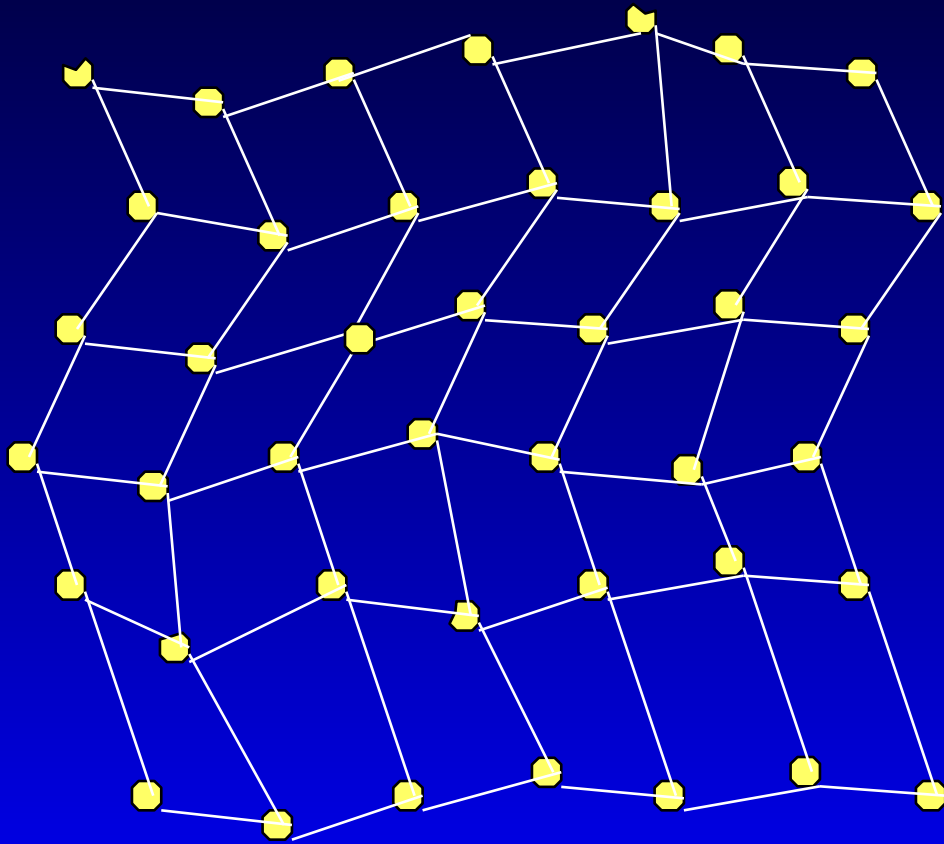
- Sample position
 - $[x_i, y_j, z_k]$
- Neighborhood relation:
 - None

Unstructured Grid



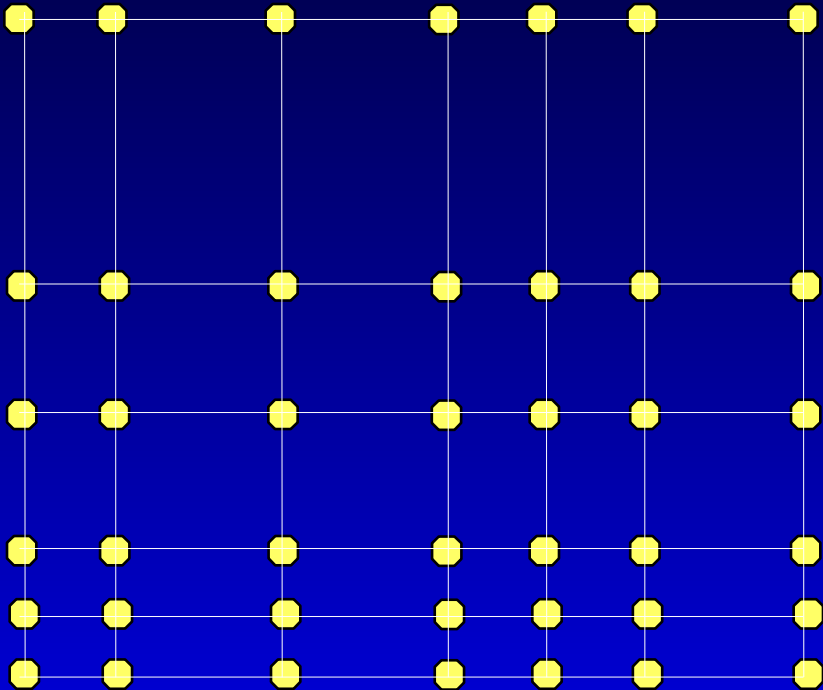
- Sample position
 - $[x_p, y_p, z_p]$
- Neighborhood relation:
 - Explicit $i-k, i-l, \dots$

Structured Grid



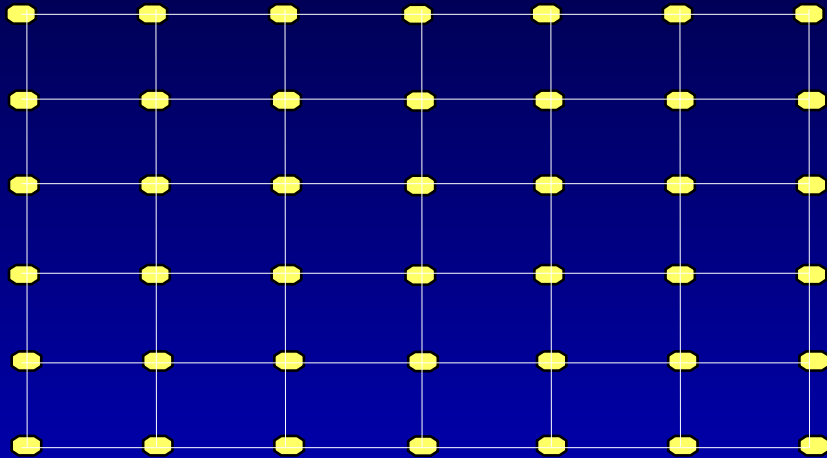
- Sample position:
 - based on coordinates at $[i,j,k]$
- Neighborhood relation:
 - Implicit, neighbors from the grid

Rectilinear Grid



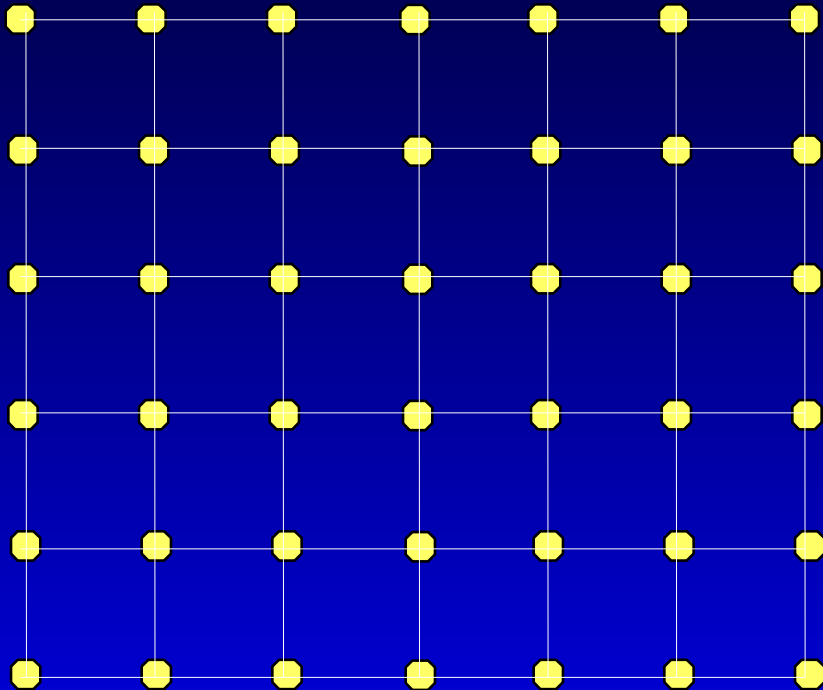
- **Sample position:**
 - Coordinates $[i,j,k]$
 - Distance between X, Y and Z planes
- **Neighborhood relation:**
 - Implicit, neighbors from the grid

Regular Grid



- **Sample position:**
 - Coordinates $[i,j,k]$
 - Cell size $[X, Y, Z]$
- **Neighborhood relation:**
 - Implicit, neighbors from the grid

Cartesian Grid



- Sample position:
 - Coordinates $[i,j,k]$
 - Cell dimension X
- Neighborhood relation:
 - Implicit, neighbors from the grid

Cartesian Grid and its Elements

Basic elements of volume data

- **Sample:**

- Dimensionless point with value

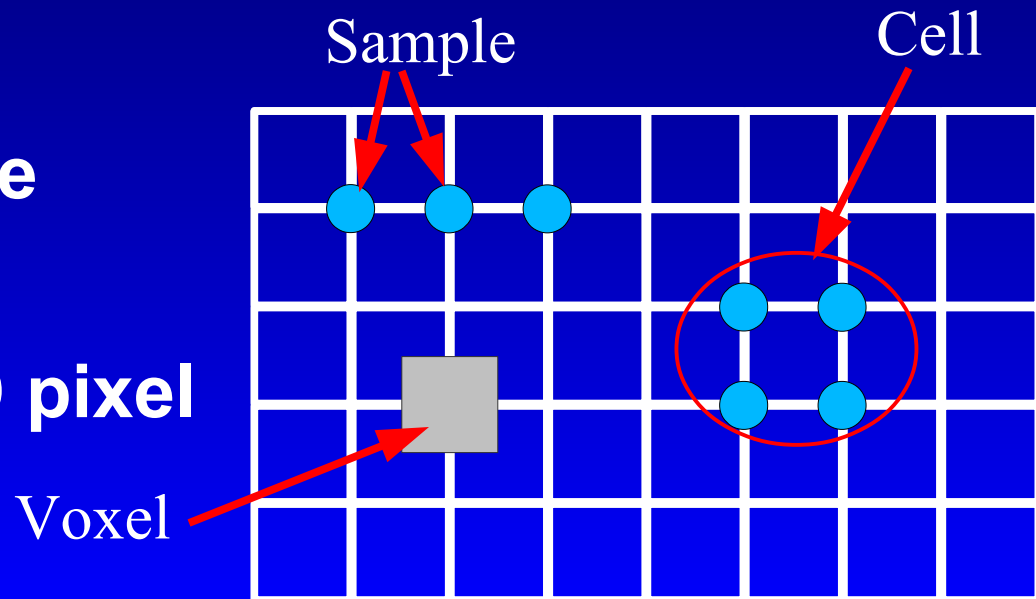
- **Cell:**

- 8 (4) samples in vertices of a cube

- **Voxel**

- Homogeneous cube centered at sample position

- Analogue of the 2D pixel



Acquisition of Volumetric Data

- 3D imaging techniques

- **Anatomically** oriented techniques:

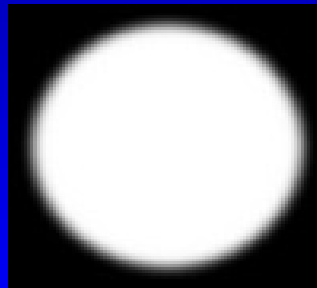
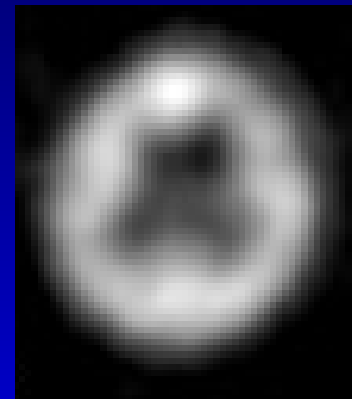
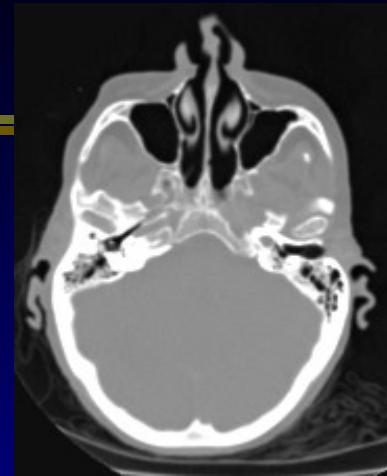
- Computer tomography-CT, magnetic resonance imaging-MRI, ultrasound imaging-US

- **Physiologically** oriented techniques :

- Positron emission tomography-PET, single-photon emission tomography-SPECT, functional MRI

- Synthetic data

- Voxelization



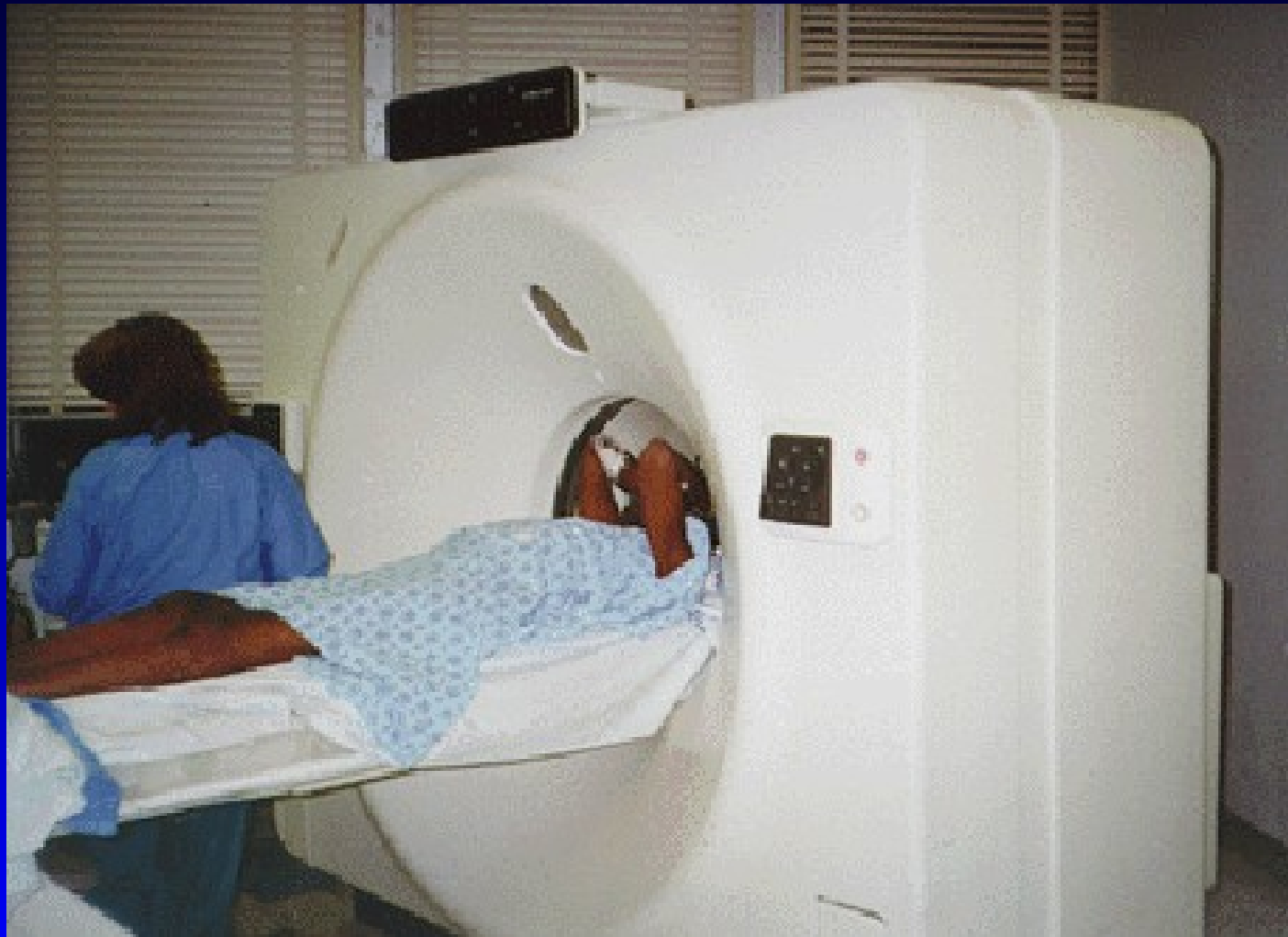
Computed Tomography (CT)

- Also: Computer Aided Tomography (CAT, CAT scan)
- Principle:
 - Measurement of X-ray attenuation along a viewing ray (projections)

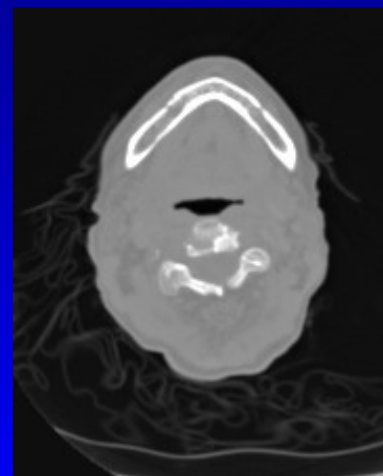
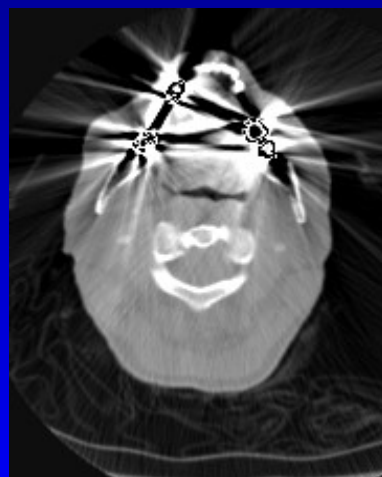
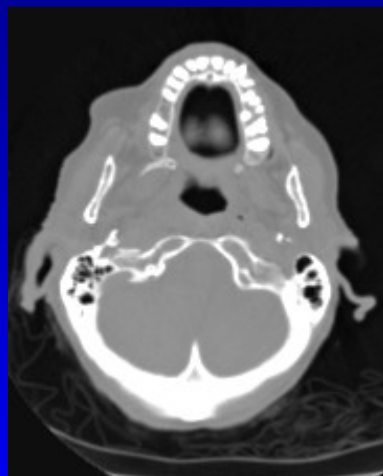
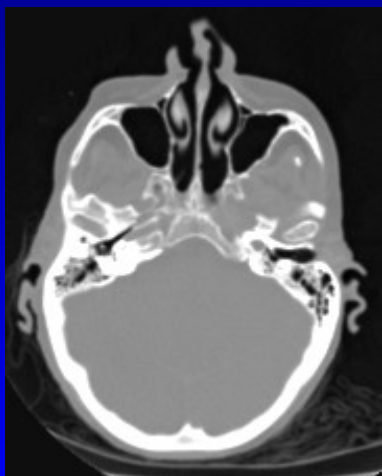
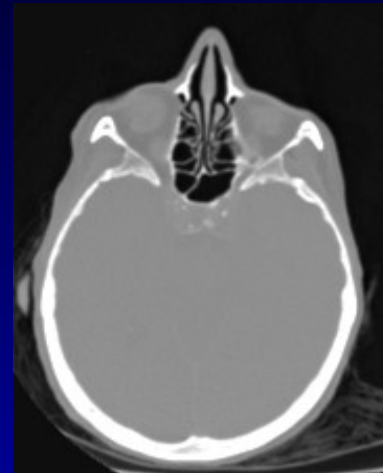
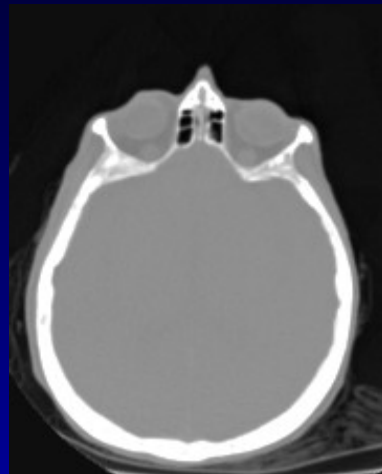
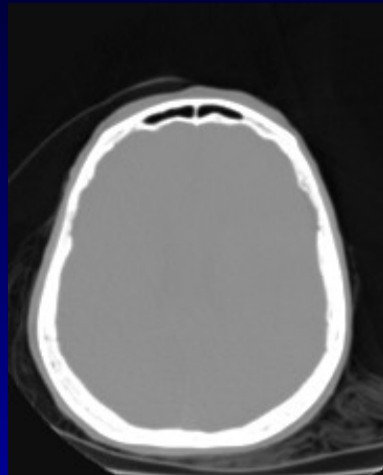
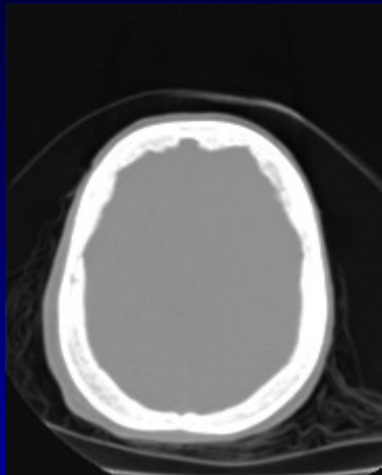
$$S = \int \mu(l) dl$$

