

# Algorithmen für die Echtzeitgrafik

## Algorithmen für die Echtzeitgrafik

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LBI Virtual Archeology



# Animation

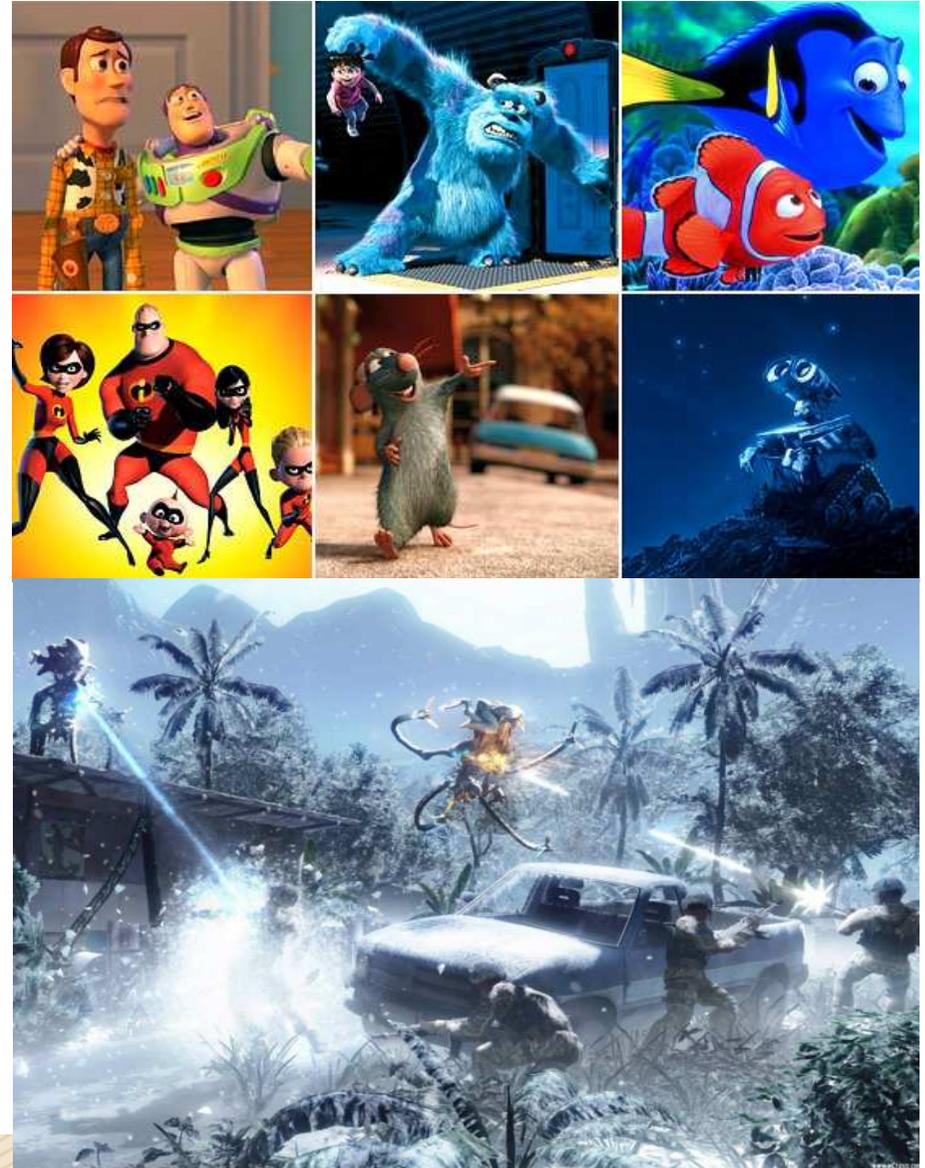


# Overview

- Animation principles
- Keyframing and interpolation
  - Artist specifies almost everything, the computer just makes it smooth
- Kinematics
  - Joints, articulated figures
- Data driven
  - Motion capture
- Procedural animation
  - Rules and simulations automatically produce the animation
  - Physics Simulation

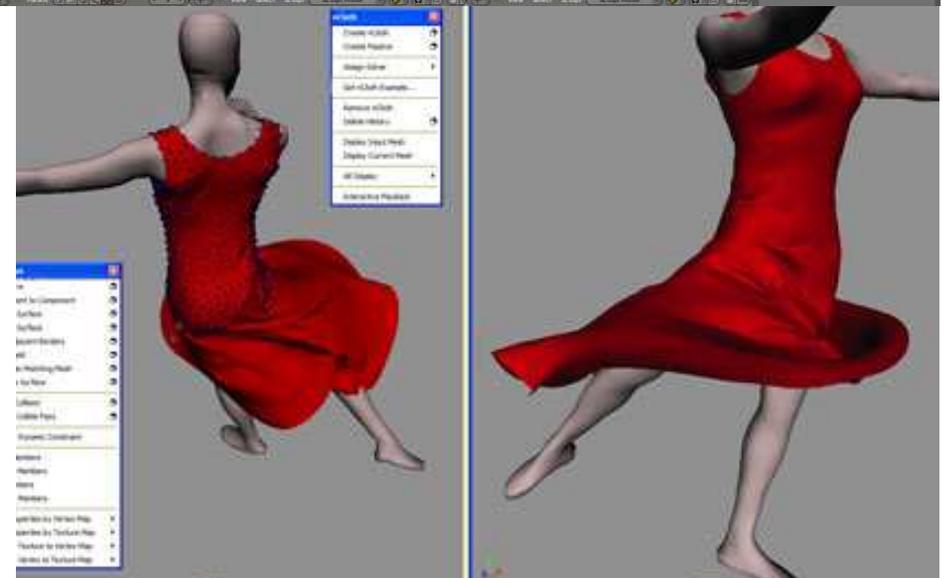
# Applications

- Special Effects
  - Movies, TV
- Video Games
- Virtual Reality
- Simulation, Training
- Medical
- Robotics, Animatronics
- Visualization
- Communication



# Animation Tools

- Maya
- 3D Studio
- Lightwave
- Filmbox
- Blender
- ...

