

## Advanced 3D-Datastructures



## 3D-Datastructures: Requirements

- general objects
- exact representation of objects
- generation of models via digitization
- combinations
- linear transformation
- interaction
- memory consumption
- fast rendering

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## 3D-Datastructures: Overview

- Point Cloud
- Wireframe
- Boundary Representation
- Binary Space Partitioning Tree
- Extended Octree
- Bintree
- Grid

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## Point Cloud

Object = set (list) of points

- e.g. from a digitizer
- for fast and simple preview
- exact representation if  $\geq 1$  points/pixel  
(more efficient than 1 pixel sized polygons)

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## Operations with Point Clouds

- **transformations**  
multiply the points in the point list with linear transformation matrices
- **combinations**  
objects can be combined by appending the point lists to each other
- **rendering**  
project and draw the points onto the image plane

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## Point Cloud Properties

- **advantages**
  - fast rendering
  - exact representation & rendering possible
  - fast transformations
  - generation of models via digitization
- **disadvantages**
  - many points (curved obj., exact representation)
  - high memory consumption
  - limited combination operations

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## Surfels (SURFace ELeMentS)

<http://www.merl.com/projects/surfels/>

movies: cab, wasp, salamander with holes, salamander corrected (more movies on web page)



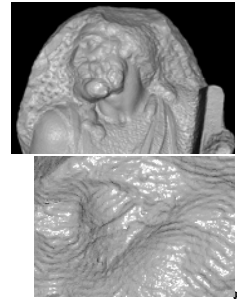
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## Qsplat (1)

- 3D scan of 2.7 meter statue of St. Matthew at 0.25 mm
- 102,868,637 points
- File size: 644 MB
- Preprocessing time: 1 hour
- Demo on laptop (PII 366, 128 MB), no 3D graphics hardware
- <http://graphics.stanford.edu/software/qsplat/>

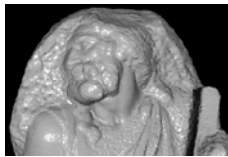


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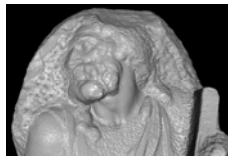
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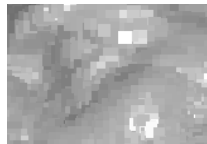
## Qsplat (2)



Interactive (8 frames/sec)



High quality (8 sec)



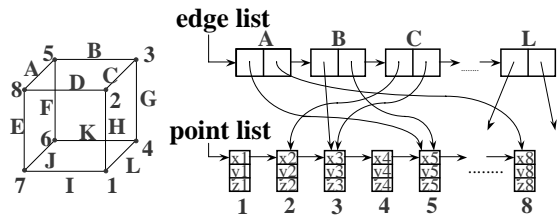
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## Wireframe

Object is simplified to 3D lines, each edge of the object is represented by a line in the model.



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## Operations with Wire-Frame Model

- **transformations**  
multiply the points in the point list with linear transformation matrices
- **combinations**  
objects can be combined by appending the point and edge lists to each other
- **rendering**  
projection of all points onto image plane and drawing of edges in between

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## Wire-Frame Model Properties

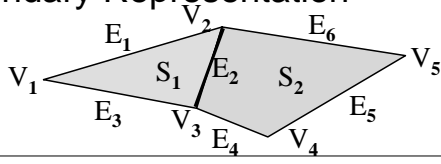
- **advantages**
  - quick rendering
  - easy and quick transformations
  - generation of models via digitization
- **disadvantages**
  - high memory consumption
  - inexact (no surfaces, no occlusion)
  - restricted combination possibilities
  - curves are approximated by straight lines