- Production of images: reconstruction from projections

A CT Tomograph

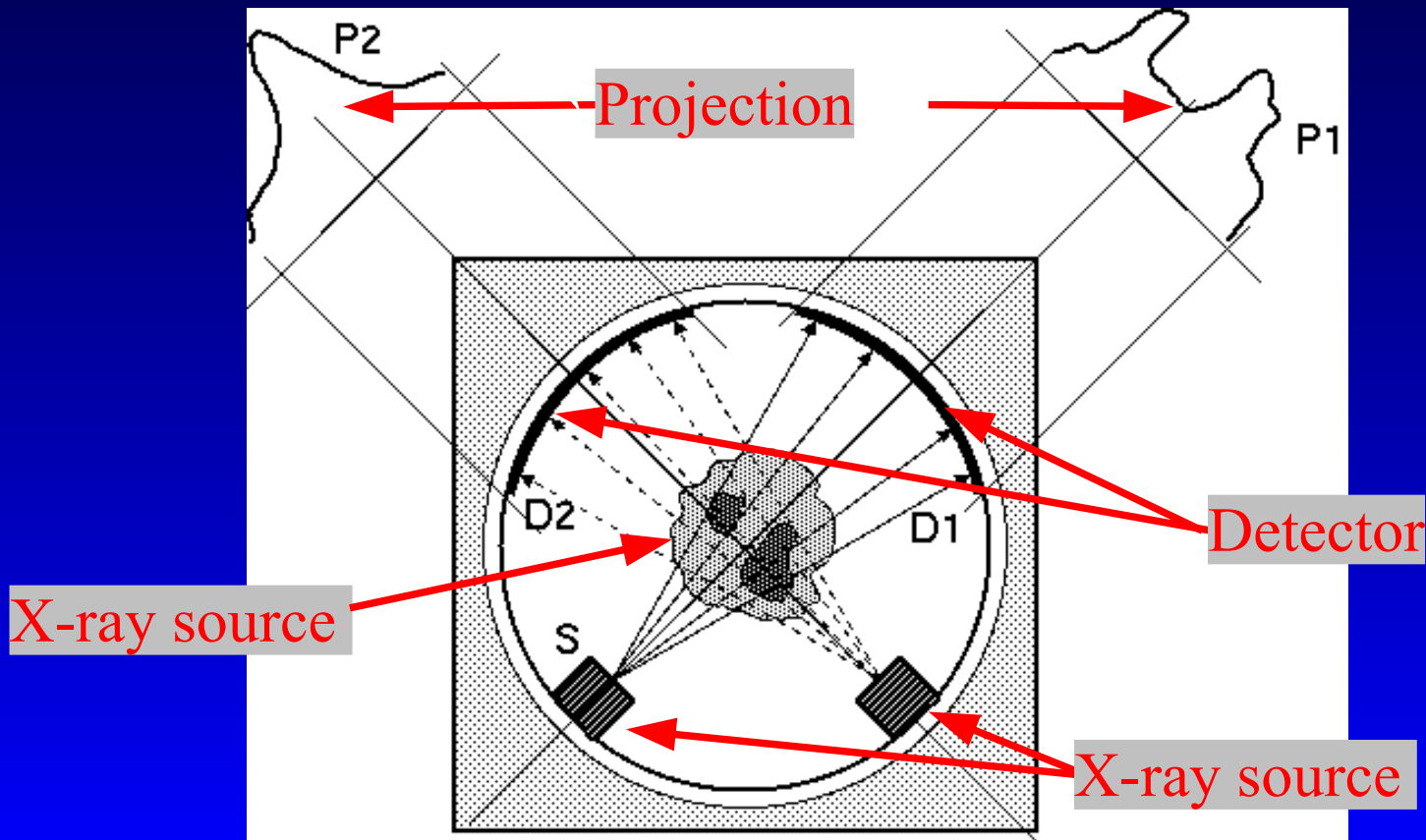


A Sample CT Scan



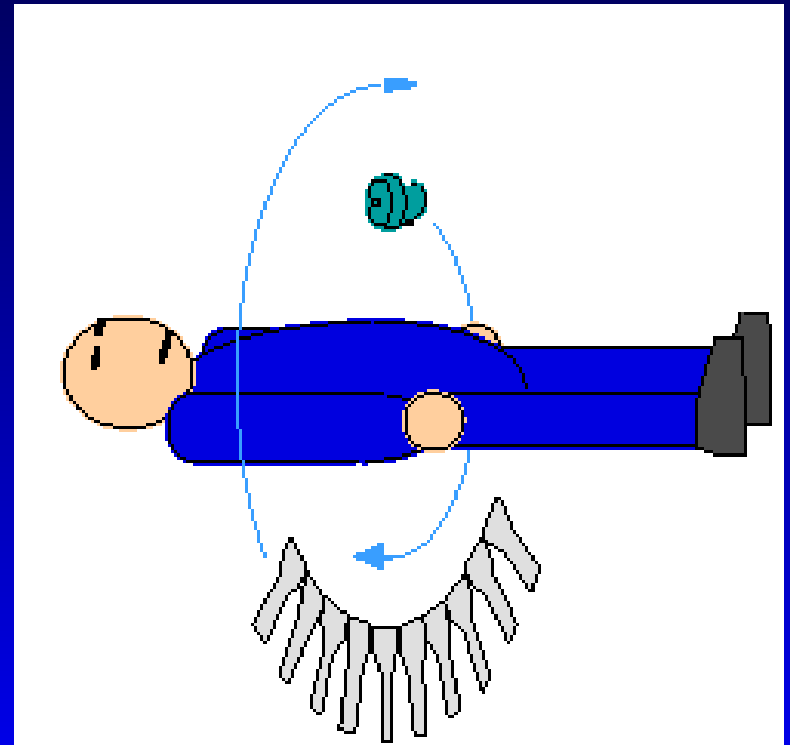
Measurement of Projections

- Standard setup:
 - cca 200 1D projections for one slice

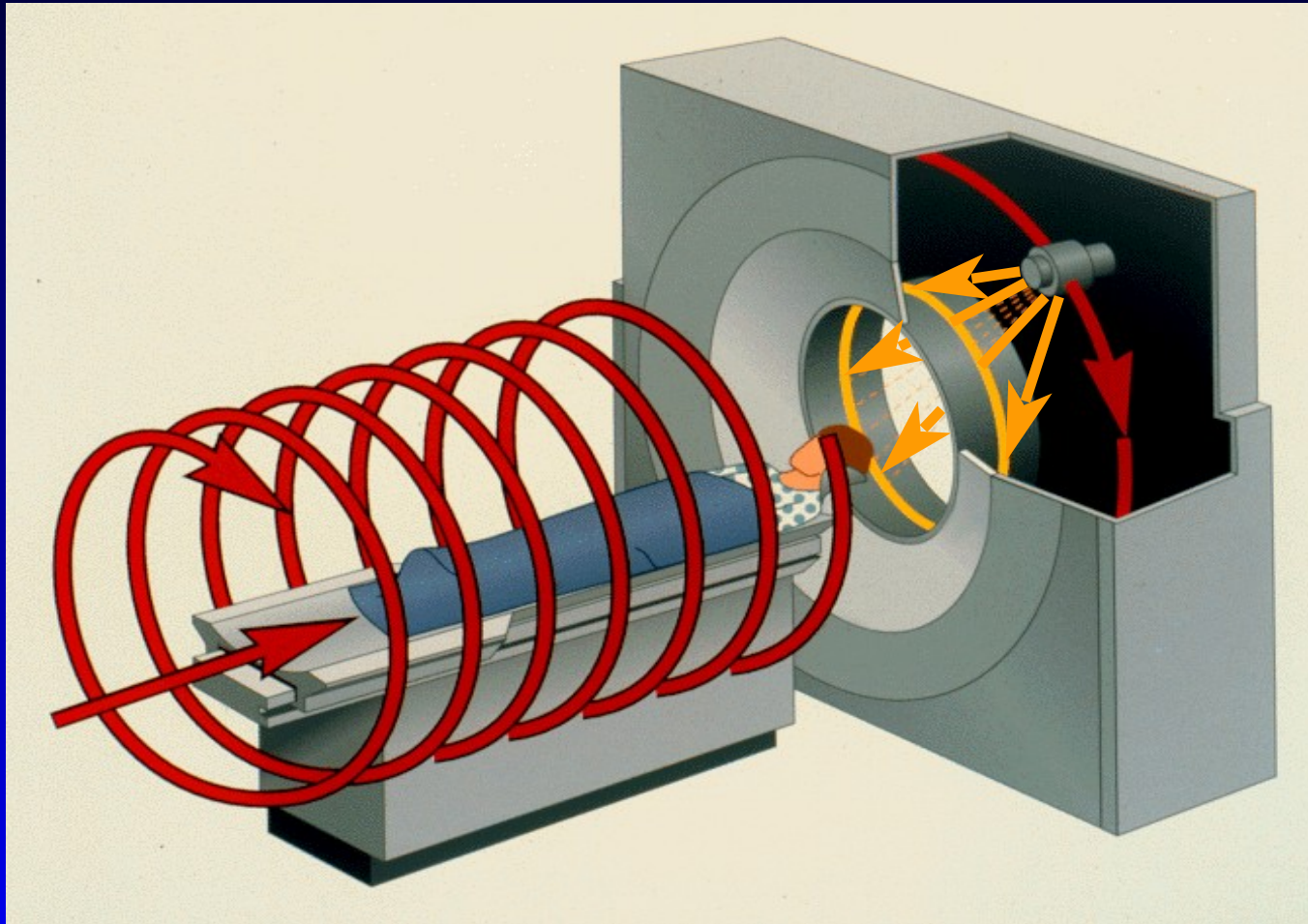


Measurement of Projections

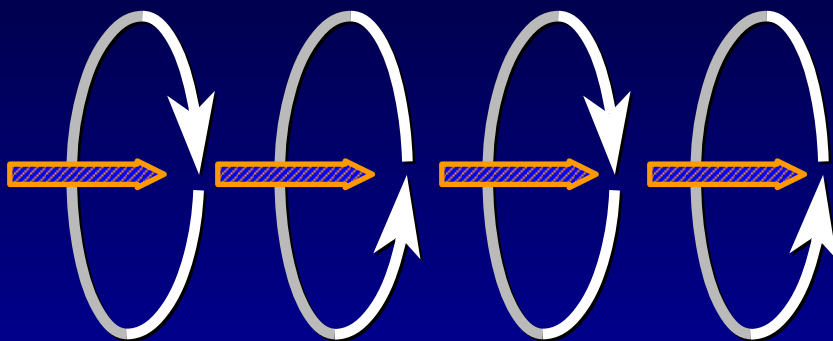
- Spatial configuration of source and detector arrays:
 - Aligned rotation
 - 180 deg



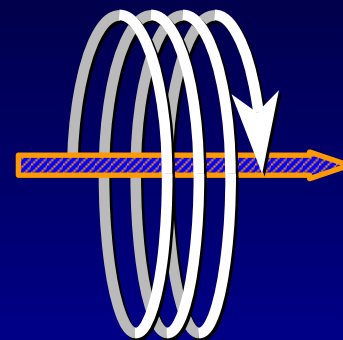
Recent Setup: Fan-Beam Spiral CT



Standard CT vs. Spiral CT



**25 Slices in
> 2 Minutes**

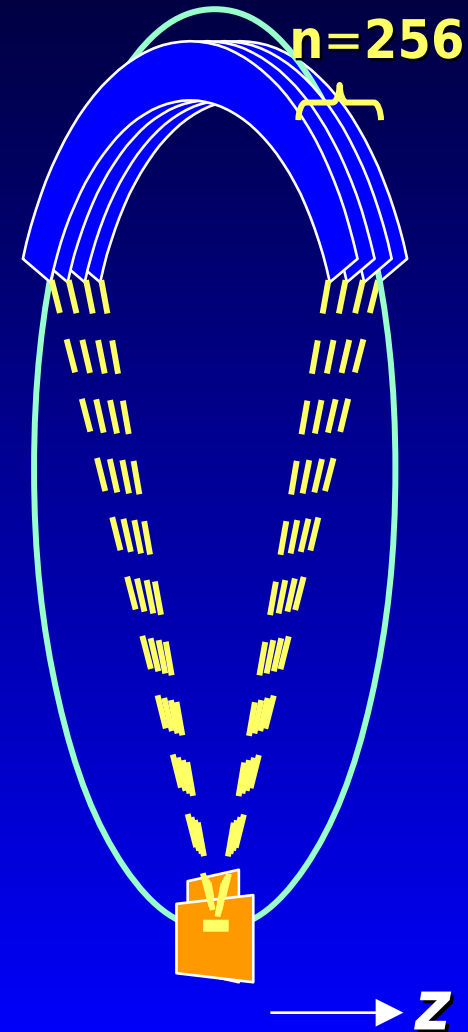


**25 Slices in
25 Seconds**

Multi-Detector CT Scanner

State of the art:

- Detectors
 - Up to 256
 - Spacing < 1mm
- Scanning speed:
 - 1m/30s



Reconstruction from Projections

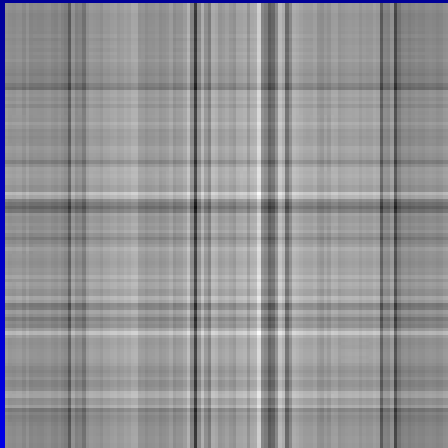
- Theory:
 - Johann Radon
- First Tomograph:
 - Godfrey Hounsfield
 - Nobel prize 1979
- Reconstruction methods:
 - Algebraic methods
 - Filtered backprojection
 - Fourier methods



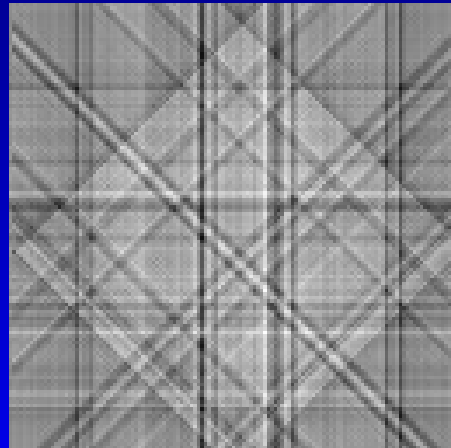
Source: Wikipedia

Filtered Backprojection

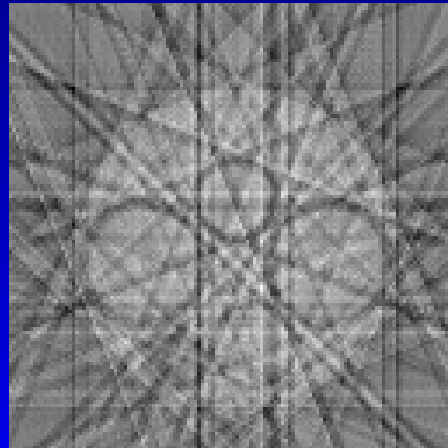
- For all projections:
 - Projection filtration (high pass filter, derivative)
 - Distribution of the filtered projection to the image in the direction of the projection



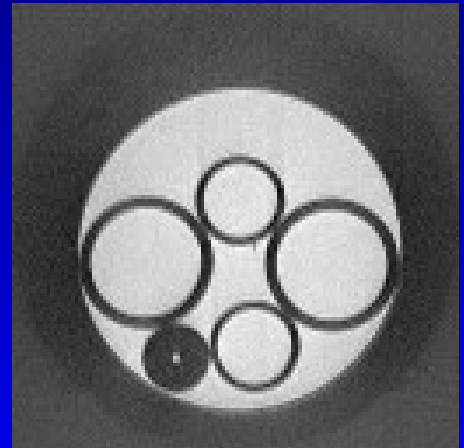
2



4

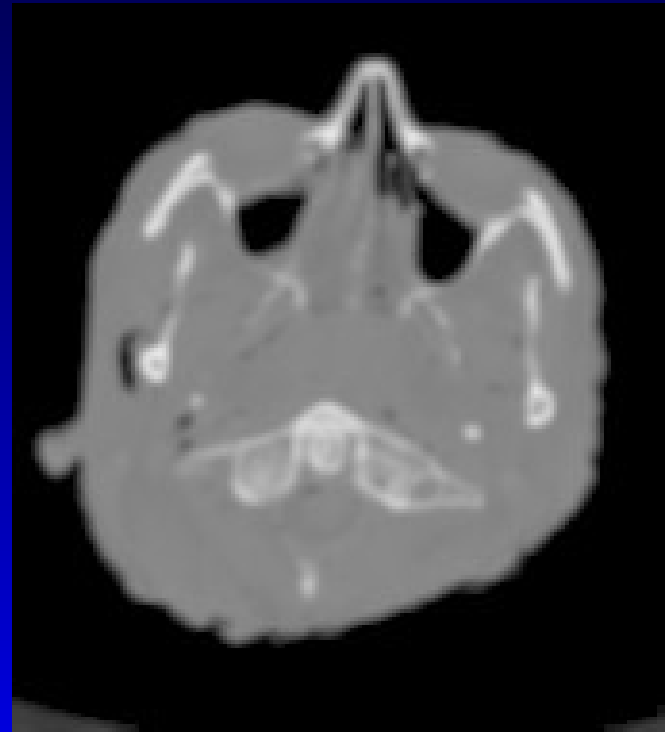
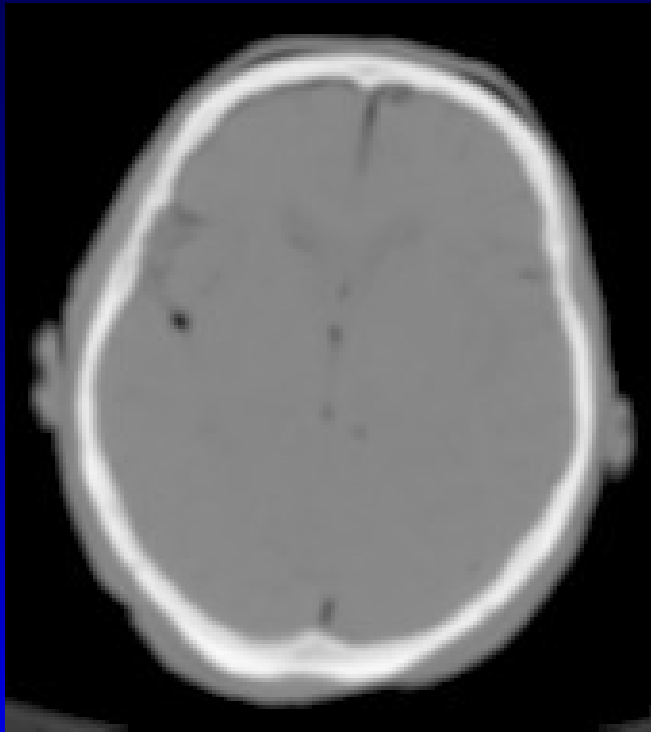