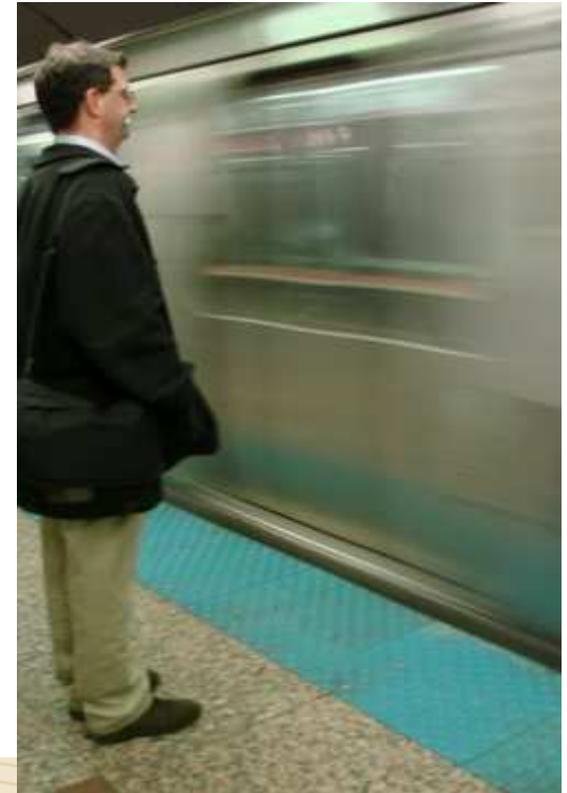


# Animation Basics

- Persistence of vision (human eye)
  - Afterimage for  $1/25$  sec (compensate blinking)
  - A sequence of images shown fast enough is hard to distinguish from true motion
    - What is fast enough?
    - Foveal vs. Peripheral vision
- Frame rate (fps = frames per second)
  - Film: 24
    - Often 48, each frame twice, to reduce flicker
  - TV: ~30 for NTSC, 25, for PAL
    - Interlaced - double the speed to reduce flicker
  - Computers: 60Hz or more

# Motion Blur

- Light persists in our vision for a while
  - Fast moving objects leave a blurred streak
- Real cameras leave shutter open for a while
  - Moving objects blurred
    - Position at start of shutter time
    - Till position at end
- Without motion blur
  - Strobbing effect
    - Trail of clear staggered images

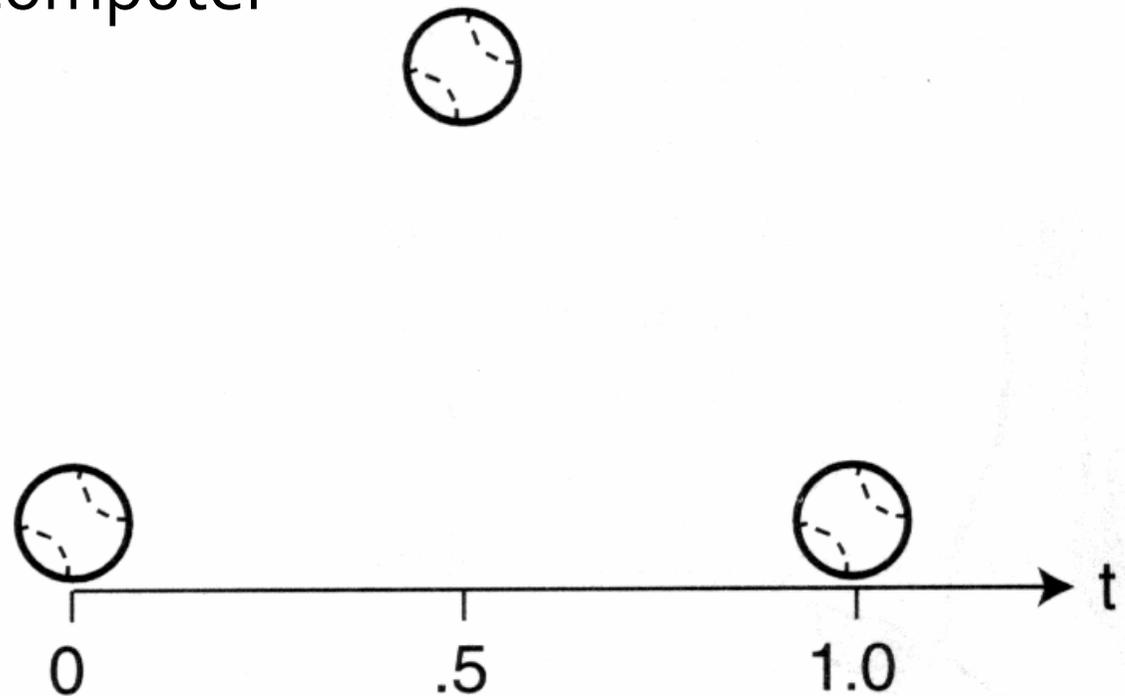


# Computer Animation

- Setting various animation parameters
  - Positions, angles, sizes, ... in each frame
- Straight-ahead
  - Set all variables in frame 0, then frame 1, frame 2, ...
- Pose-to-pose:
  - Set variables at keyframes, let the computer smoothly interpolate values in between
- Can mix the methods:
  - Keyframe some variables (maybe at different frames), do others straight-ahead

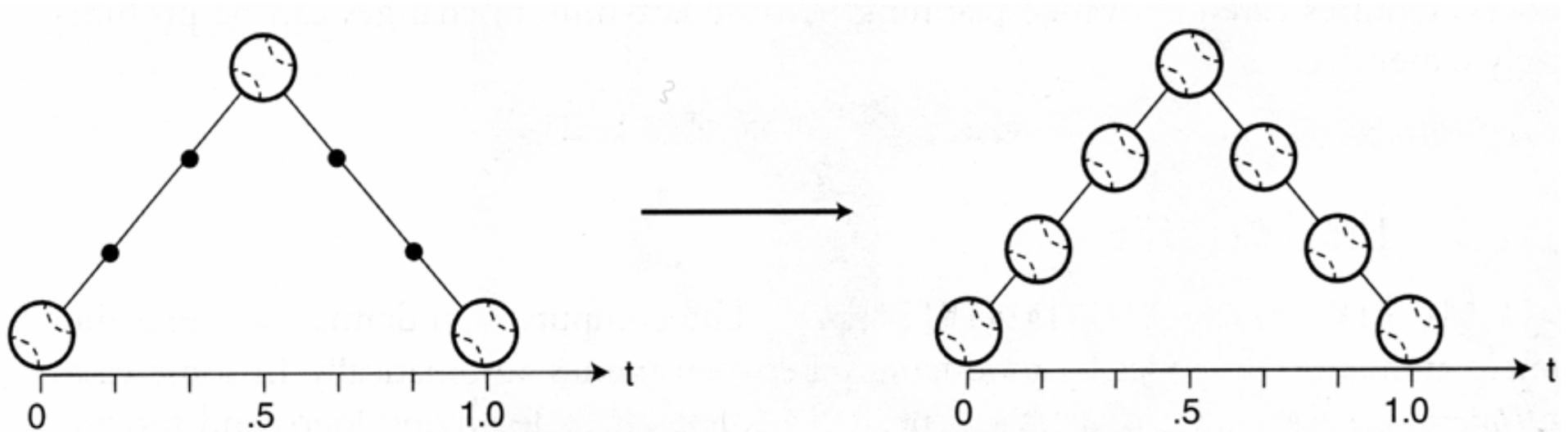
# Keyframing

- Traditional animation technique
- Dependent on artist to generate 'key' frames
- Additional, 'inbetween' frames are drawn automatically by computer