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## Boundary Representation

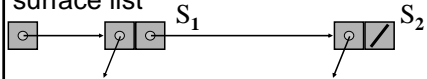


vertex list	edge list	surface list
$V_1: x_1 \ y_1 \ z_1$	$E_1: V_1 \ V_2$	$S_1: E_1 \ E_2 \ E_3$
$V_2: x_2 \ y_2 \ z_2$	$E_2: V_2 \ V_3$	$S_2: E_2 \ E_4 \ E_5 \ E_6$
$V_3: x_3 \ y_3 \ z_3$	$E_3: V_3 \ V_1$	
$V_4: x_4 \ y_4 \ z_4$	$E_4: V_3 \ V_4$	
$V_5: x_5 \ y_5 \ z_5$	$E_5: V_4 \ V_5$	
	$E_6: V_5 \ V_2$	



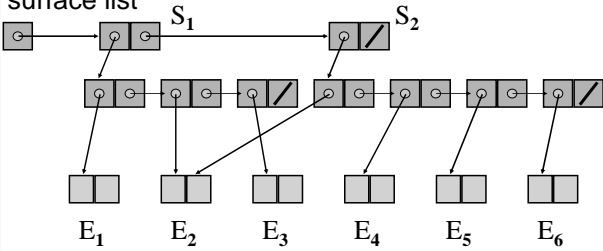
## Lists for B-Reps (1)

surface list



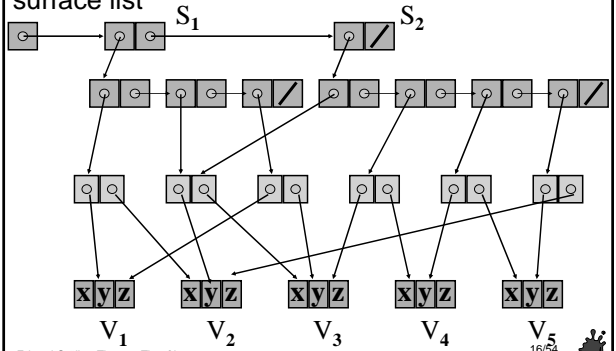
## Lists for B-Reps (2)

surface list



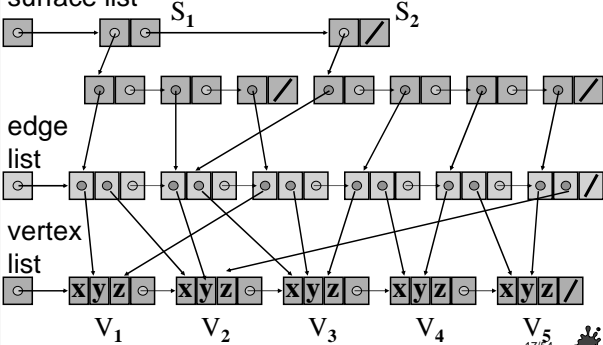
## Lists for B-Reps (3)

surface list



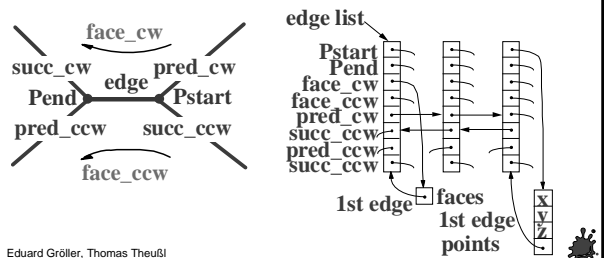
## Lists for B-Reps (4)

surface list



## Winged Edge Data Structure

alternative for normal hierarchical B-Rep.  
here the central element is the edge:



## Operations with B-Reps (1)

- **transformations**

all points are transformed as with wire-frame model, additionally surface equations or normal vectors can be transformed



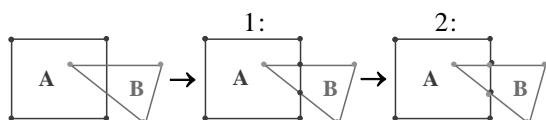
## Operations with B-Reps (2)

- **combinations**

1. split the polygons of object A at the intersections with the polygons of object B
2. split the polygons of object B at ... of A
3. classify all polygons of A as "in B", "outside B" or "on the surface of B"
4. classify all polygons of B in the same way
5. remove the redundant polygons of A and B according to the operator and combine the remaining polygons of A and B



## Combinations of B-Reps, steps 1. and 2.



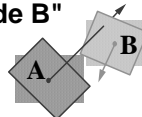
- every polygon has a box enclosure  
⇒ simple test if polygons can intersect
- use only convex polygons and produce only convex polygons as results  
⇒ simple intersection tests



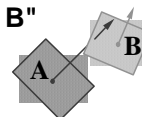
## Combinations of B-Reps, steps 3. and 4.