8



All

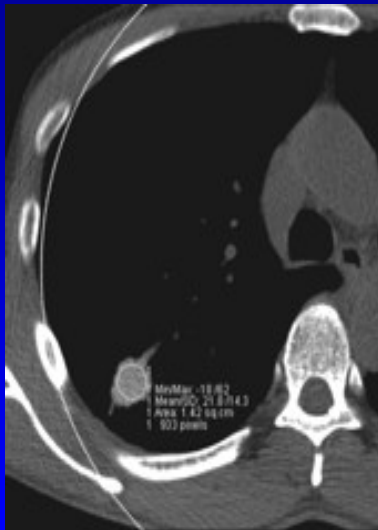
CT Tomogram - an Example



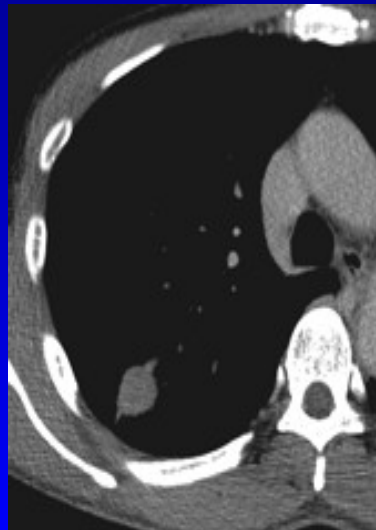
Dual Energy CT

- Attenuation coefficient μ depends on the wavelength
- Scanning with two X-ray lamp voltages (energies)
- Advantage: Discrimination of tissue types

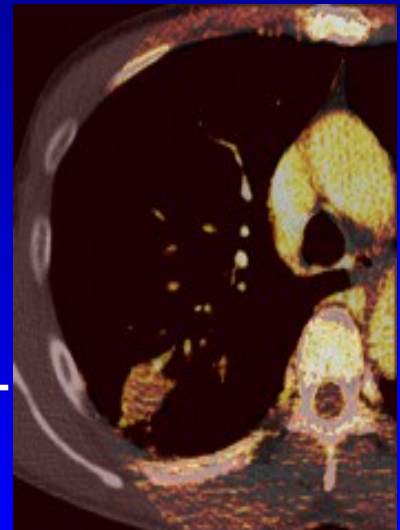
Voltage 80kV



Voltage 120kV



Composited



Hounsfield Unit

- Normalization of measured values to a -1000 – 3095 (12 bit) scale:

Substance	Value [HU]
Air	-1000
Water	0
Fat	70 – 120
Soft tissues	15 – 80
Bone	>1000

- Tissue density is defined by its physical properties

CT Data Properties

- Axial slices 0.5-10 mm thick
- Images 256 x 256 to 512 x 512 pixels of 0.5-2 mm side
- Up to 2000 images per study
- High spatial resolution
- Consistent values (HU scale)
- X-ray irradiation

Application Fields

- **Contrast determined by tissue density:**
 - Bone imaging
 - Calcifications
 - Inflammations
 - Hematomata
 - Tumors
- **Imaging with contrast agent:**
 - Blood vessels, vessel lumen

Overview

- Computer tomography (CT, CAT)
- **Magnetic resonance imaging (MRI)**
- **fMRI**
- **SPECT**
- **PET**

Magnetic Resonance Imaging

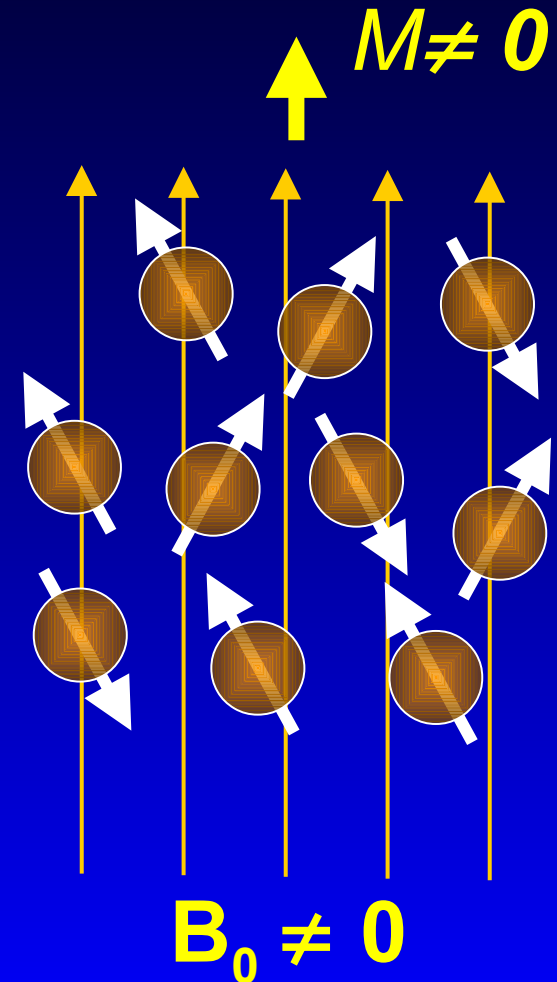
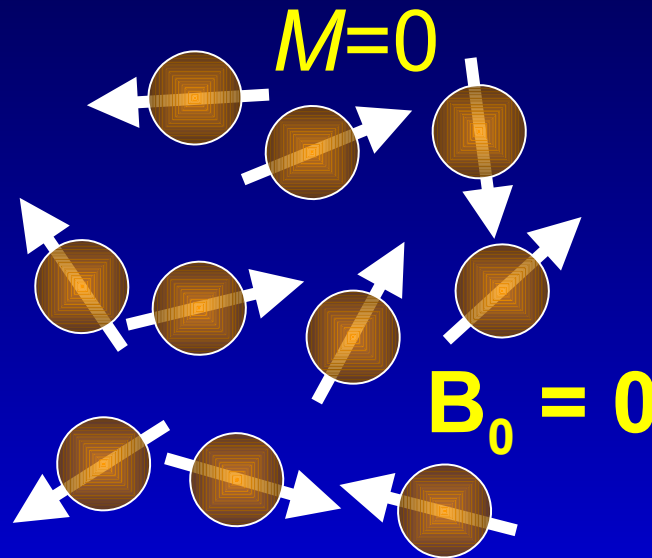
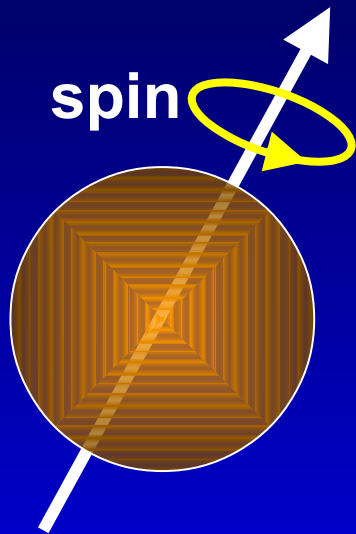
- ~~Nuclear Magnetic Resonance (NMR)~~
Magnetic Resonance Imaging (MRI)
- Physical principle
 - Interaction of atom nuclei with an external magnetic field (resonance)
 - Requirement: Nonzero magnetic or spin moment of the atoms
- Resonance
 - Energy transfer between coupled systems with equal characteristic frequency
 - Example: The Tacoma Narrows bridge

Common NMR Active Nuclei

Isotope	Spin I	% abundance	γ MHz/T
^1H	1/2	99.985	42.575
^2H	1	0.015	6.53
^{13}C	1/2	1.108	10.71
^{14}N	1	99.63	3.078
^{15}N	1/2	0.37	4.32
^{17}O	5/2	0.037	5.77
^{19}F	1/2	100	40.08
^{23}Na	3/2	100	11.27
^{31}P	1/2	100	17.25

Spins in a Magnetic Field

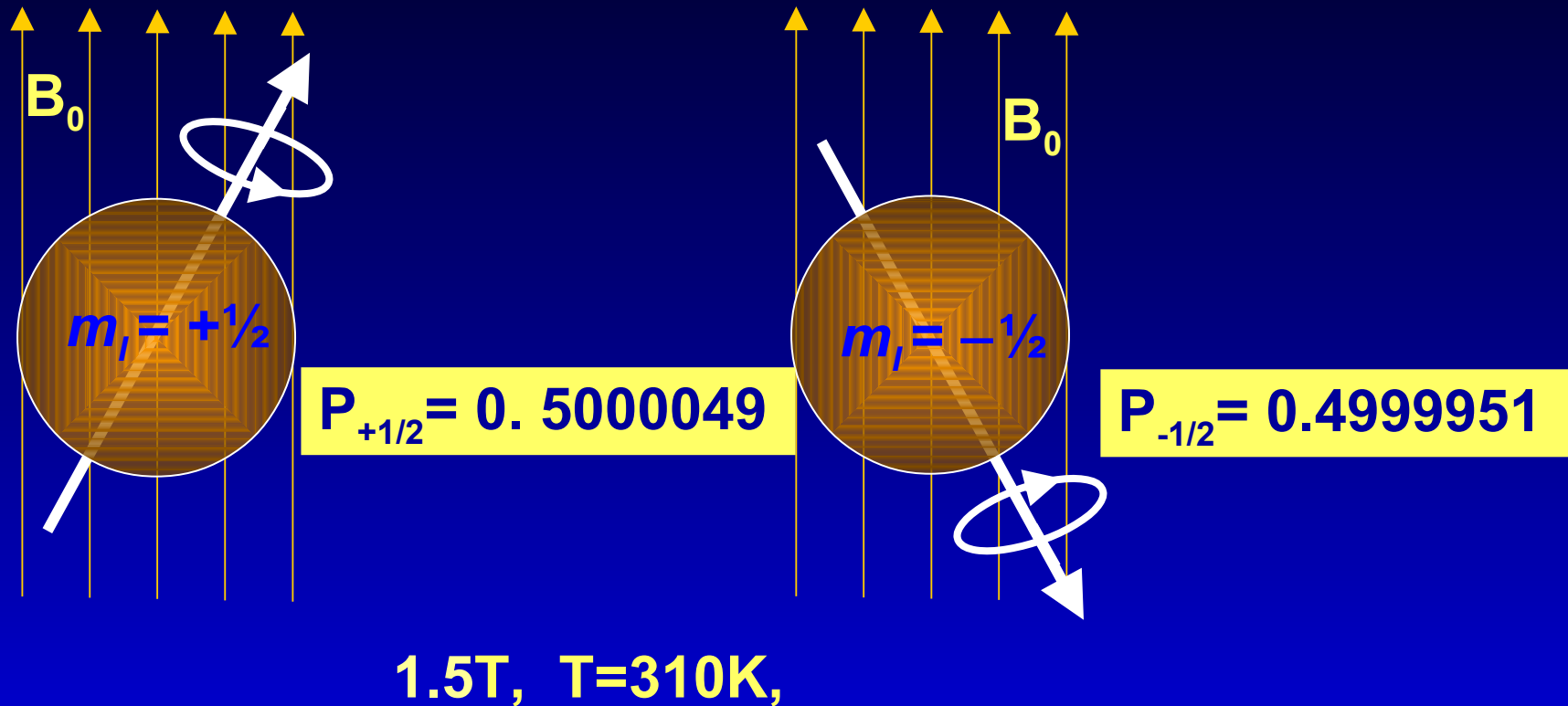
Atoms with uncompensated magnetic moment



M - Magnetization (material)

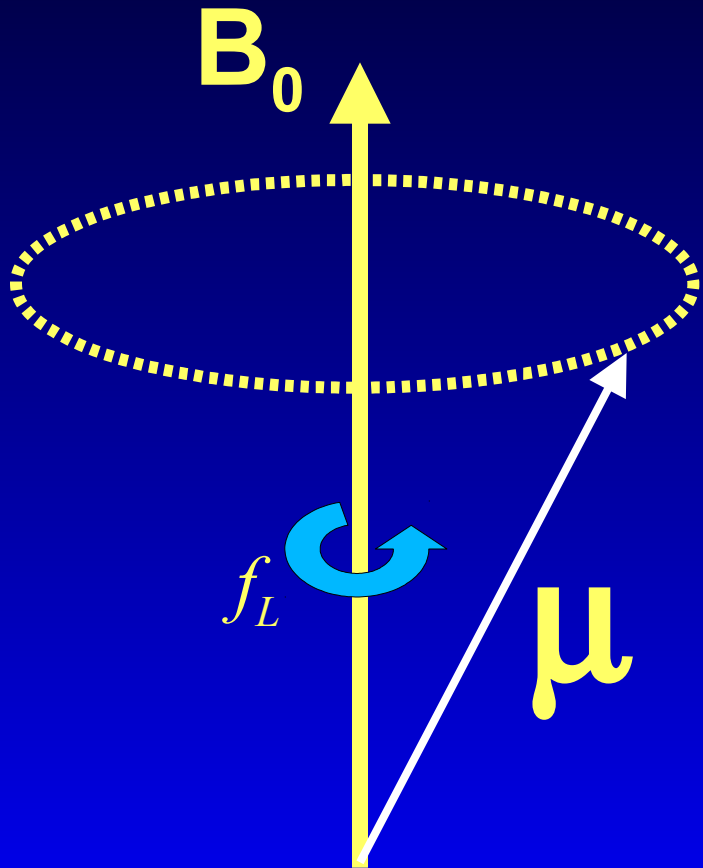
B - Induction (field strength)

Spin in a Magnetic Field (Zeeman Splitting, Spin $\frac{1}{2}$)



\Rightarrow Total magnetization M is parallel to B_0

Spin in a Magnetic Field



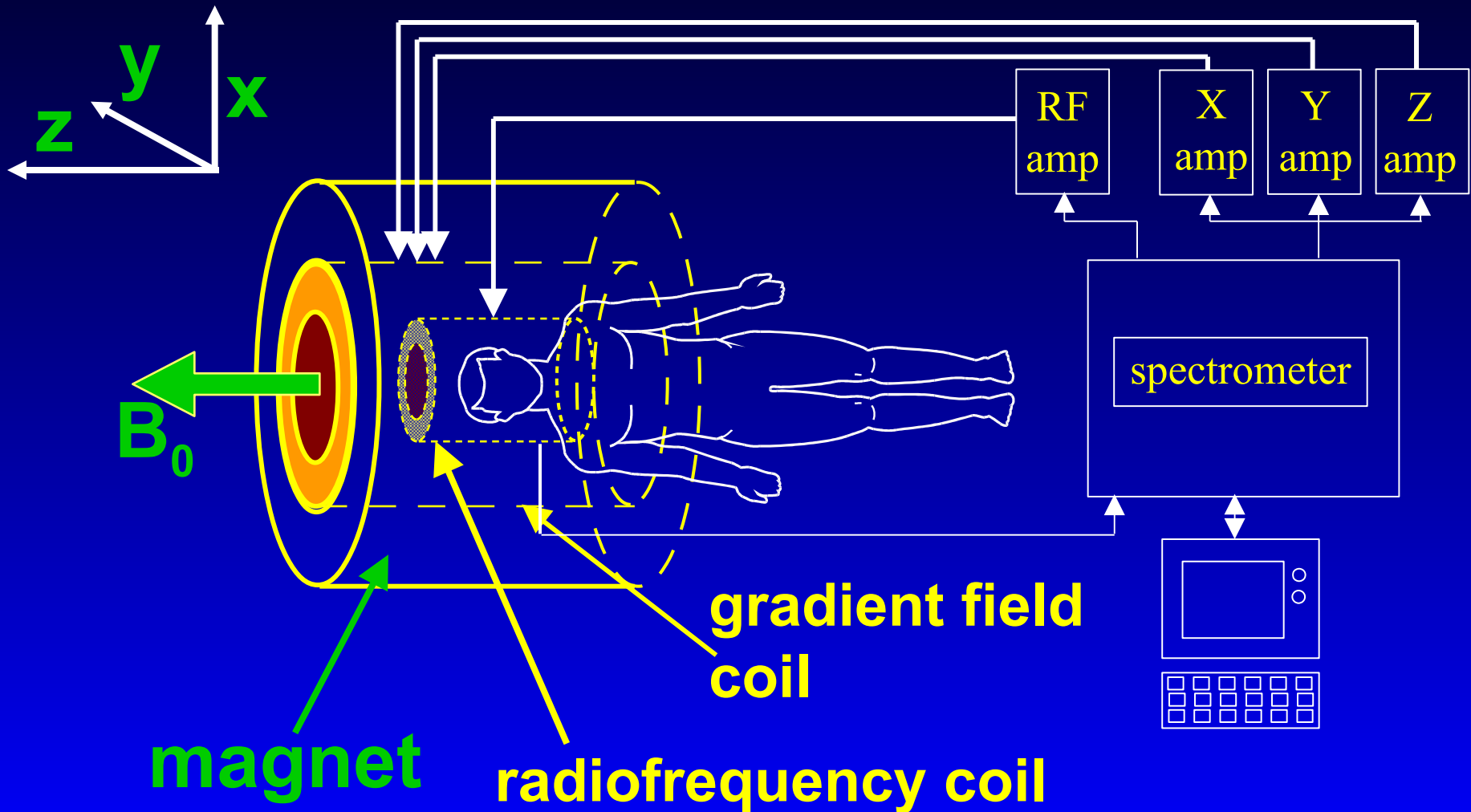
- μ rotates around B_0
- B_0 – external mag. field
- μ – spin moment
 - rotates around B_0 with Larmor frequency

$$f_L = \gamma B_0$$

- γ – gyromagnetic ratio
($\gamma = 42.58$ MHz/T for H)
- Total magnetization:

$$M = \sum \mu_i$$

MRI System Block Diagram



Magnetic Field of a Tomograph

- Induced magnetic field:
 - Electromagnets
 - Superconductive electromagnets
 - Permanent magnets
- Field strength
 - 0.5T – 3T, (up to 15T for research)
- Earth's mg. field : $0.3 - 0.7 \times 10^{-5}\text{T}$

Principle of MR Imaging

Absorption and emission of energy by spins in external magnetic field (resonance)

- **Equilibrium:** $M \parallel B_0$: Uncoupled μ_i vectors:

$$M_z = M, \quad M_{x,y} = 0$$

- **Absorption of RF (radiofrequency) energy:** excitation ($f = f_L$)