# Linear Interpolation

- Simple
- Constant velocity at edges
- Discontinuous velocity at corners
  - Can be unnatural



# Linear Interpolation

- Given points  $P_0$  and  $P_1$ , define curve  $L(t)$ :

$$L(t) = (1-t)P_0 + tP_1 \quad t \text{ in } [0,1]$$

- Weighted average of endpoints
- “Curve” is linear segment

# Linear Interpolation: $N$ Points

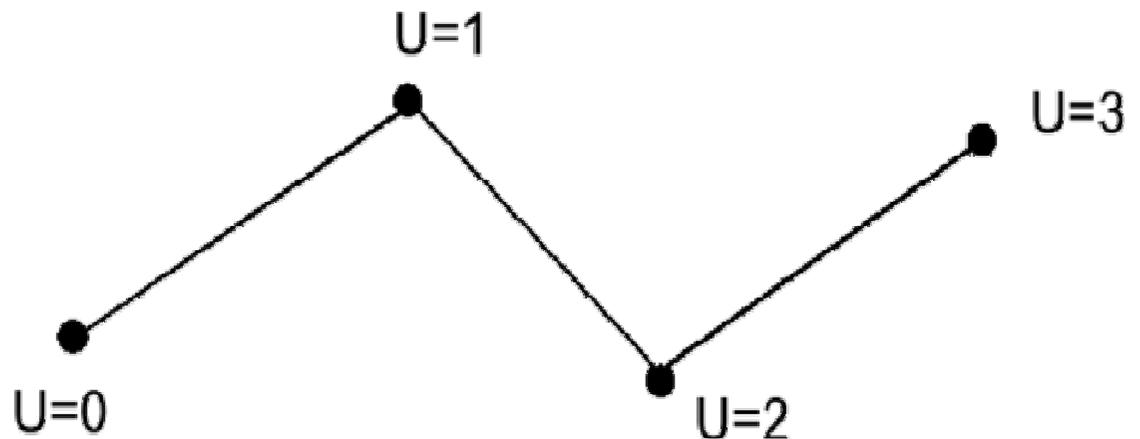
- Given  $P_0 \dots P_N$  define segment:

$$L_i(s) = (1-s) P_i + s P_{i+1} \quad s \text{ in } [0,1]$$

- Then define piecewise-linear curve:

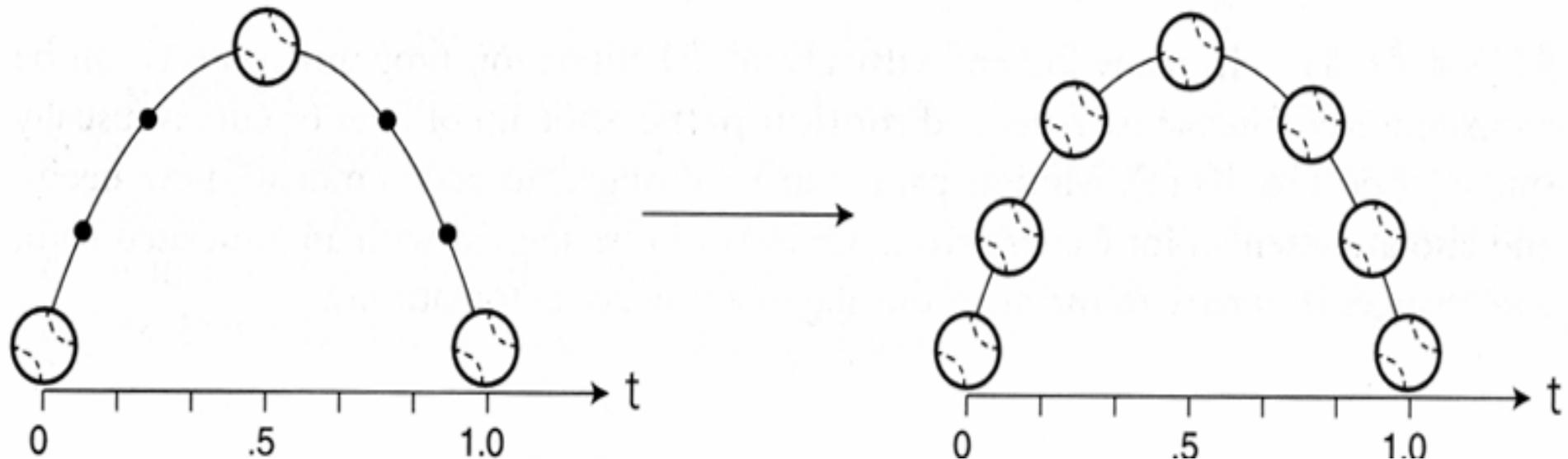
$$L(u) = L_i(s)$$

- Use fractional value of  $u$  for piecewise curves
- Sharp discontinuities  $C^0$  but not  $C^1$