- a ray is traced in the direction of the normal vector of the polygon to be classified:
  - ray hits no polygon of B ⇒ "outside B"
  - first polygon of B hit from front ⇒ "outside B"
  - first polygon of B hit from back ⇒ "in B"

"outside B"

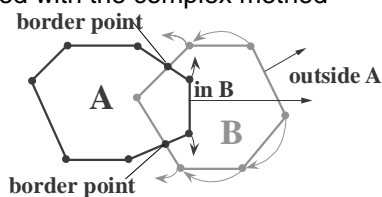


"in B"



## Combinations of B-Reps, steps 3. and 4.

**improvement:** points of A, which lie on the surface of B, are marked as border points during the dividing process (and vice versa)  
⇒ only very few polygons have to be classified with the complex method



## Combinations of B-Reps, step 5.

polygons can be removed according to the tables:

for poly- gons of A	op.	in B	outside B	on B (coplanar)	
				NV equal	different
A or B	yes	no	no	yes	yes
A and B	no	yes	no	yes	yes
A sub B	yes	no	yes	no	no

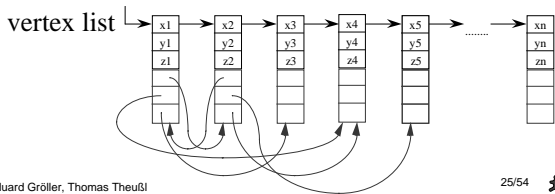
  

for poly- gons of B	op.	in A	outside A	on A (coplanar)	
				NV equal	different
A or B	yes	no	yes	yes	yes
A and B	no	yes	yes	yes	yes
A sub B	no	yes	yes	yes	yes



## Requirements on B-Reps for this Alg.

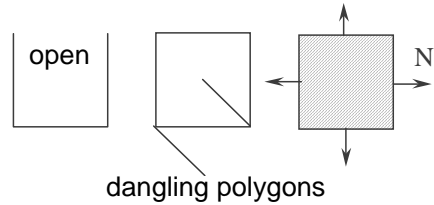
- no open (non-closed) objects
- only convex polygons
- no double points
- additional links in the vertex list between neighbor points with equal classification



## Representation of Solids in a B-Rep

a B-Rep allows also polygon sets which represent no solid object.

therefore: definition of a semantic



## Operations with B-Reps (3)

- **rendering of B-Rep objects**  
hidden surface or hidden line algorithms can be used because the surfaces of the objects are known, so that the visibility can be calculated.

## Properties of B-Reps

- **advantages**
  - general representation
  - generation of models via digitization
  - transformations are easy and fast
- **disadvantages**
  - high memory requirement
  - combinations are relatively costly
  - curved objects must be approximated

## Partitioning of Object Surfaces

necessary to approximate curved surfaces

- surfaces that **can** be parametrized:  
e.g. free form surfaces, quadrics, superquadrics  
partitioning of parameter space,  
one patch for every 2D parameter interval
- surfaces that **cannot** be parametrized:  
e.g. implicit surfaces, "bent" polygons  
⇒ tessellation, subdivision surfaces

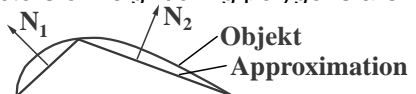
## Tessellation

divide polygons in smaller polygons (triangles) until the approximation is exact enough.