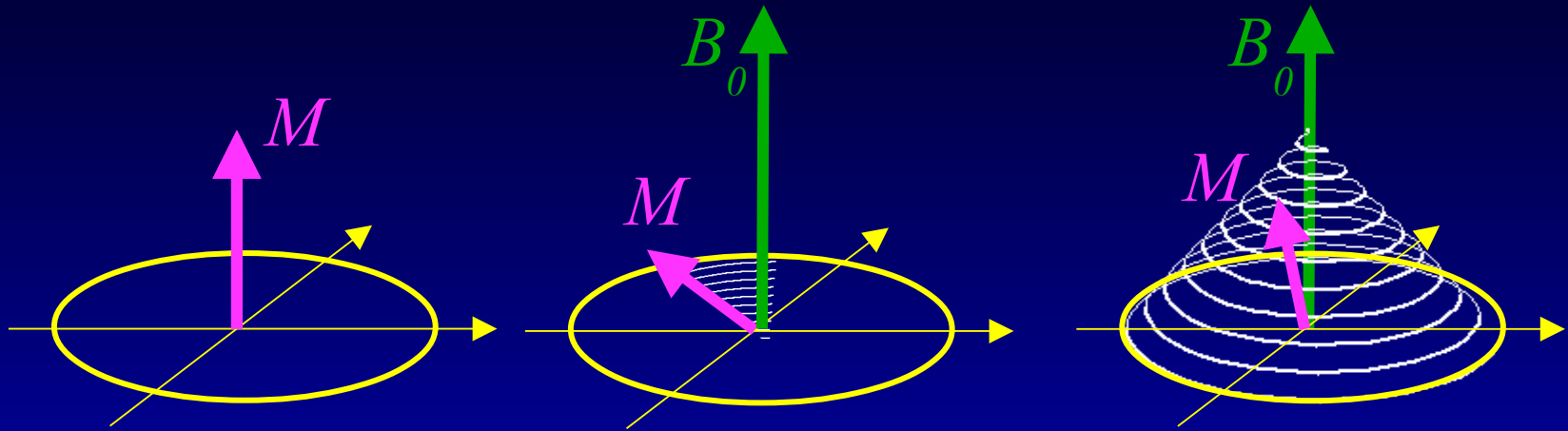
- Transition to higher energy state: $M_z < M$ owing to vector μ_i flipping

- Coupled rotation of μ_i : $M_{x,y} \neq 0$

- Measurable signal due to $M_{x,y}$

- **Relaxation:** return to equilibrium

Spin Excitation and Relaxation



Equilibrium

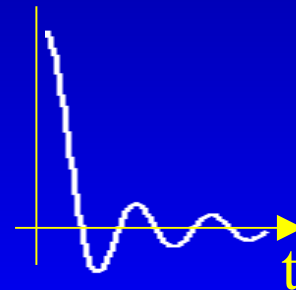
Excitation
by RF
impulse

Relaxation:
Return back to
equilibrium.

Relaxation

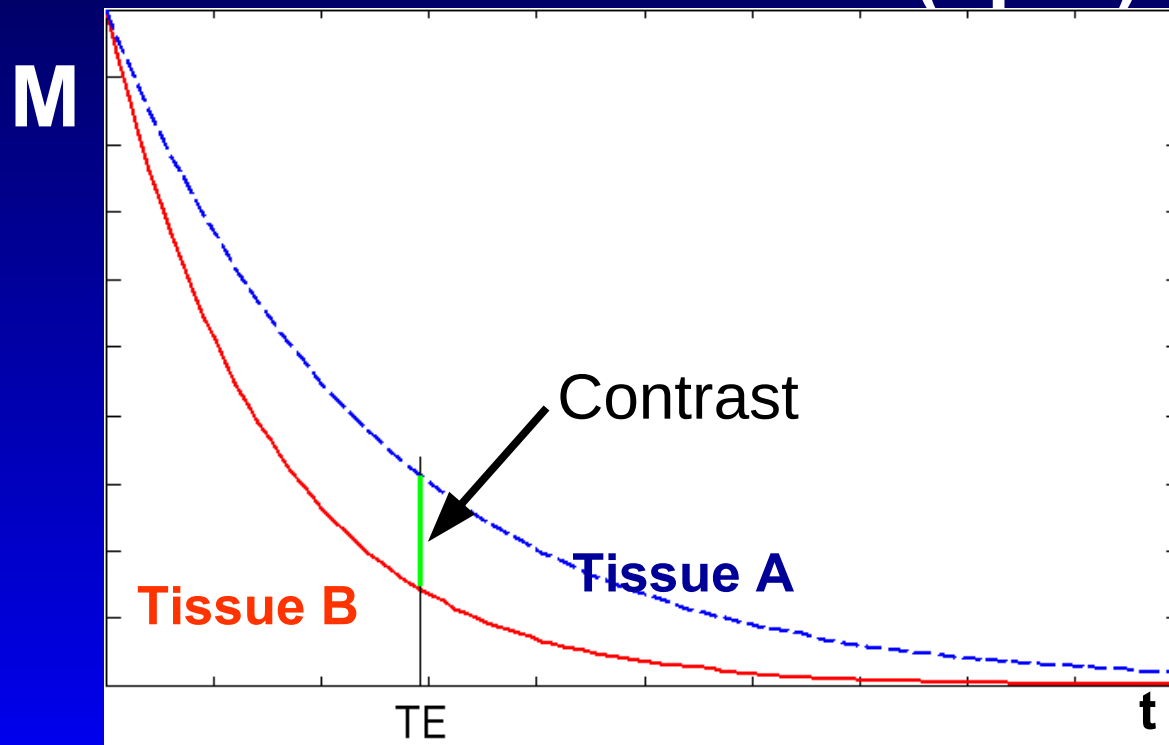
Return to equilibrium state after the RF pulse

- **Longitudinal relaxation** (spin-lattice, rate T_1):
 - Energy transfer to surrounding tissue
 - Flipping of μ_i vectors to original orientation
- **Transversal relaxation** (spin-spin, rate T_2):
 - Decoupling of μ_i due to field inhomogeneities and spin-spin interaction
- Measured signal during the relaxation
 - **FID** (Free Induction Decay)



Tissue Contrast

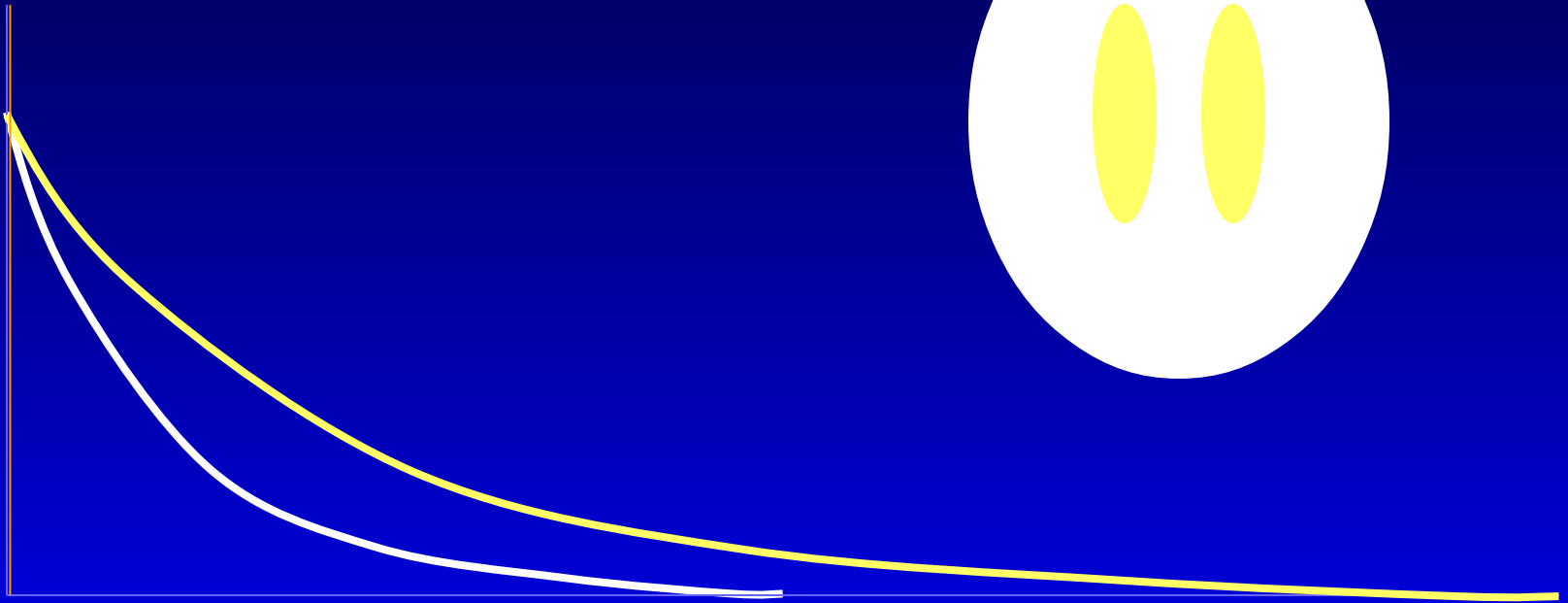
- Both T_1 and T_2 depend on the chemical environment of the nucleus (spin).



TE: time of measurement, echo time

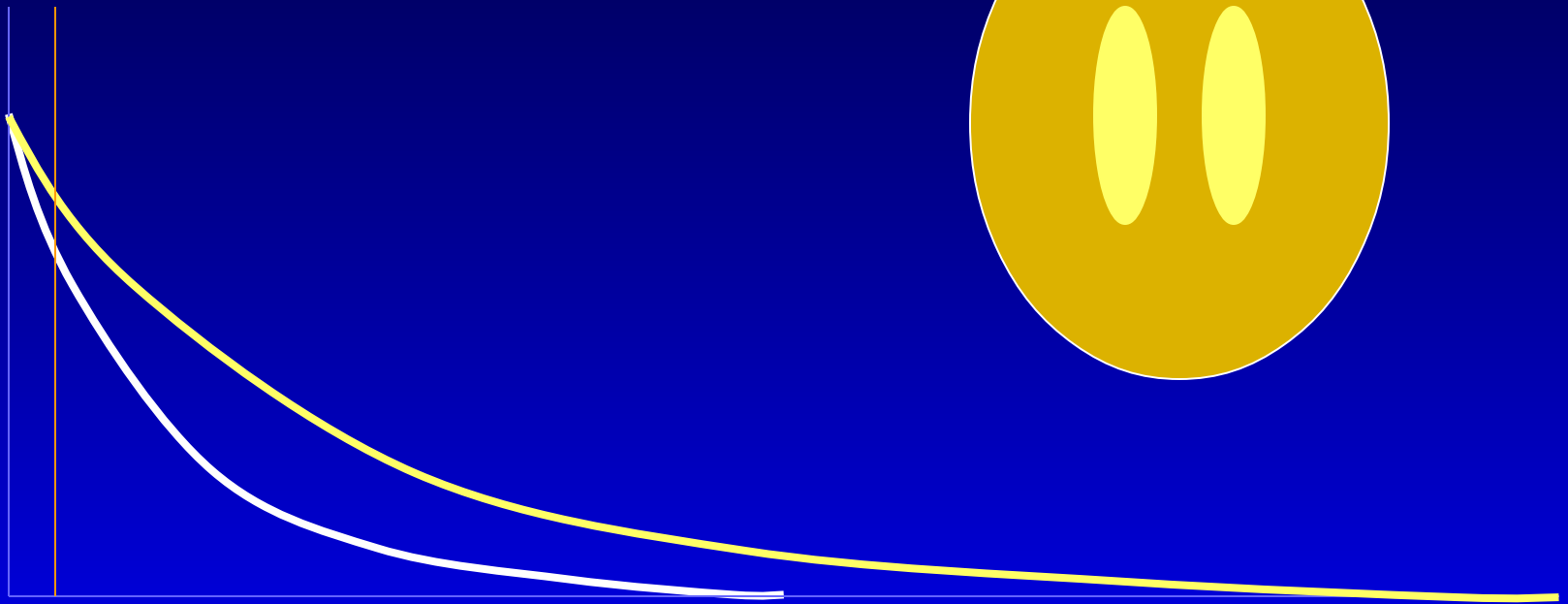
Tissue Contrast

- Effect of TE (echo time, time of measurement)



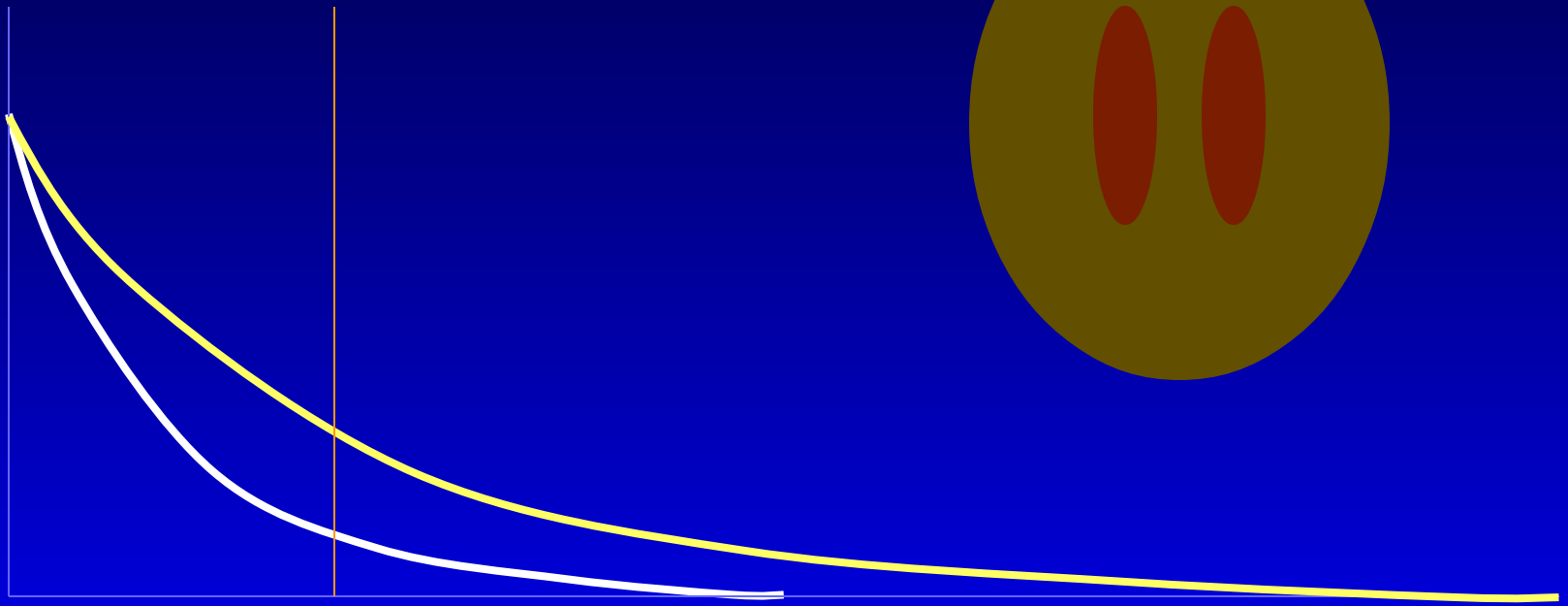
Tissue Contrast

- Effect of echo time



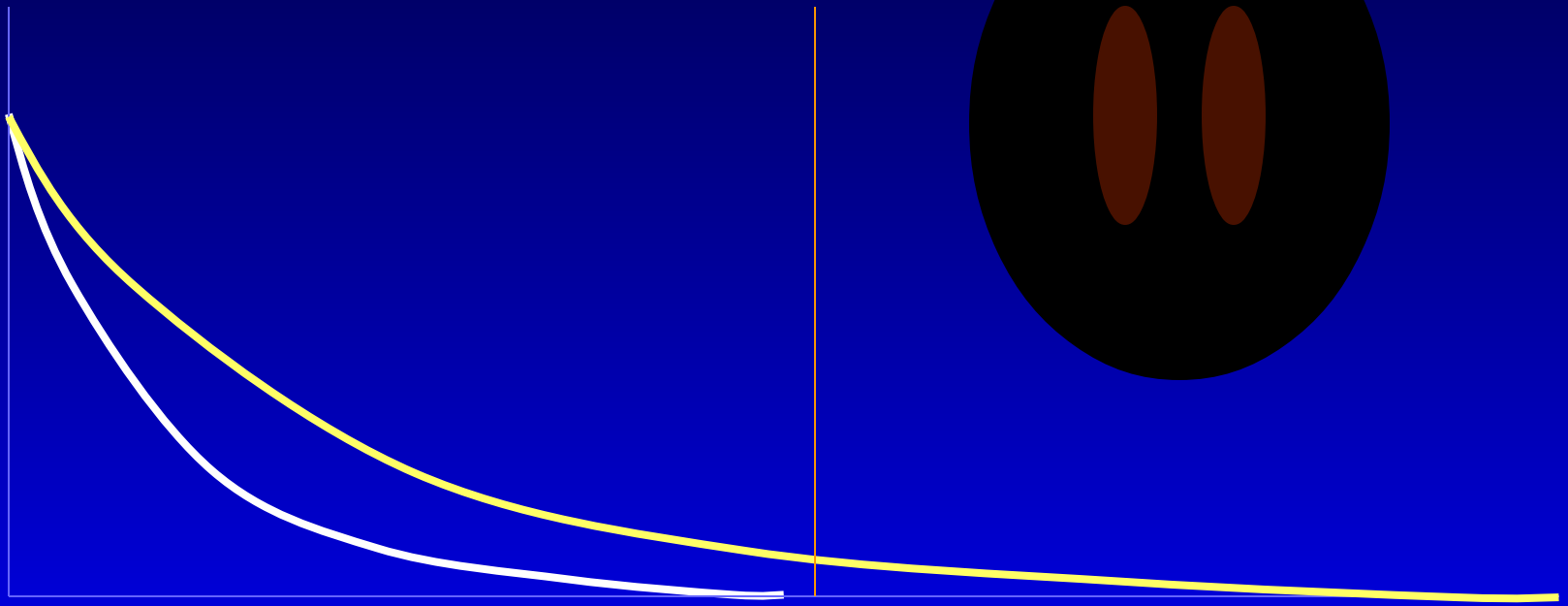
Tissue Contrast

- Effect of echo time



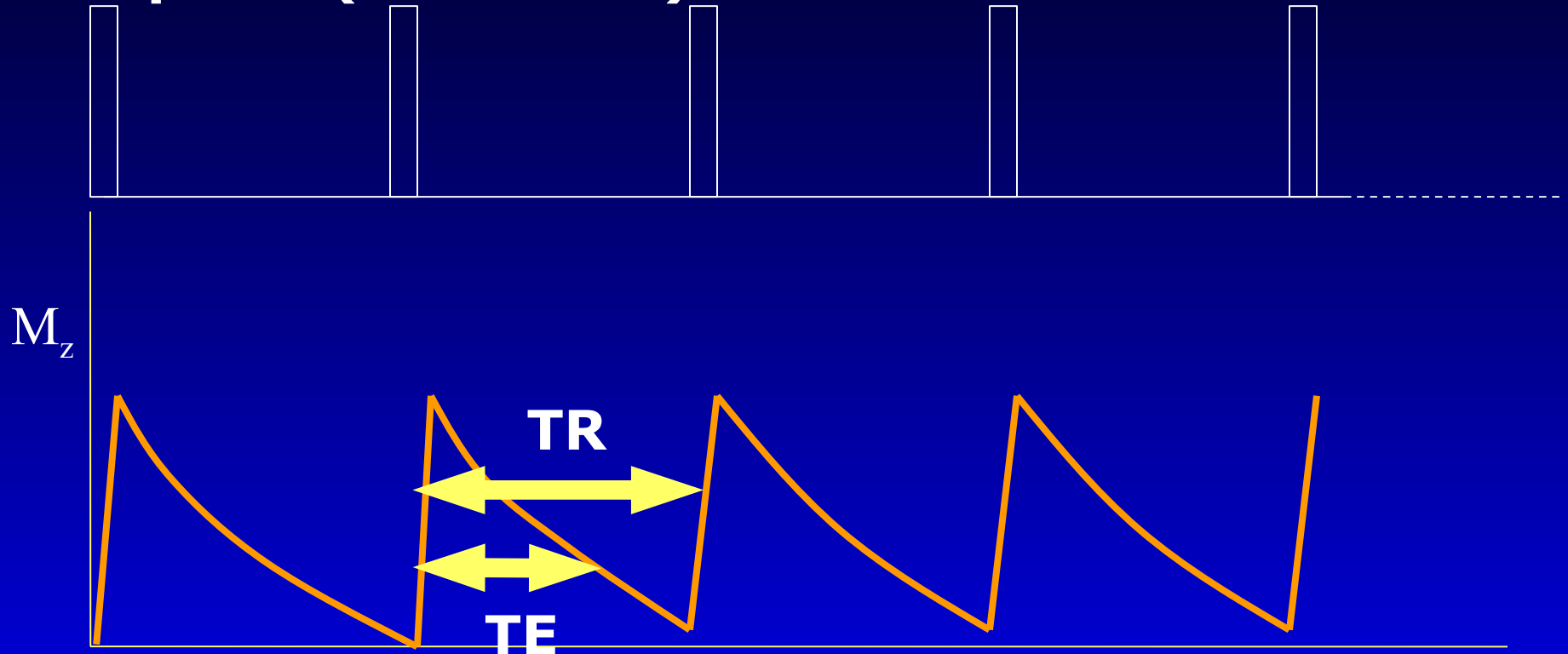
Tissue Contrast

- Effect of echo time



MRI Measurement

RF pulse (excitation)