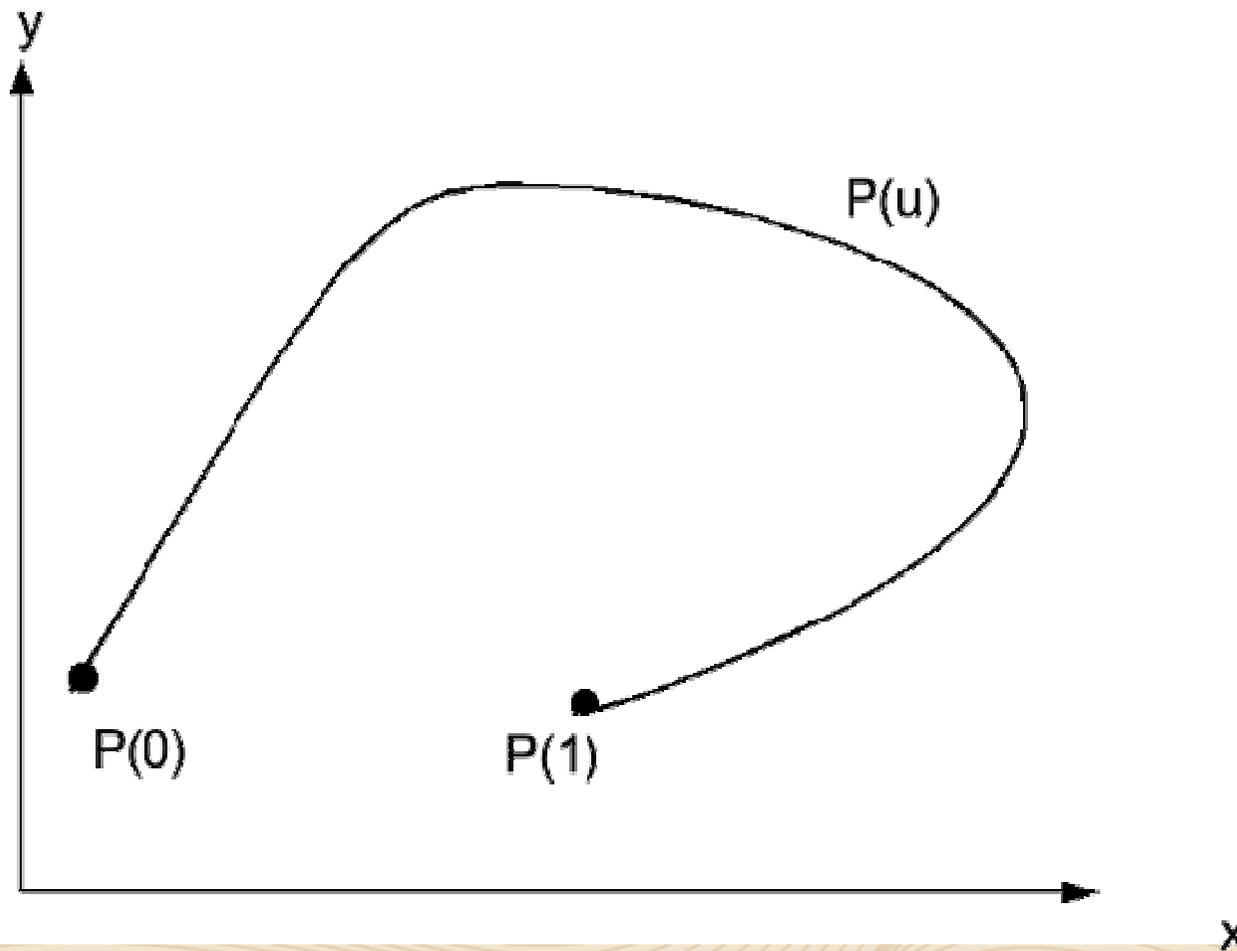
# Nonlinear Interpolation

- Often Catmull-Rom-Splines
- Removes discontinuities at corners
  - $C_0, C_1$
  - $C_2$  often unnecessary (acceleration often changes discontinuous in nature)