normal vector criterion as termination condition:

$$N_1 \cdot N_2 \geq 1 - \epsilon$$

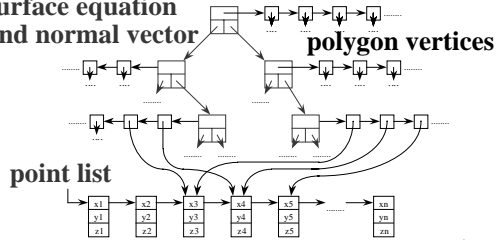
normal vectors of neighboring polygons are similar:



## Binary Space Partitioning Tree

special B-Rep for quick rendering with visibility especially of static scenes

**polygon nodes with surface equation and normal vector**



## Binary Space Partitioning Tree

the base plane of the polygon in a node partitions space in two halves: in front of and behind the polygon.

- **left subtree** of the node: contains only polygons that are **in front of** the basis plane
- **right subtree** of the node: contains only polygons that are **behind** the basis plane

polygons that lie in both halves are divided by the base plane into two parts

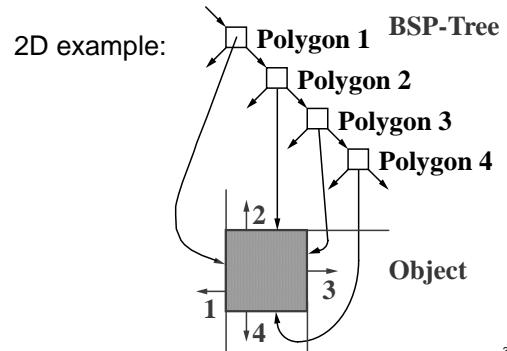
## Generation of BSP Trees

- convex objects: BSP tree is linear list
- else: conversion B-Rep  $\Rightarrow$  BSP tree

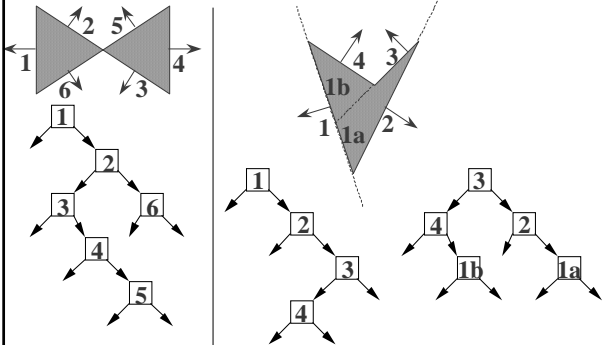
Algorithm:

1. find the polygon whose plane intersects the fewest other polygons and cut these in two
2. divide the polygon list in two sets: in front of that plane / behind that plane
3. the polygon found in 1. is the root of the BSP tree, the left and the right subtrees can be generated recursively (from two "halves")

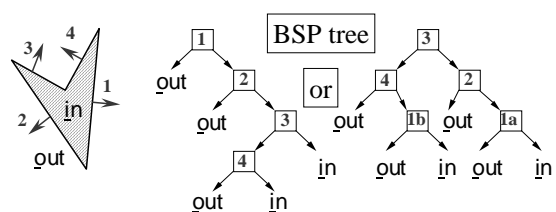
## BSP Example



## More BSP Examples



## BSP Trees as Solids



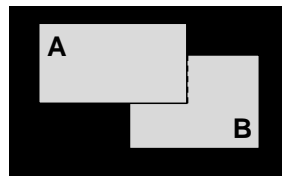
left empty trees represent outside space, right empty trees represent inside volumes

## Operations with BSP Trees (1)

- **transformations**  
points, plane equation and normal vector have to be transformed
- **combinations**
  - perform combination with B-Rep, then generate BSP tree
  - combine BSP trees directly (faster)