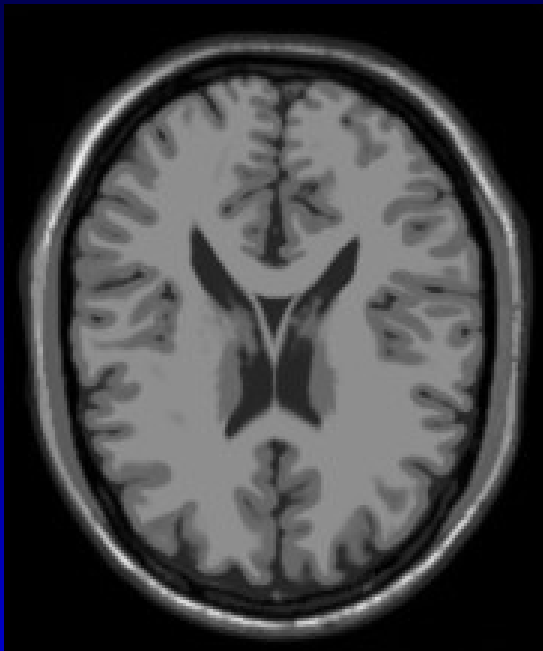


- TR: repetition time
- TE: excitation time, moment of measurement

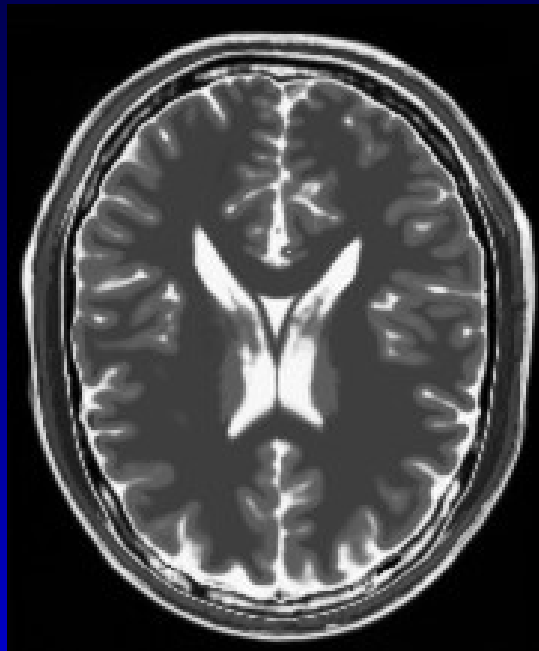
T_1 , T_2 and PD Images

- Different combinations of TR and TE yield different tissue contrast:
 - Long TR ($>1500\text{ms}$)
 - Short TE ($<25\text{ms}$) PD (Proton Density) weighting (no T_1 and T_2 influence)
 - Long TE ($>50\text{ms}$) T_2 weighting
 - Short TR ($<500\text{ms}$)
 - Short TE ($<25\text{ms}$) T_1 weighting

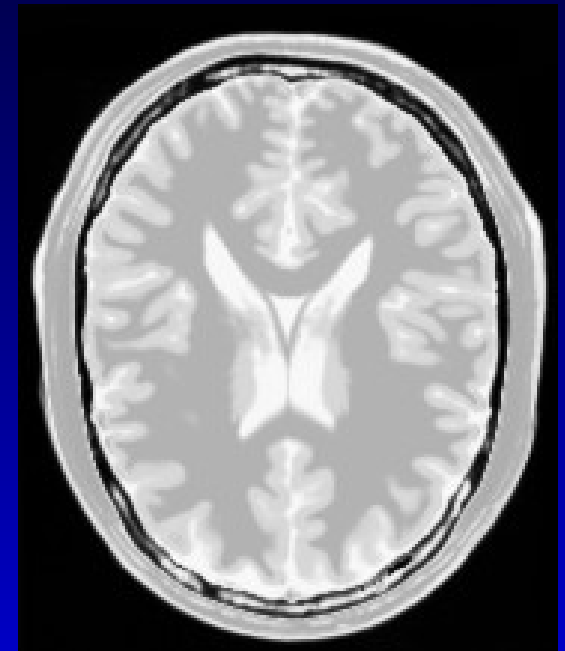
T₁, T₂ and PD Images



T1



T2



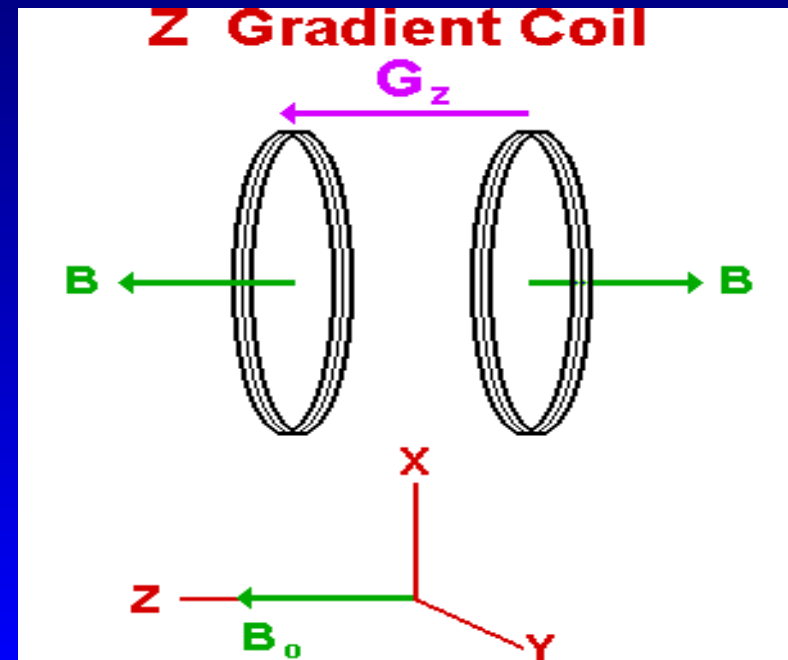
PD

MRI Overview

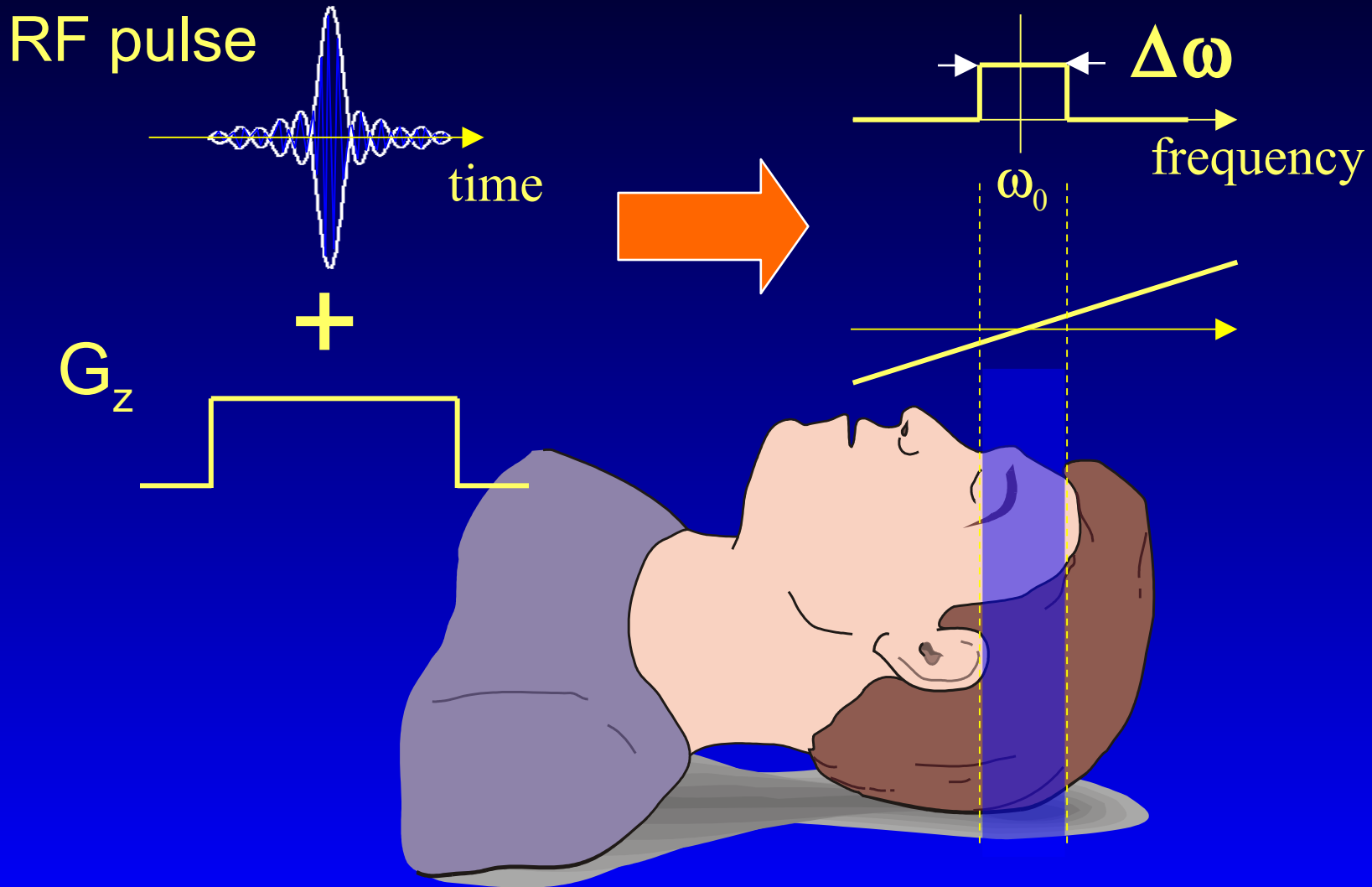
- Physical Background
- Excitation and Relaxation
 - T_1 Relaxation
 - Spin Echo and T_2 Relaxation
- **Coding of Spatial Information**
 - Slice Selection
 - Read-out Gradient
 - Phase Encoding

Spatial Localization in MRI

- Position encoding by means of gradient fields:
 - **Z-gradient**: slice selection by changing the Larmor frequency $f_L = \gamma(B_0 + G_z \cdot z)$
 - Z-gradient is applied during the RF pulse

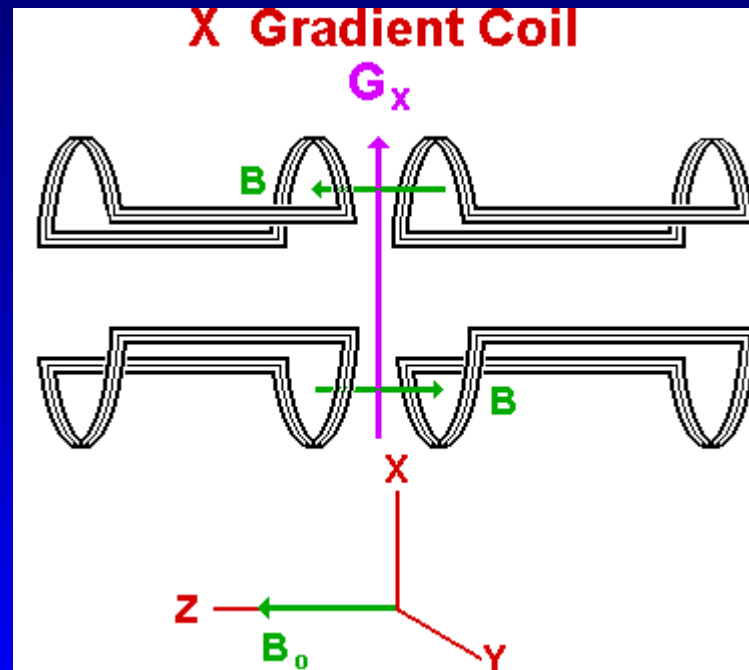


Slice Selection



X, Y encoding

- Similar tricks to encode the **x** and **y** coordinates
 - Only one row measured in one excitation



$$\frac{\partial B_z}{\partial x}$$

Examination Time

- Image is measured row-by-row
- Basic formula: $T = TR \times R \times N$ [ms]
 - TR : repetition time
 - R : number of image rows
 - N : Number of accumulations (noise)

Example: $T = 2000 \times 256 \times 2 = 17 \text{ min}$

- Speed-up:
 - Low excitation angle \Rightarrow shorter TR (low energy pulse)
 - Multislice techniques

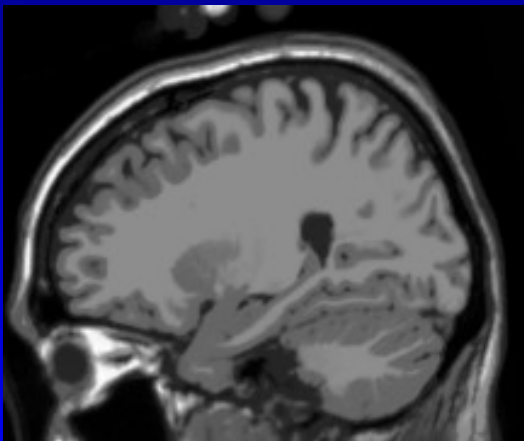
Multislice Technique

- Interleaved excitation of several (64) slices:

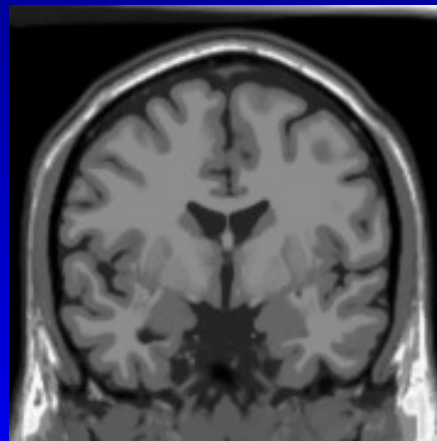


Imaging in Other Planes

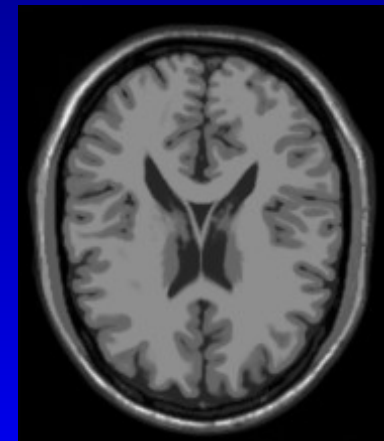
- B_0 always remains in the same direction
- Choice of imaging plane depends on the order of gradients' application
- Oblique planes: simultaneous application of 2 gradients



Sagittal



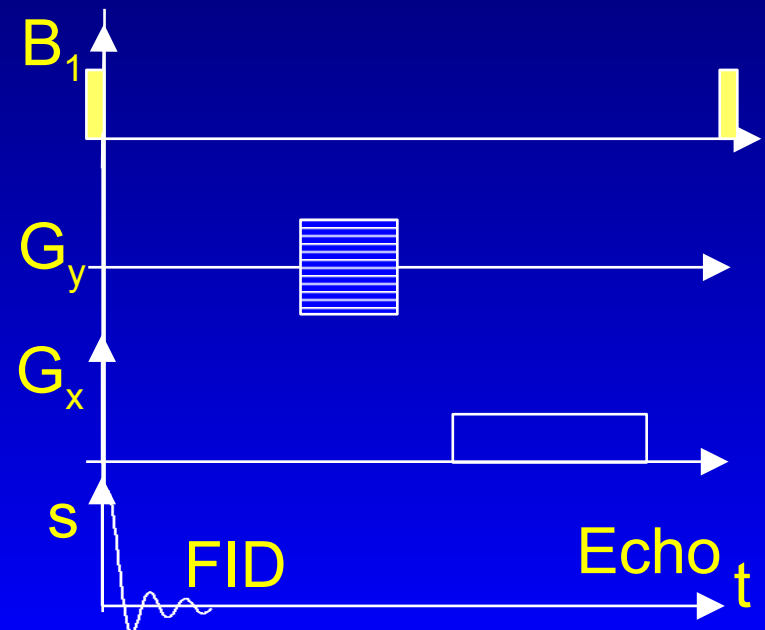
Coronal



Transversal

Scanning Protocols

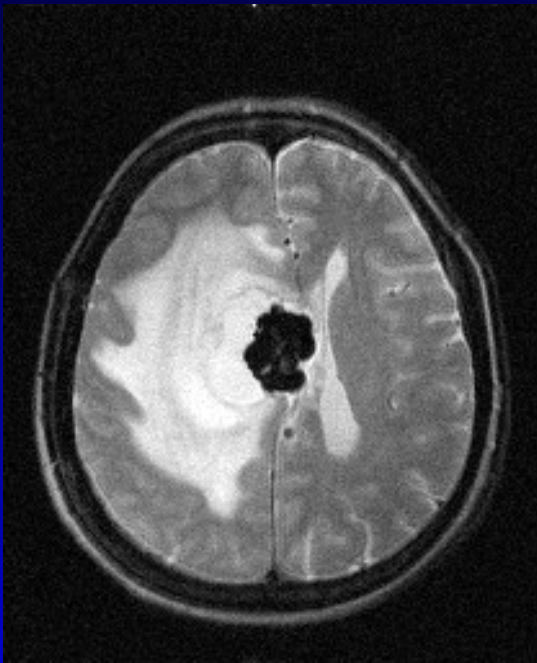
- **Protocol:** a sequence of pulses, gradients and signal measurements
- Protocols influence image properties and examination time
- Patented and sold by scanner vendors
- FISP, FAST, FLASH, STAGE, STERF