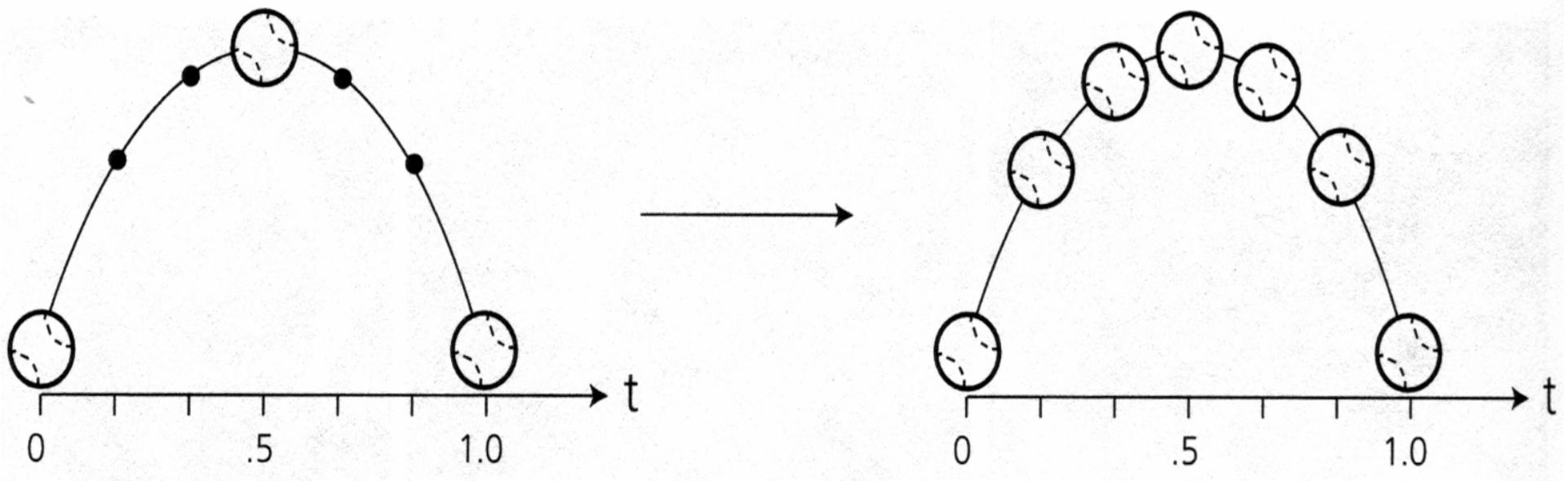
# Parametric Curves

- $P(u) = (x(u), y(u), z(u)) \quad 0 \leq u \leq 1$



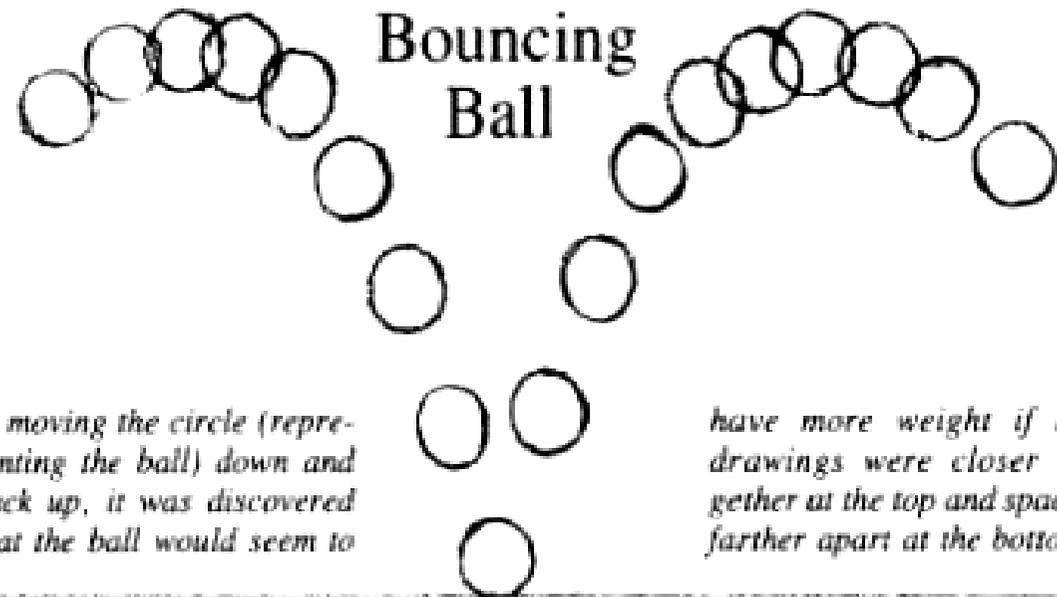
# Easing

- Velocity is changed near a keyframe
  - Ball should slow down at apex

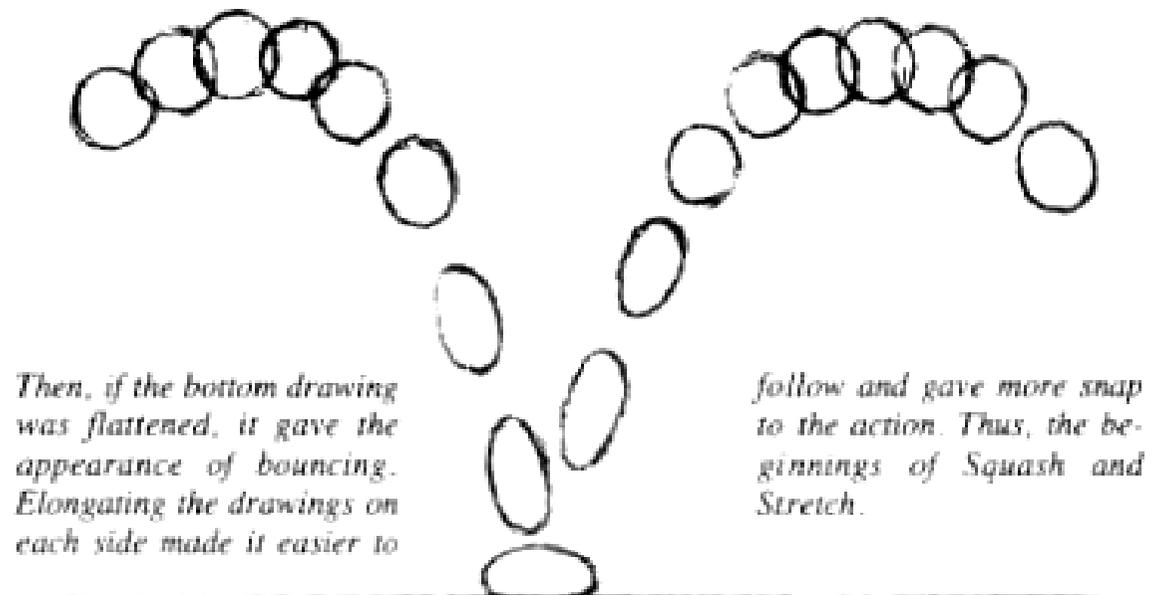


# Style or Accuracy

- More weight



- Squash and stretch



# More Squash and Stretch



# Traditional Motivation

- A keyframe should contain all information to understand a situation



*The famous half-filled flour sack, guide to maintaining volume in any animatable shape, and proof that attitudes can be achieved with the simplest of shapes.*