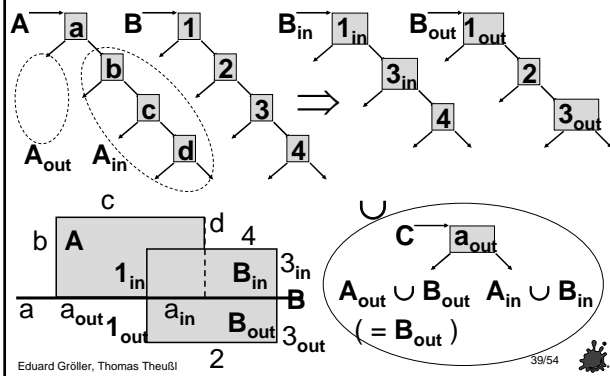
## Combination of BSP Trees



the structure of one tree has to act as structure for the result  
 $\Rightarrow$  one tree has to be included into the other



## Combination of BSP Trees: $\cup$



## BSP Algorithm for $A \text{ op } B = C$ :

- A or B homogeneous (full or empty)  
 $\Rightarrow$  simple rules
- else:
  1. divide root polygon a of A at object B in  $a_{in}$ ,  $a_{out}$
  2. root node c of C: if op="and" then  $c:=a_{in}$  else  $c:=a_{out}$  (with its plane)
  3. divide B at plane of a in  $B_{in}$ ,  $B_{out}$
  4. recursive evaluation of the subtrees:  
 $C_{left}=A_{out} \text{ op } B_{out}$      $C_{right}=A_{in} \text{ op } B_{in}$

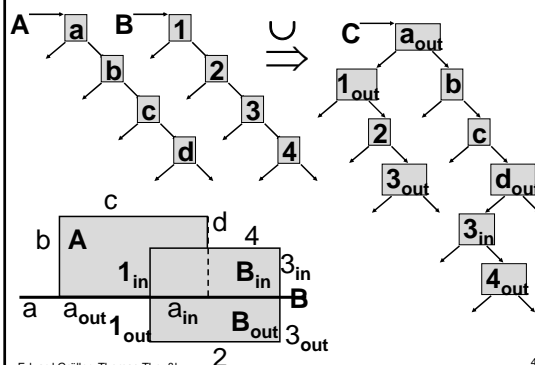


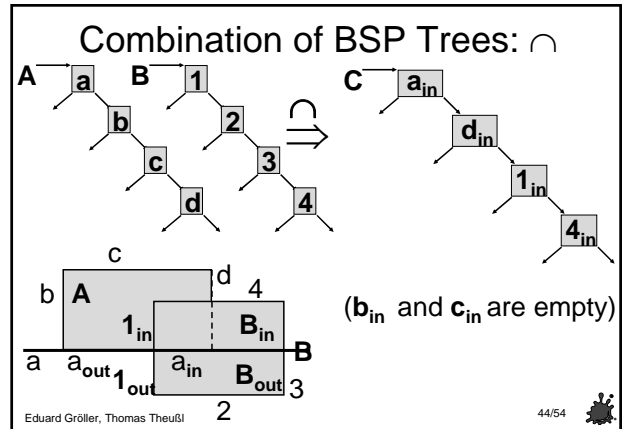
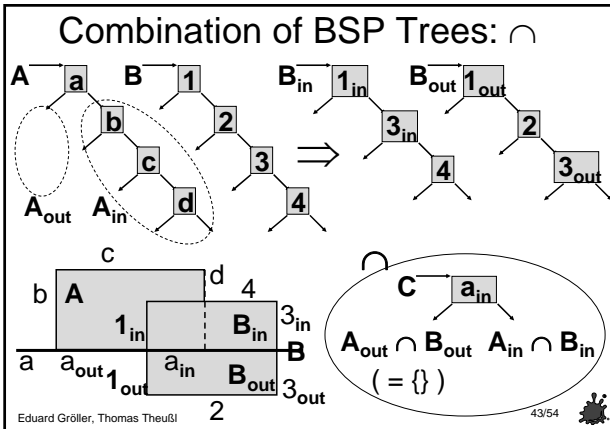
## Simple BSP Node Combination Rules

op	A	B	A op B
or	inhom.	full	full
	inhom.	empty	A
and	full	inhom.	full
	empty	inhom.	B
sub	inhom.	full	A
	inhom.	empty	empty
sub	full	inhom.	B
	empty	inhom.	empty
sub	inhom.	full	empty
	inhom.	empty	A
sub	full	inhom.	-B
	empty	inhom.	empty