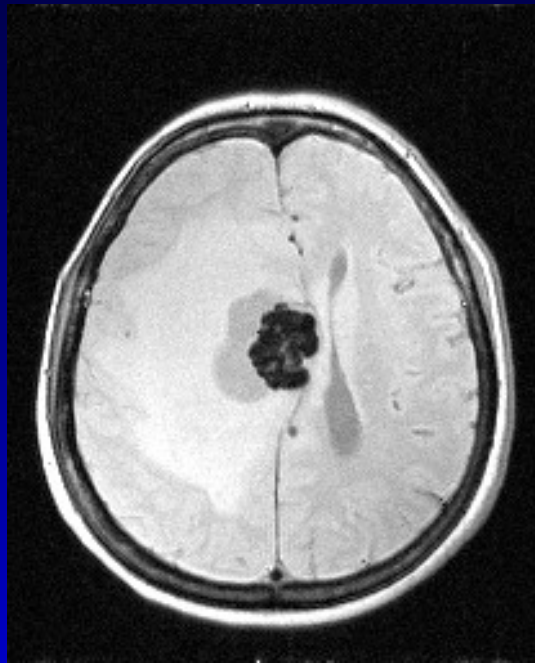
Properties of MR data

- Measurement in arbitrary planes
- Typically 256x256 (512x512) pixels
- No absolute scale for measured values
- Significant level of noise
- Good soft tissue contrast
- Spatial inhomogeneities - bias
- No irradiation

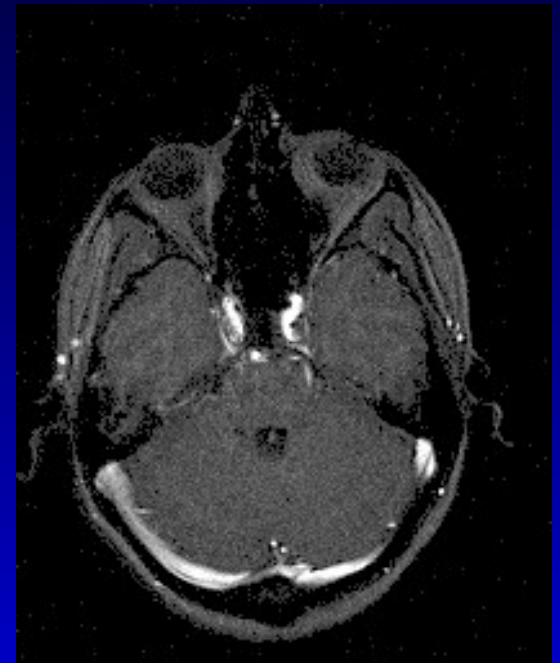
MR data - examples



T_1



PD



MRA

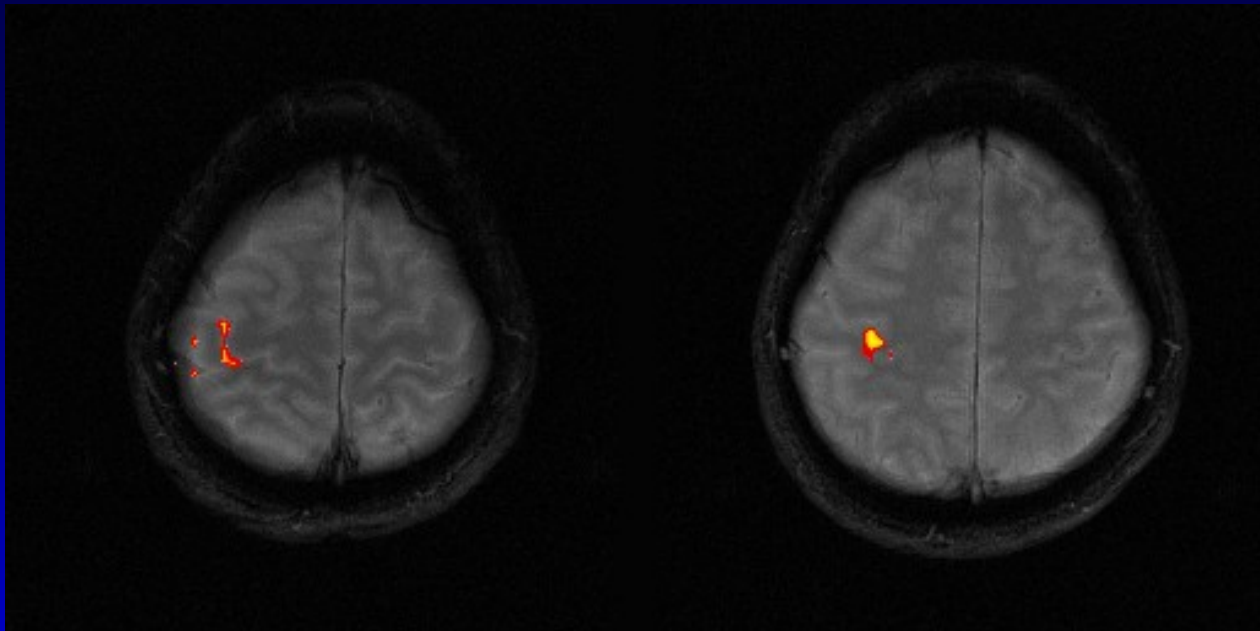
Overview

- Computer tomography (CT, CAT)
- Magnetic resonance imaging (MRI)
- **fMRI**
- **SPECT**
- **PET**

Functional MRI (fMRI)

- **Assumption: Active brain area needs more oxygen than inactive ones**
- **fMRI: statistical detection of areas with oxygenated blood flow**
- **Visualization by merging with regular MRI data**

fMRI Example



Right hand finger tapping at 2Hz

Overview

- Computer tomography (CT, CAT)
- Magnetic resonance imaging (MRI)
- fMRI
- **Emission Tomography**
 - SPECT
 - PET

Emission Tomography

ECT - Emission computed tomography

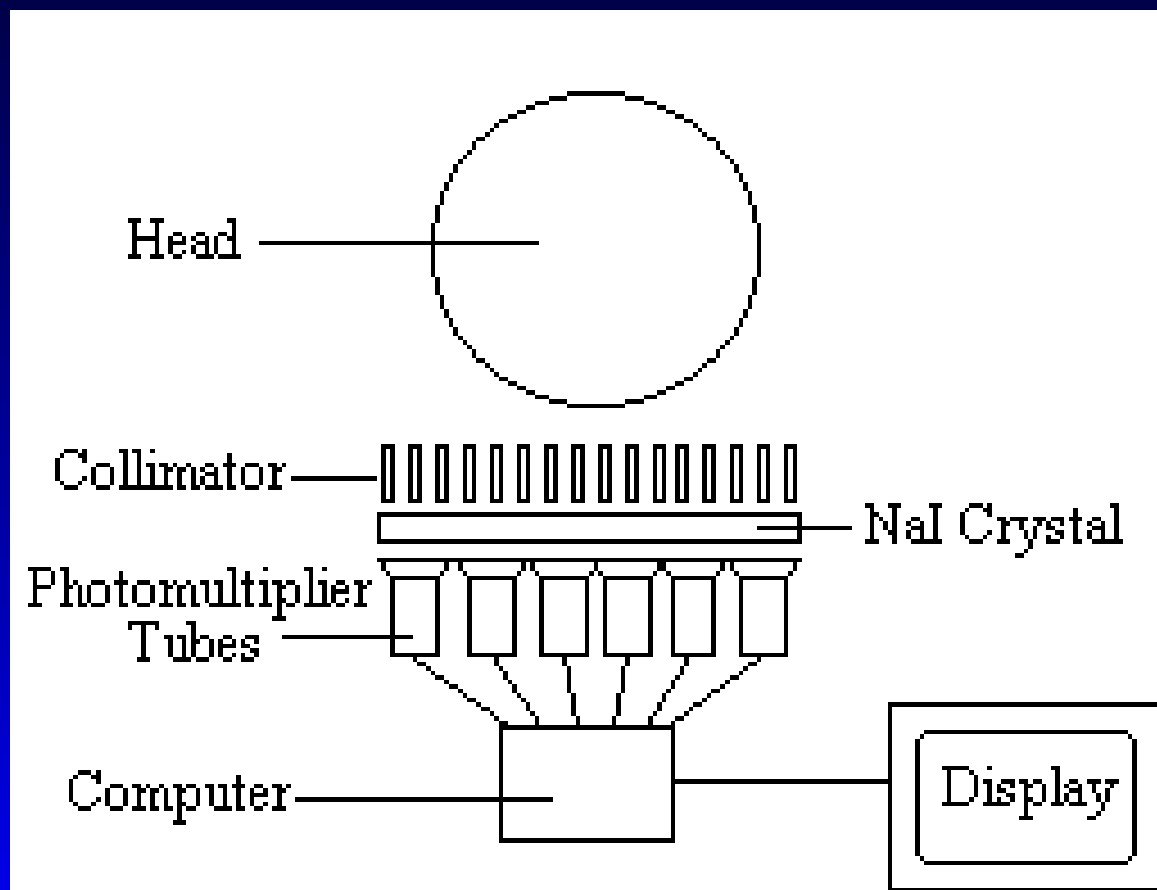
- Introduction of a radioactive agent into the patient's body (tagged substance)
- Agent's distribution based on metabolism
- Measurement of its spatial distribution

SPECT

Single-Photon Emission Computed Tomography

- Isotopes emitting γ -photons (Tc-99, I-125, I-131)
- Uniform distribution of photons in all directions
- Scanner - a set of detectors with collimators - gamma camera

Gamma Camera



Gamma Camera

radiation area and creates an image.

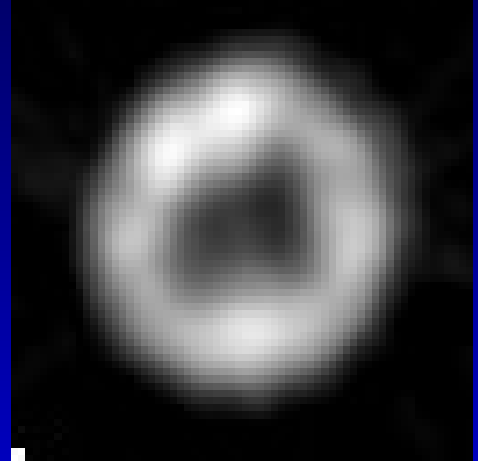
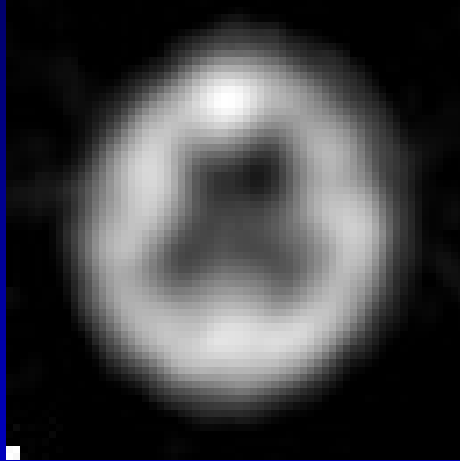
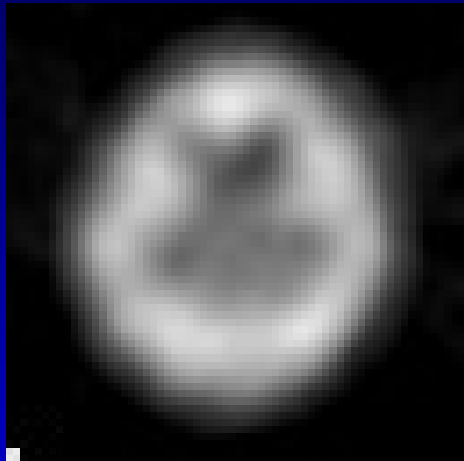


Gamma
camera



ADAM.

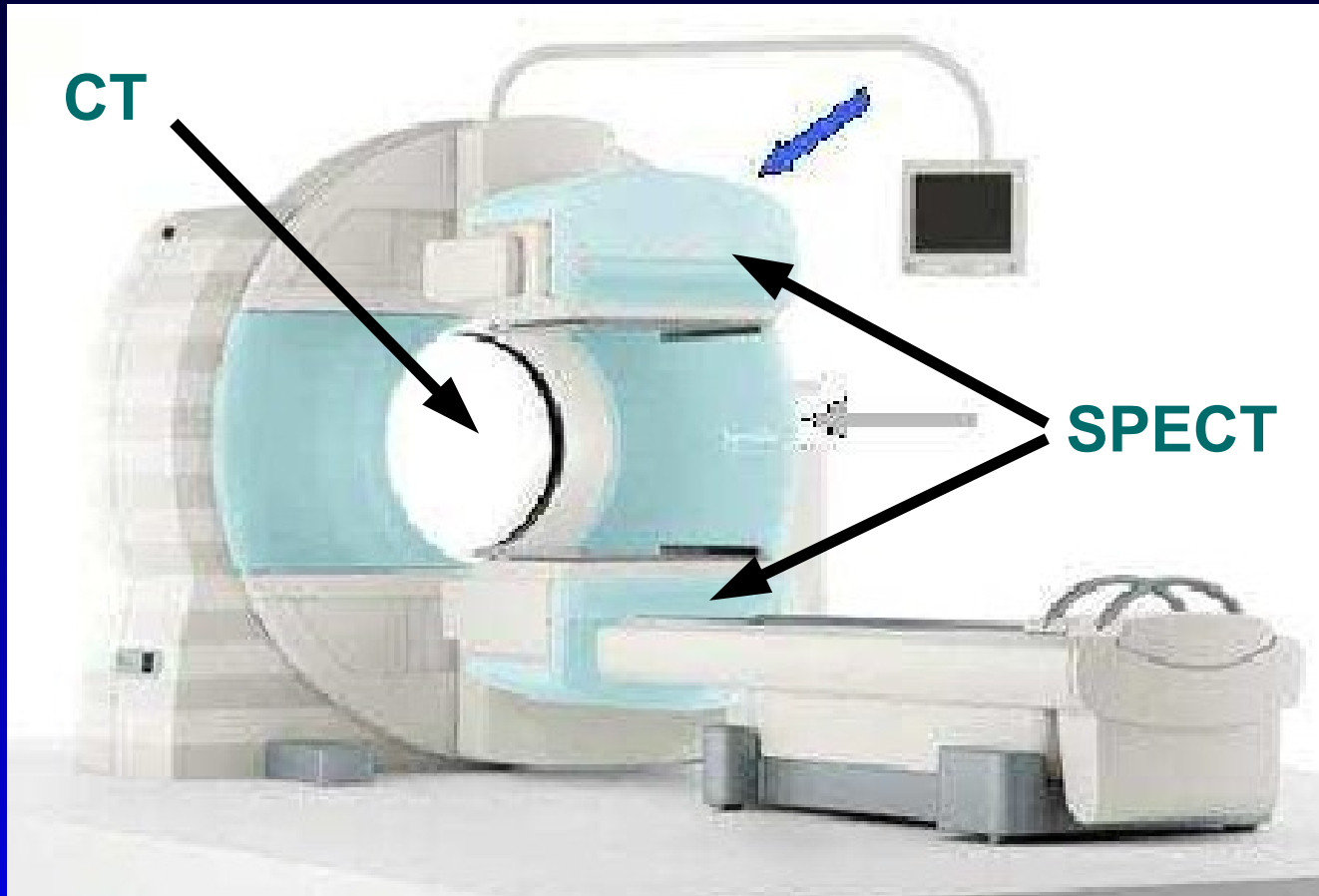
SPECT data



CT-SPECT

- **Combination of different techniques – supplementary information**
- **Registration is required**
 - **Not a trivial task**
 - **Solution: CT-SPECT scanner**

CT-SPECT (2)

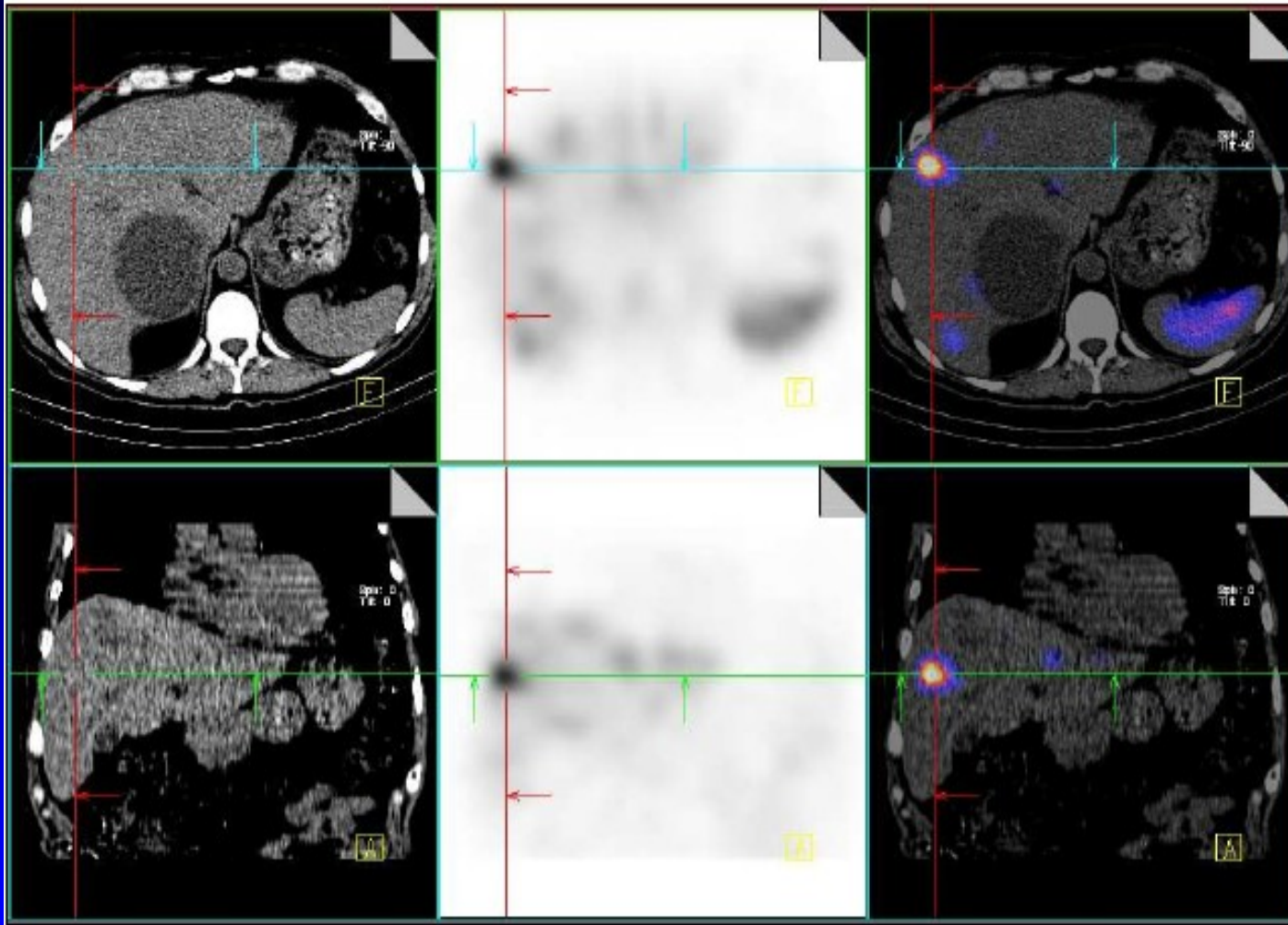


CT-SPECT (3)