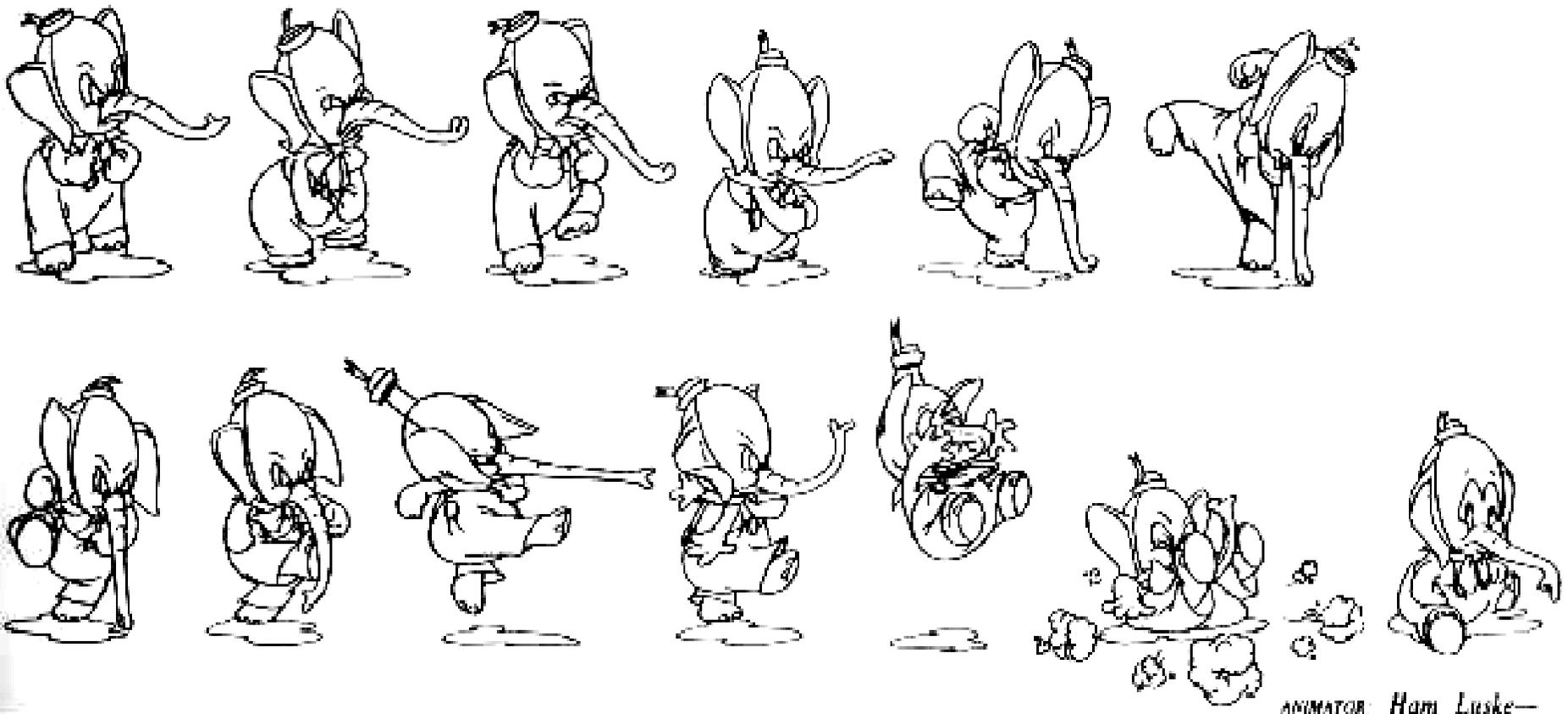
# Anticipation and Staging

- Don't surprise the audience
- Direct their attention to what's important



# Follow Through

- Audience likes to see resolution of action
- Discontinuities are unsettling



ANIMATOR: Ham Luske—

# Secondary Motion

- Characters should exist in a real environment
- Extra movements should not detract



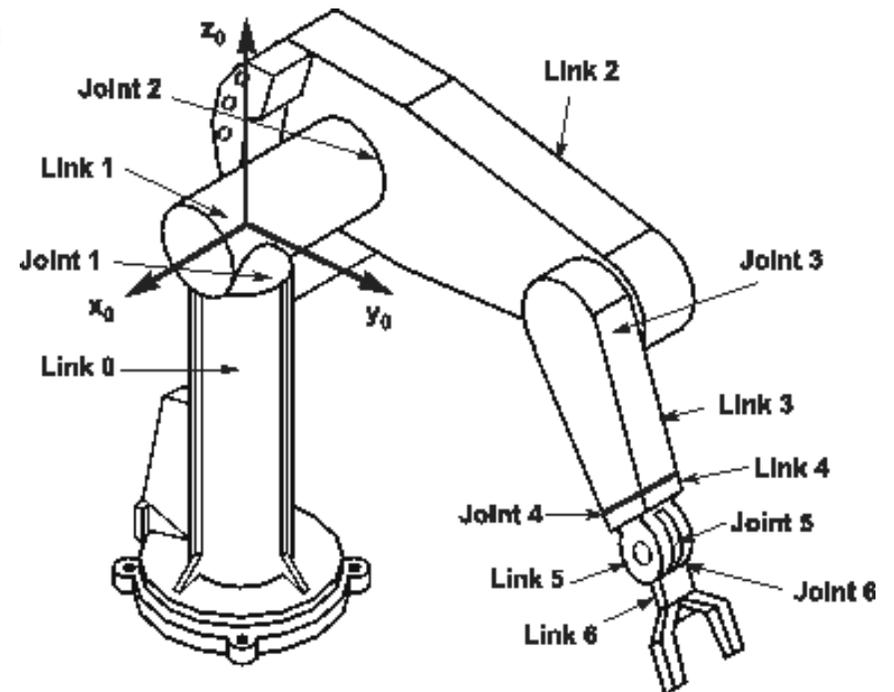
# Animation

## Kinematics



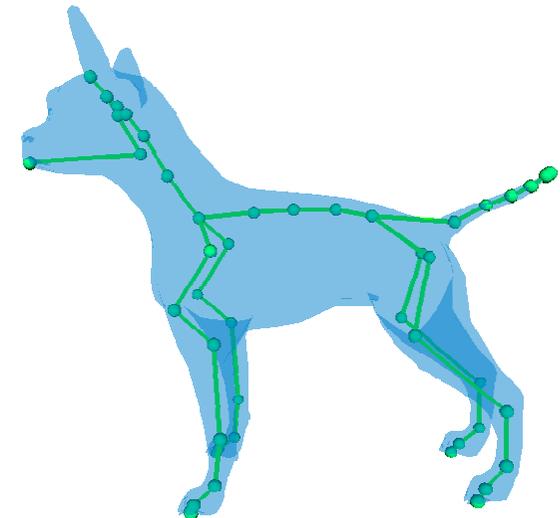
# Kinematics

- The study of how things move
  - Without considering the causes
- Describing the motion of articulated rigid figures
  - Things made up of rigid “links” attached to each other at movable joints (articulation)
- Many mathematical approaches