## Combination of BSP Trees: $\cup$





### Operations with BSP Trees (3)

- rendering of BSP objects

BSP trees are very good for fast rendering

**Painter's Algorithm:**

```

IF eye is in front of a (in A+)
THEN BEGIN draw all polygons of A-
draw a;
draw all polygons of A+ END
ELSE BEGIN draw all polygons of A+
(draw a);
draw all polygons of A- END;

```

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### BSP Tree Properties

- advantages
  - fast rendering
  - fast transformation
  - combinations faster than for B-Reps
  - general representation
  - generation of models via digitization

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### BSP Tree Properties

- disadvantages
  - curved objects must be approximated
  - only convex polygons
  - high memory cost

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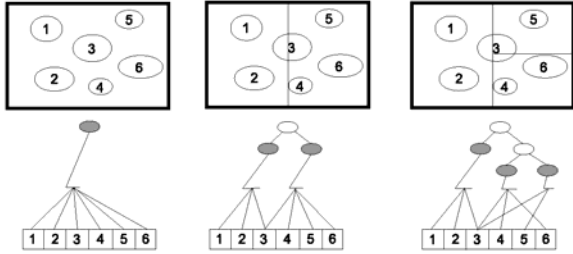
### k-D Tree

- Special case of BSP Tree
- Only axes-aligned partitioning planes => specified by one value
- Partitioning direction specified either implicitly (pre-defined order) or explicitly
- 1-D Tree  $\Leftrightarrow$  binary tree

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## k-D Tree Example: 2-D Tree



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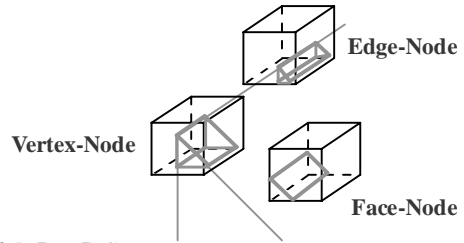
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## Extended Octrees

additional node types:

- **face nodes** contain a surface
- **edge nodes** contain an edge
- **vertex nodes** contain a corner point



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## Generation of Extended Octrees

1. generate B-Rep
2. divide point and surface list at the subdivision planes into 8 sets
3. for each octant:
  - point and surface lists empty  $\Rightarrow$  full or empty
  - only one vertex  $\Rightarrow$  vertex node
  - only one surface  $\Rightarrow$  face node
  - only two surfaces  $\Rightarrow$  edge node
  - else: subdivide recursively

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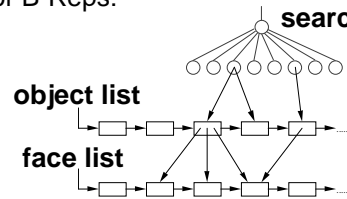
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## Octree as Spatial Directory

Octree as search structure for objects in other representations

e.g. for B-Reps:



octree of low depth is sufficient

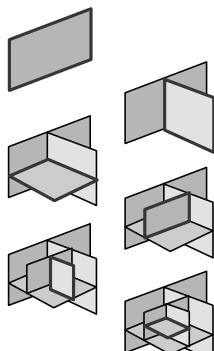
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## Bintree

- 3-D Tree
- subdivision order xyzxyz...
- choose separation plane for optimized (irregular) subdivision
- fewer nodes than octree



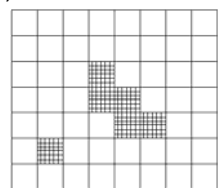
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## Grid

- regular subdivision
- directly addressable cells
- simple neighbour finding  $O(1)$ , e.g., for ray traversal
- problem:
  - too few/many cells
  - $\Rightarrow$  **Hierarchical Grid**



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