CT Image:

SPECT Image:

Fused Image:

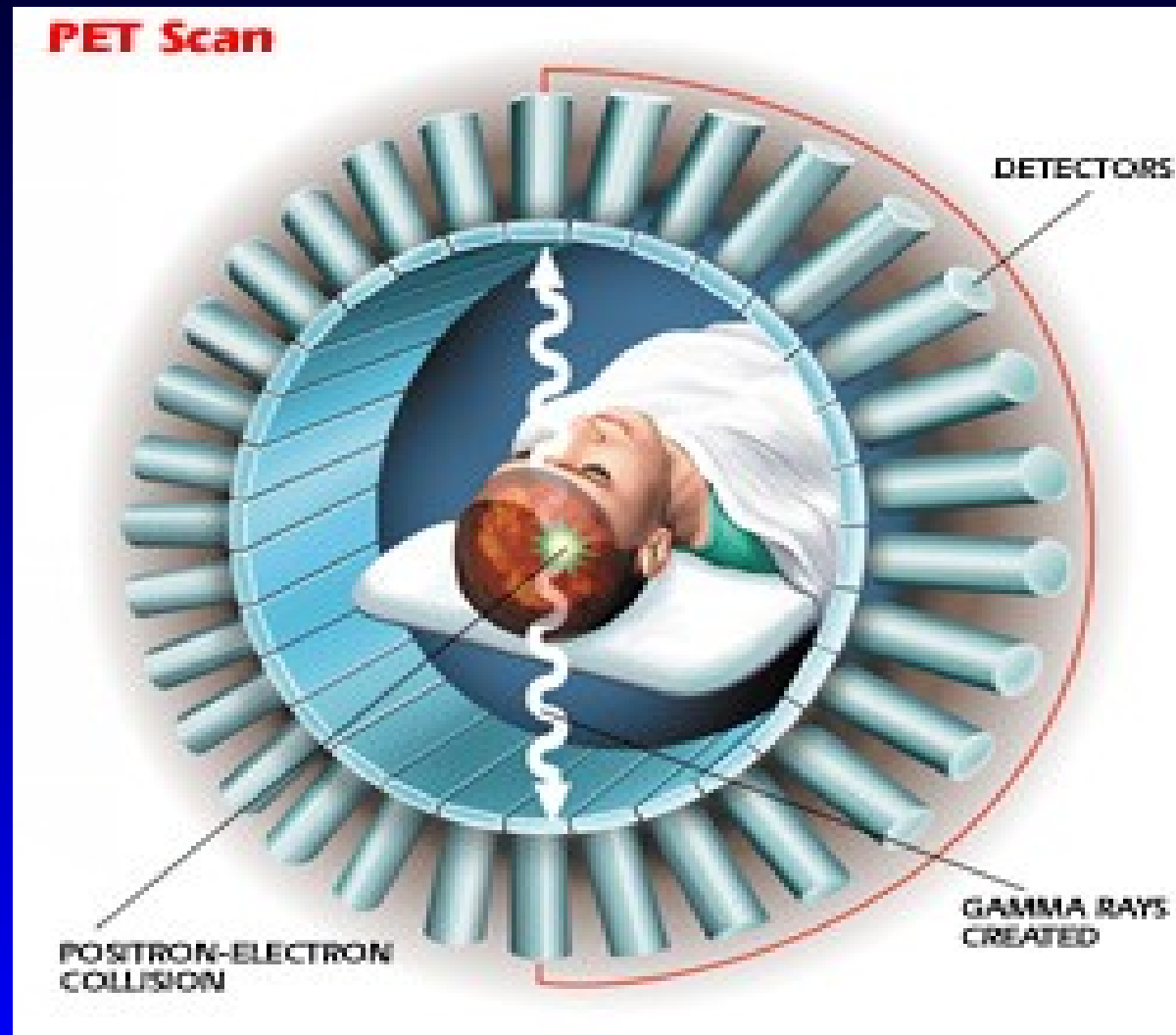


PET

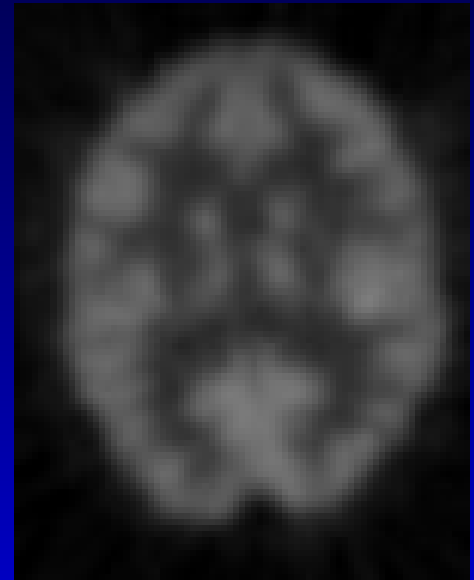
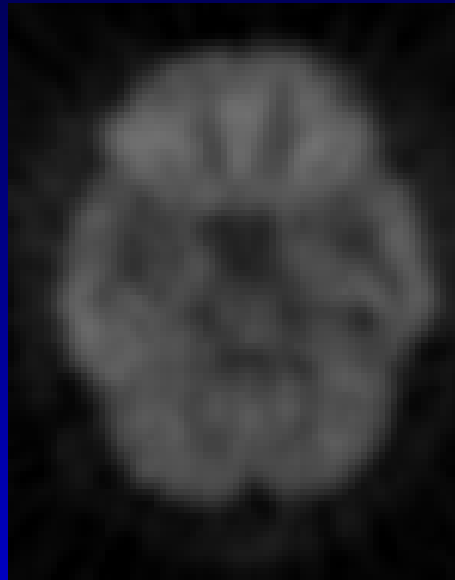
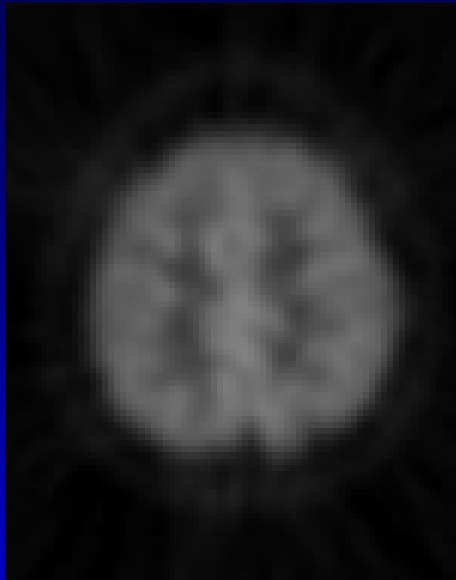
Positron Emission Tomography

- β^+ decay (positrons)
- Annihilation - a pair of photons with energy 511keV in opposite directions
- Detection without collimators:
registration of *concurrent* events in detector pairs
- 3D measurement, statistical reconstruction (MRF)

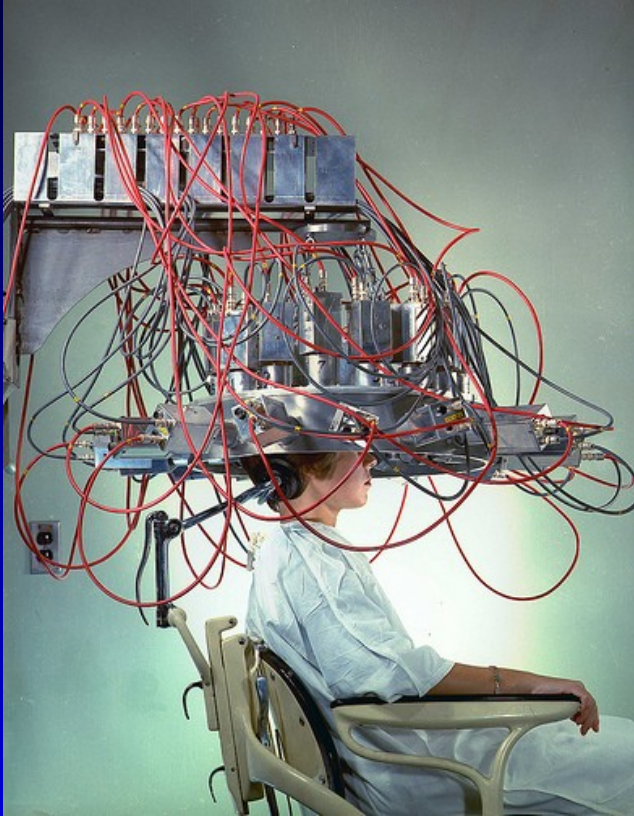
PET Scanner



PET data



PET Scanners

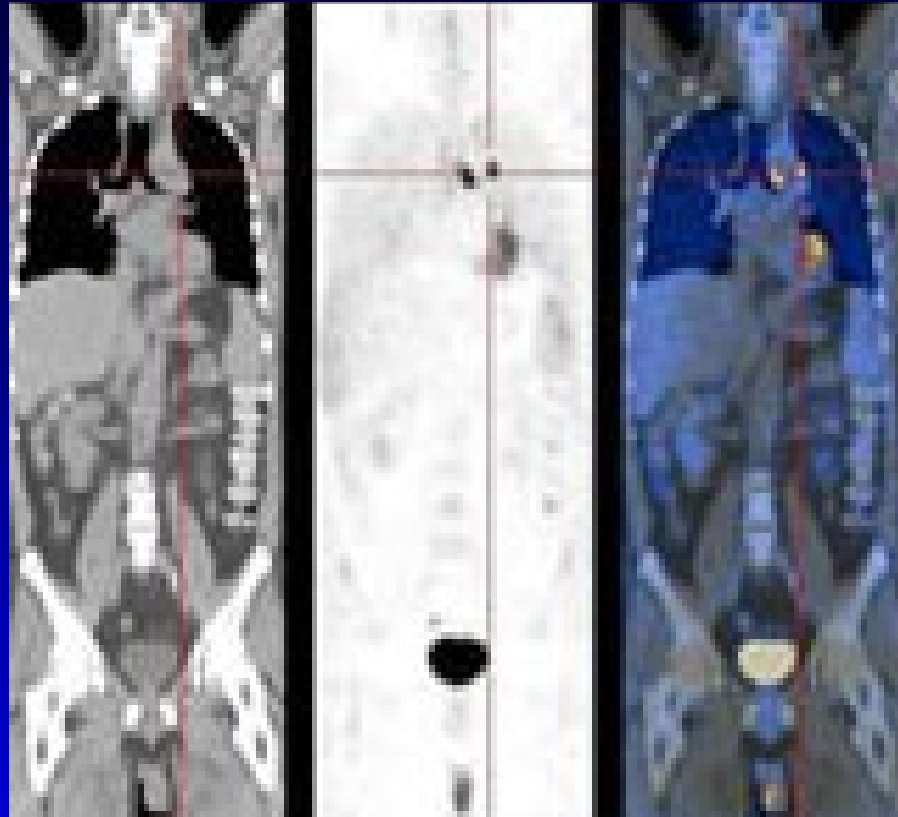


Research prototype
at BNL (1961)

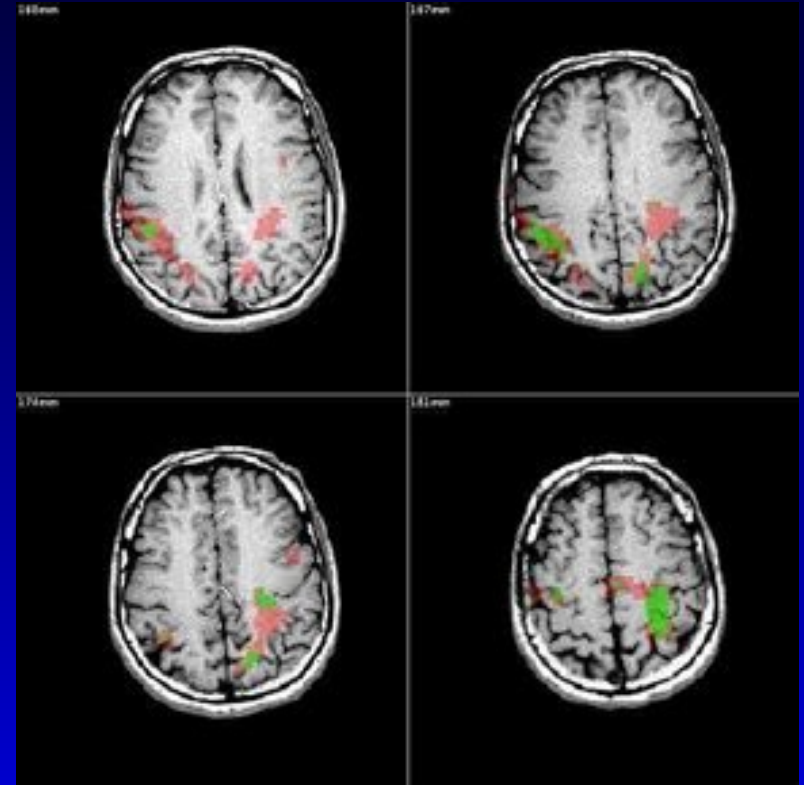


PET today

Combined PET/CT, MRI



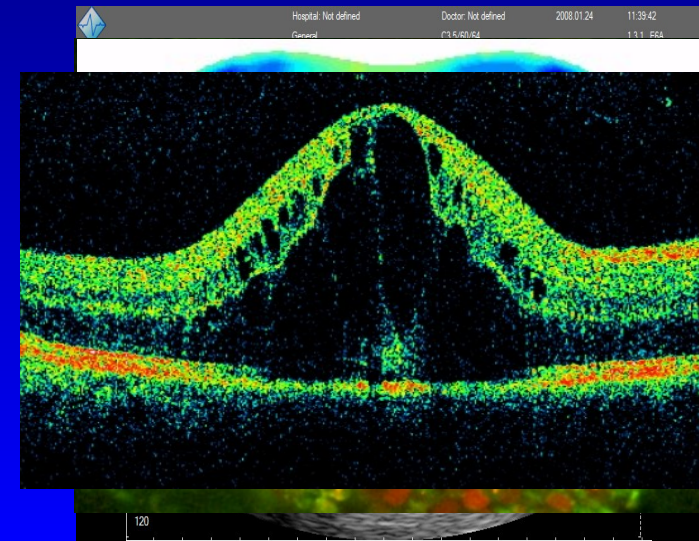
PET / CT



PET / MRI

Other Imaging Modalities

- Ultrasound
- Confocal microscopy
- Electrical impedance tomography
- Optical coherence tomography
- ...



Overview

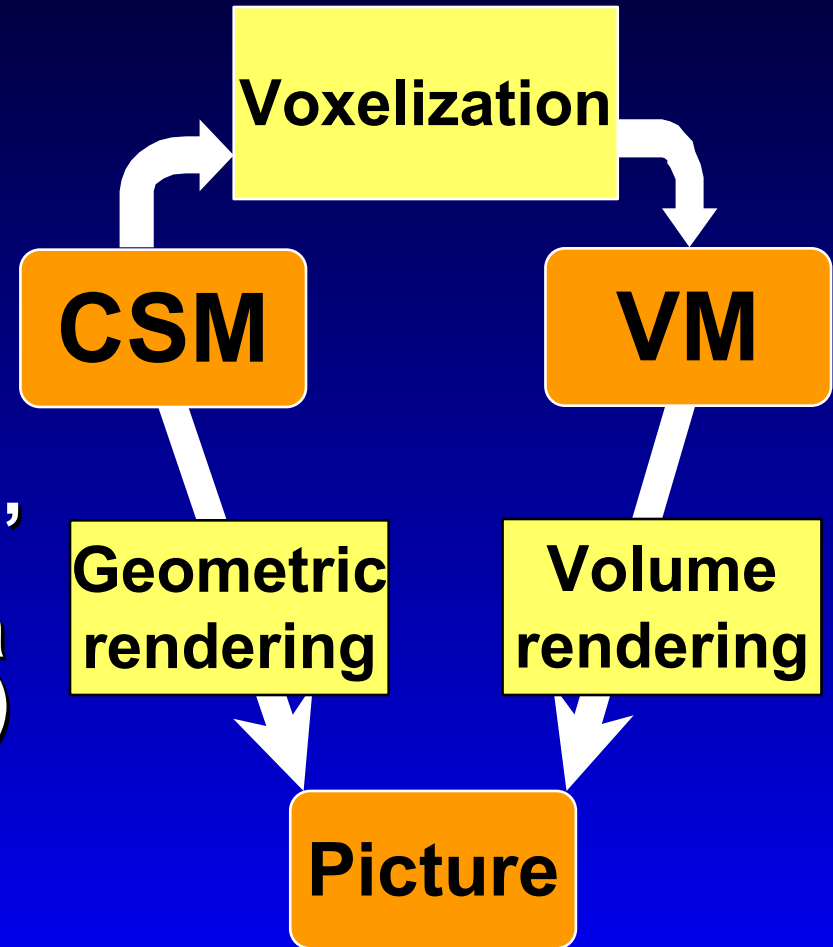
- Computed tomography (CT / CAT)
- Magnetic resonance imaging (MRI)
- fMRI
- SPECT
- PET
- **Synthetic Data**

Voxelization of Geometric Objects

- Preparation of “synthetic” data
- A CG alternative
- Simultaneous visualization of geometric and volume data
- Modeling of volumetric properties (e.g. weathering)

Surface and Volume Graphics

- **Surface Graphics:** Geometric rendering of Continuous Spatial Models (CSM)
- **Volume Graphics:** Voxelization of a CSM, manipulation, and volume rendering of a Volumetric Model (VM)



Voxelization

- ◆ A **process** of approximating a continuous geometric primitive in the 3D discrete space
- ◆ The **result** of this process

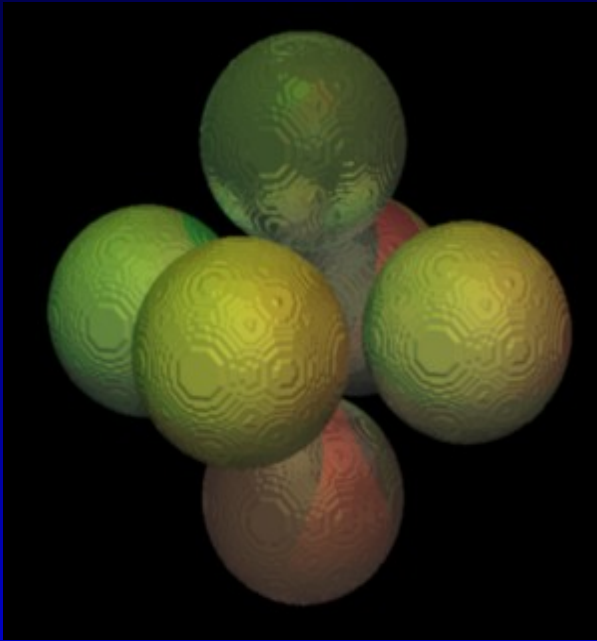
Binary voxelization

Voxels & occupancy $O \in \{0,1\}$ ({Background, Foreground}, {Black, White})