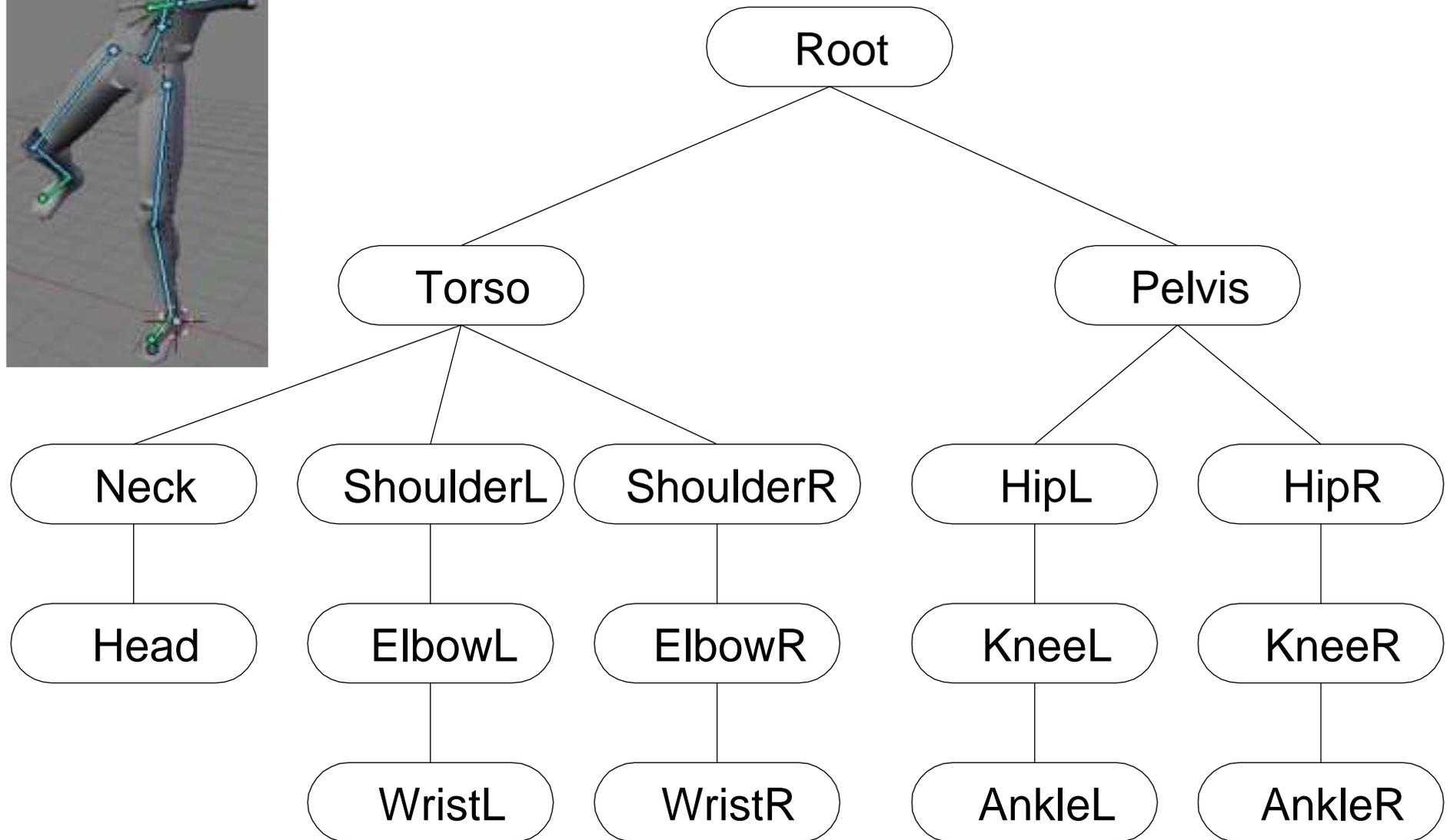
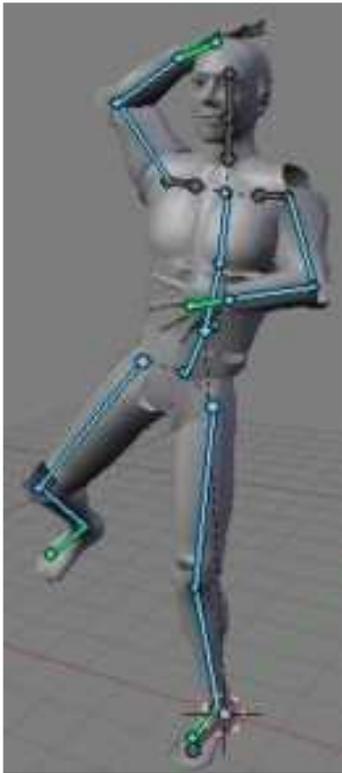


# Skeletons

- Skeleton
  - Pose-able framework of joints
  - Arranged in a tree structure.
  - Invisible armature
- Joint (Bone)
  - Allows relative movement within the skeleton.
  - Essentially  $4 \times 4$  matrix transformations
  - Rotational, translational, ...
- Rigging
  - Building the skeleton

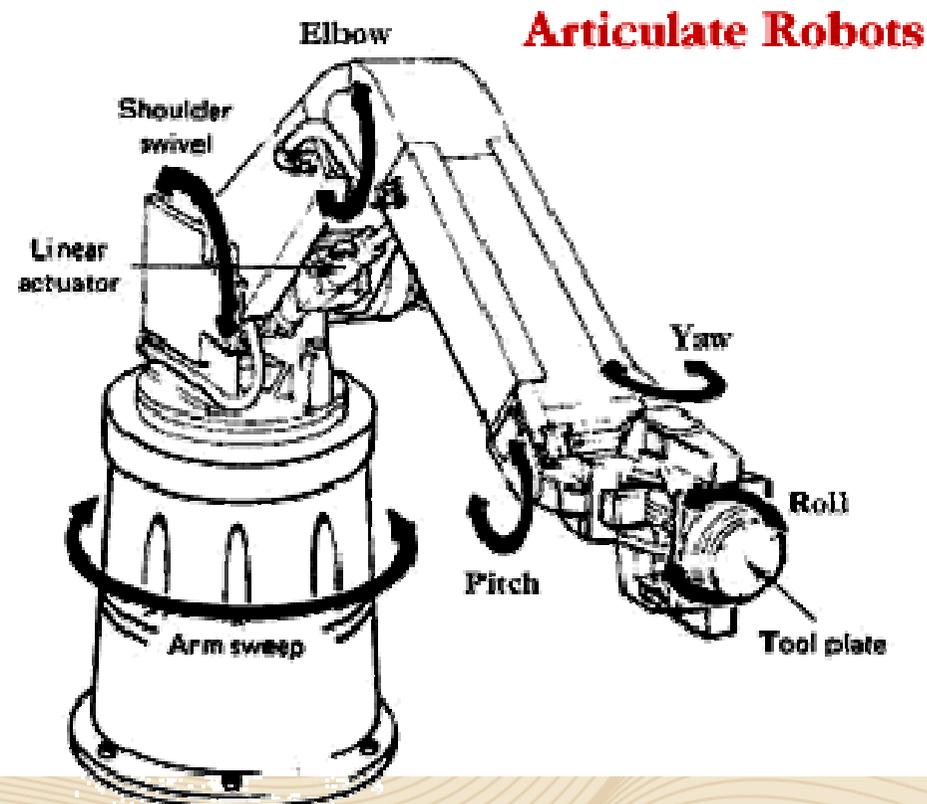


# Example Joint Hierarchy



# Degree of Freedom (DOF)

- A variable  $\varphi$  describing a particular axis or dimension of movement within a joint
- Joints typically have around 1-6 DOFs ( $\varphi_1 \dots \varphi_N$ )