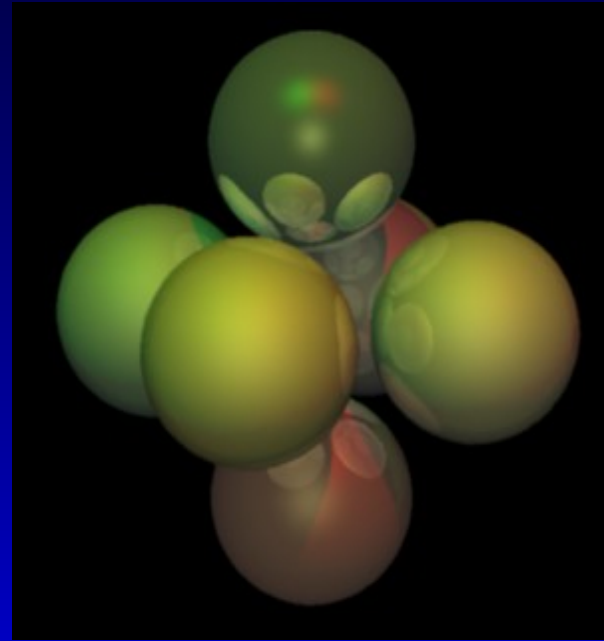
Non-binary voxelization (fuzzy, filtered)

Grid points & densities $D \in \mathbb{R}$

Binary vs. nonbinary



Binary

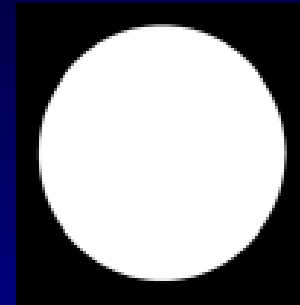


Non binary

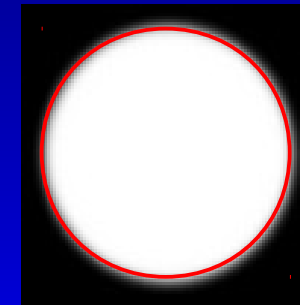
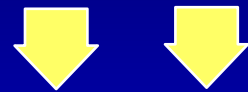
Non-binary Voxelization

Suppression of aliasing in 3D model by smooth density transition in the surface area

- Truncated distance field
- Surface reconstruction
 - Interpolation and thresholding

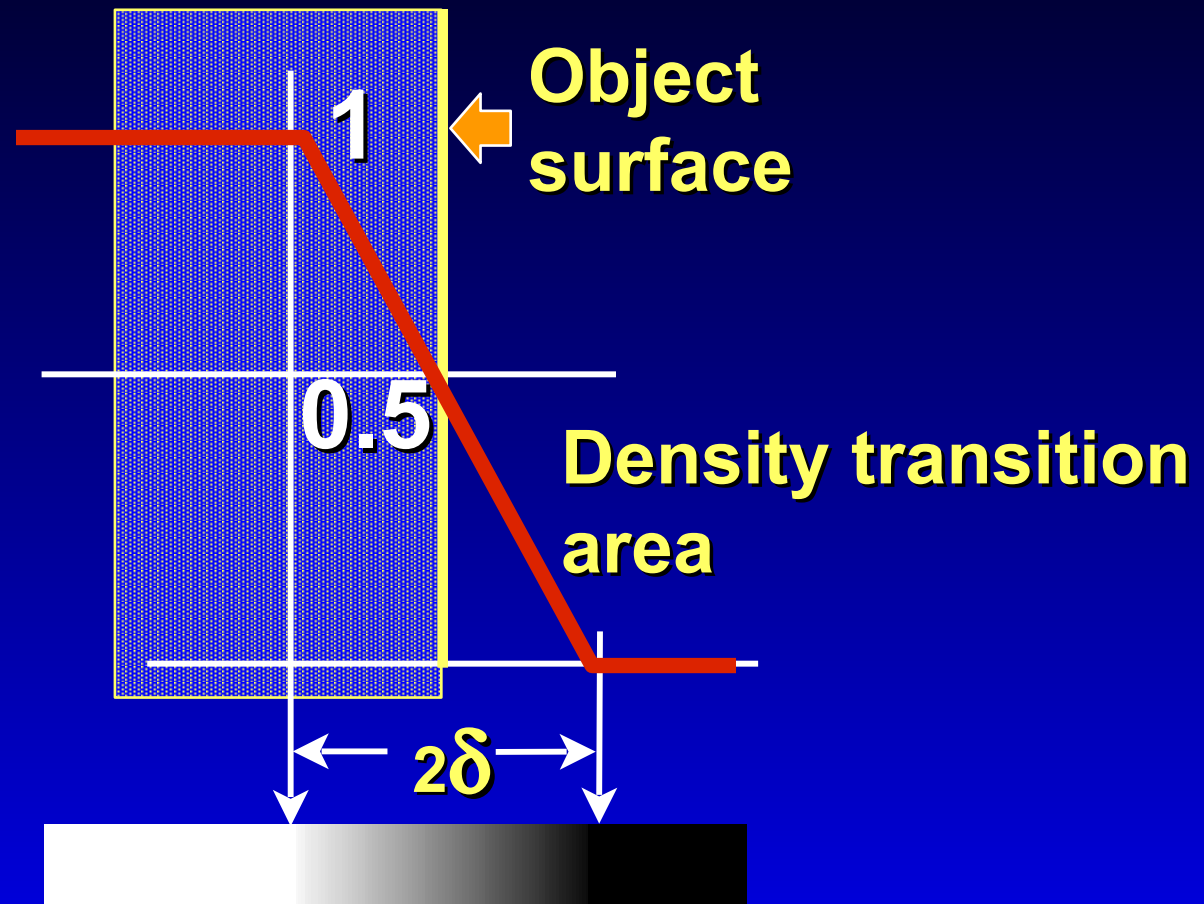


Analytic object



Voxelized object

Solids in Truncated Distance Fields



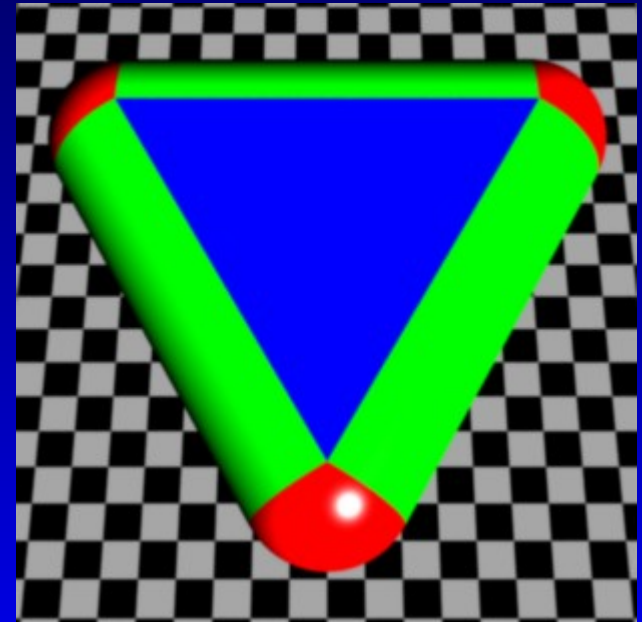
Surface density profile

Voxelization by Direct Distance Computation

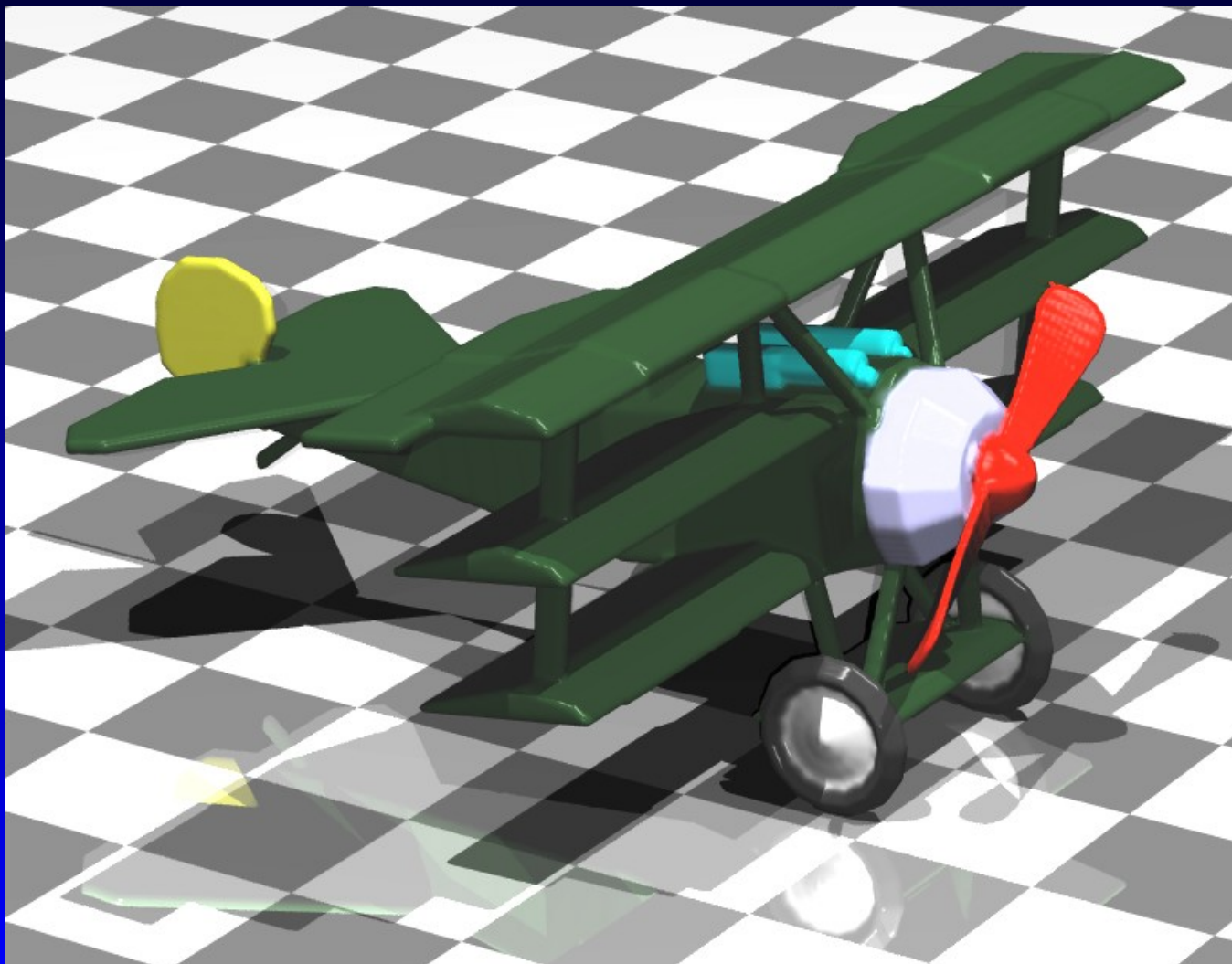
Simple primitives (sphere, torus, polygon)

Example: Voxelization of a triangle:

- Bounding box
- Voxel-by-voxel update of distances to **plane, edges & vertices**
- Density according to the minimal distance



Voxelized Polygonal Model



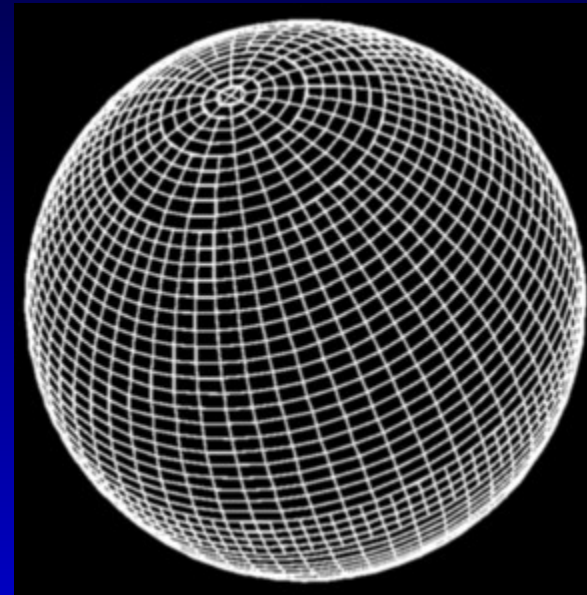
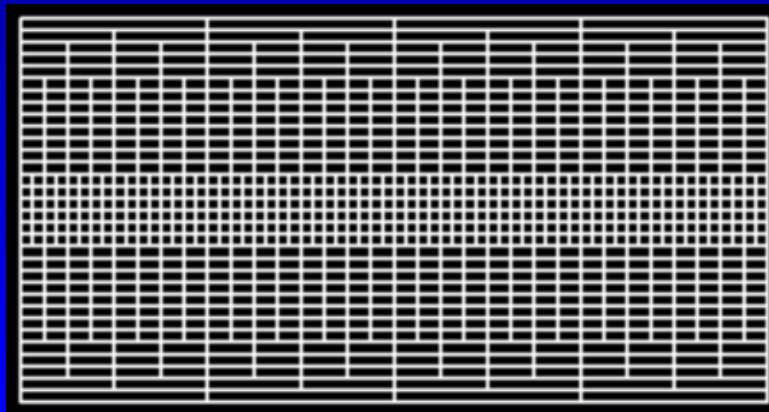
Voxelization of Parametric Surfaces

$$P(u,v) = [x(u,v), y(u,v), z(u,v)]$$

$$[u, v] \in (u_0, u_1) \times (v_0, v_1)$$

1. Splatting – adding small voxelized balls
2. Approx uniform sampling by binary domain subdivision

**Domain
subdivis.**



**Surface
subdivision**

Voxelization of Parametric Surfaces



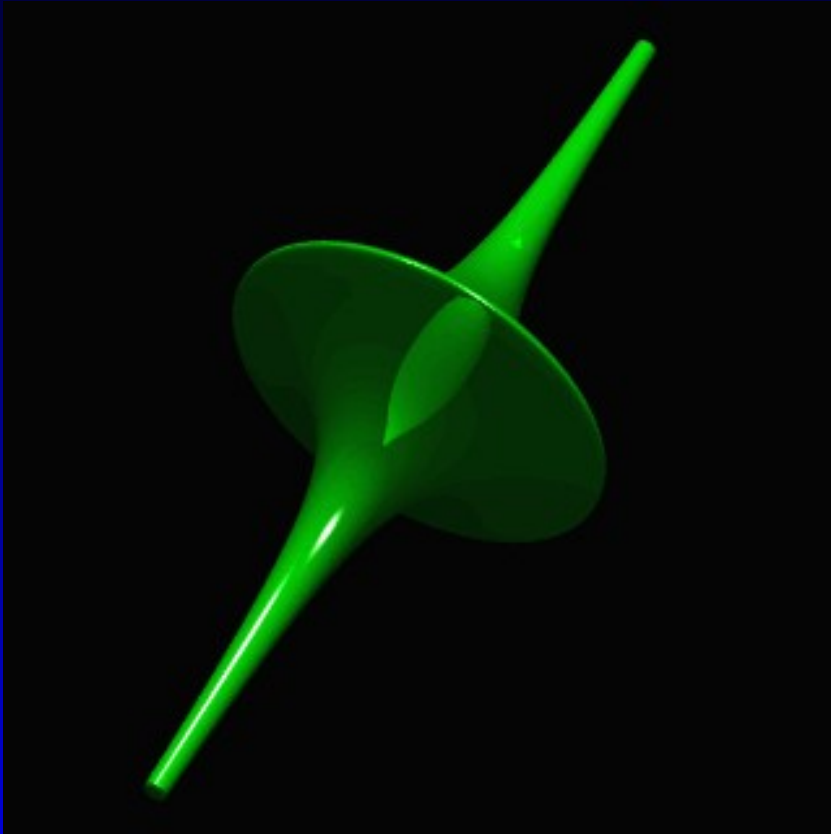
Voxelization of Implicit Solids

$$\{[x,y,z]: f(x, y, z) < 0\}$$

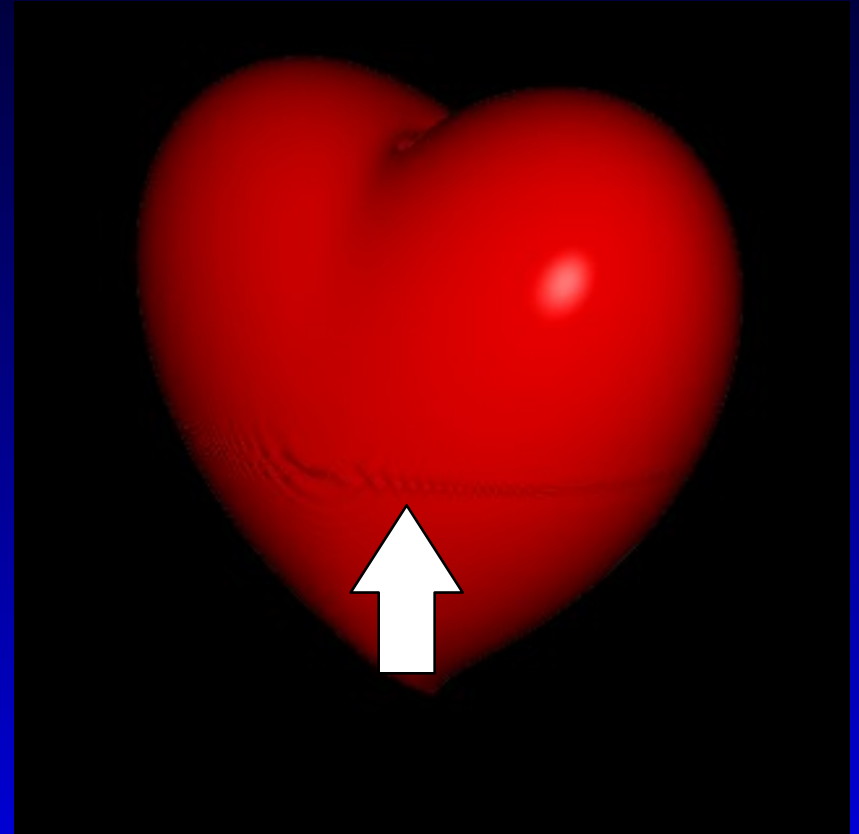
- **Distance estimation by linear approximation:**

$$d(x, y, z) = \frac{f(x, y, z)}{\|f'(x, y, z)\|}$$

Voxelization of Implicit Solids



$$(y^2 + s)(x^2 + z^2) - s$$



$$(2x^2 + y^2 + z^2)^3 - (x^2/10 + y^2)z^3$$

CSG Operations

Operation	Density	Color
Intersection	$d_{A*B} = \text{Min}(d_A, d_B)$	$C_{A*B} = \text{WA}(A, B)$
Union	$d_{A+B} = \text{Max}(d_A, d_B)$	$C_{A+B} = \text{WA}(A, B)$
Difference	$d_{A-B} = \text{Max}(0, d_A - d_B)$	$C_{A-B} = C_A$ if $d_{A-B} > 0$

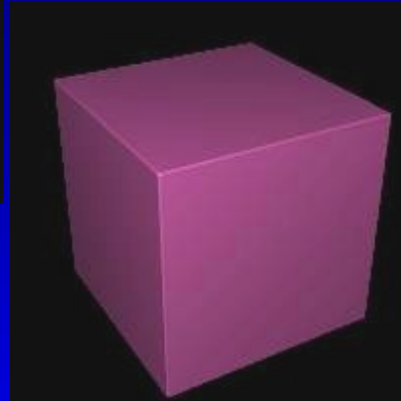
CSG Operations



a



b



c

$a * (b + c)$