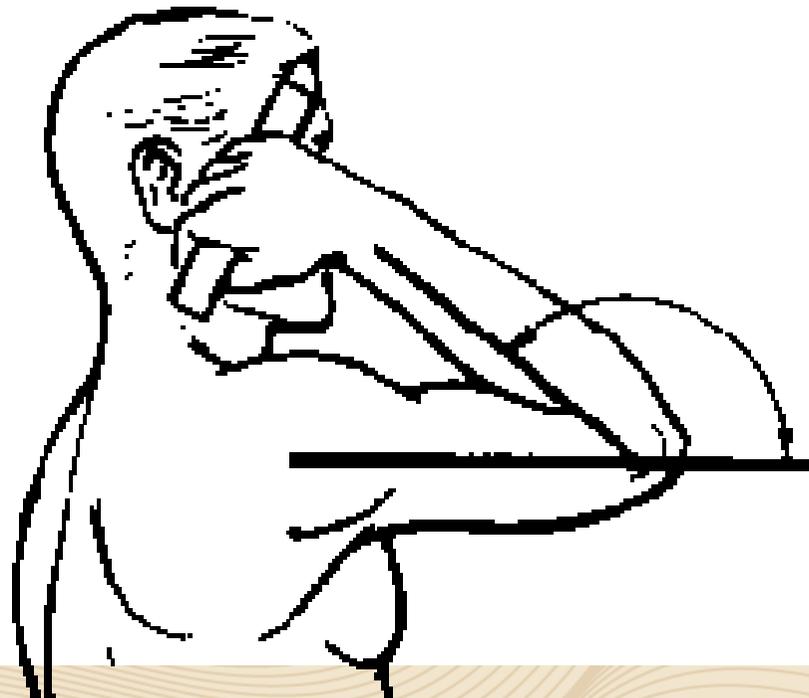


# Degree of Freedom (DOF)

- A variable  $\varphi$  describing a particular axis or dimension of movement within a joint
- Joints typically have around 1-6 DOFs ( $\varphi_1 \dots \varphi_N$ )
- Changing DOF values over time results in animation of skeleton
- Example
  - Free rigid body has 6 DOFs
    - 3 for position
    - 3 for rotation

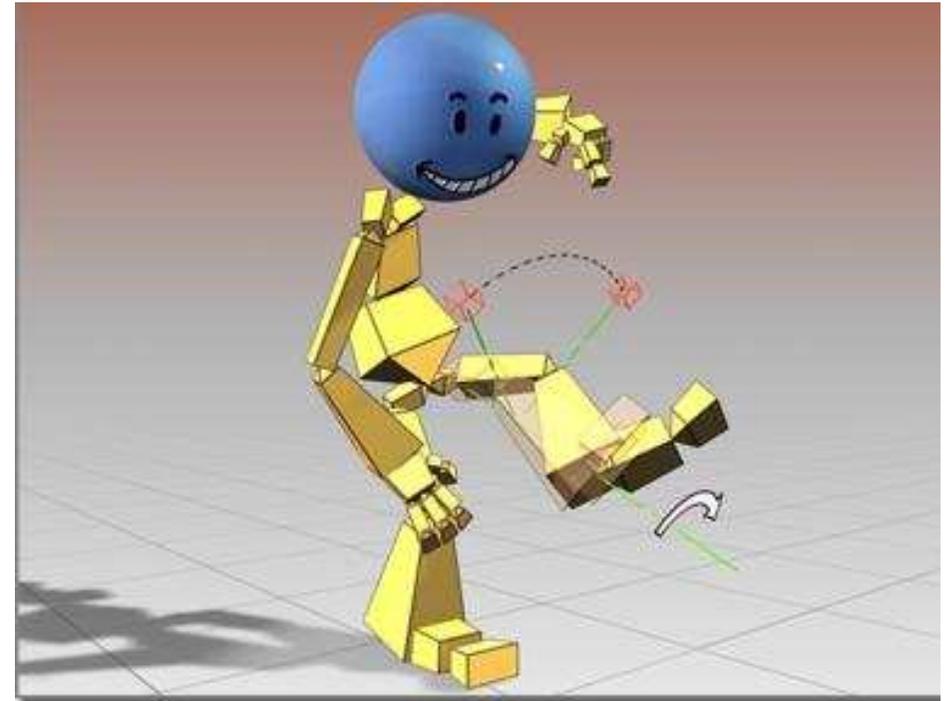
# DOF Limits

- Limit DOF to some range
  - E.x. limit elbow from  $0^\circ$  to  $150^\circ$
- Usually, in a realistic character, all DOFs will be limited except the ones controlling the root



# Joints

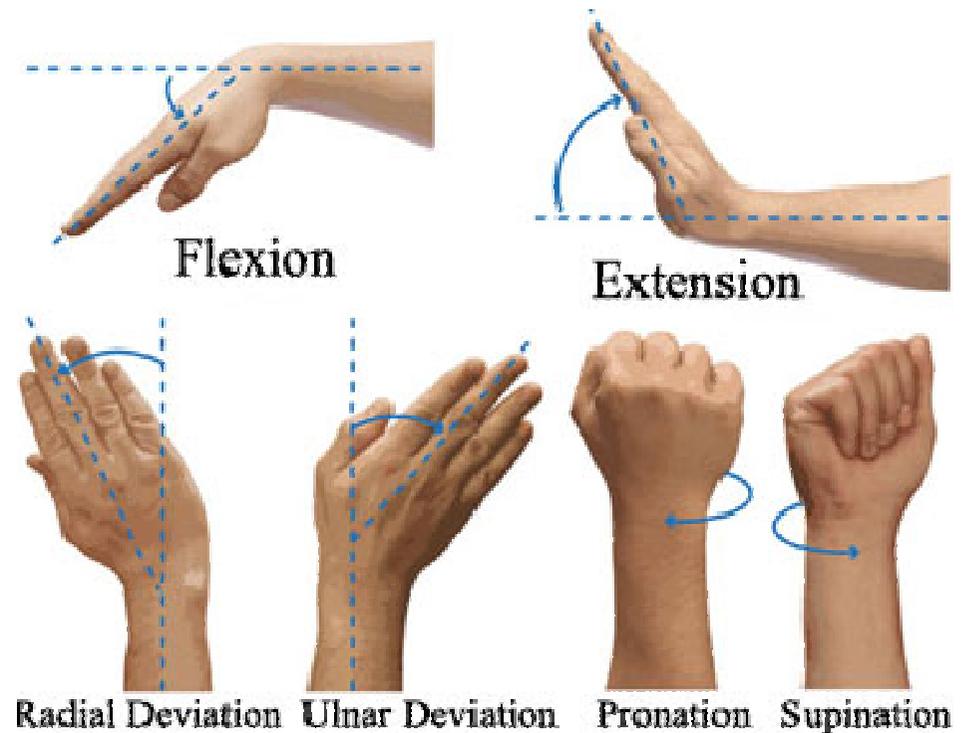
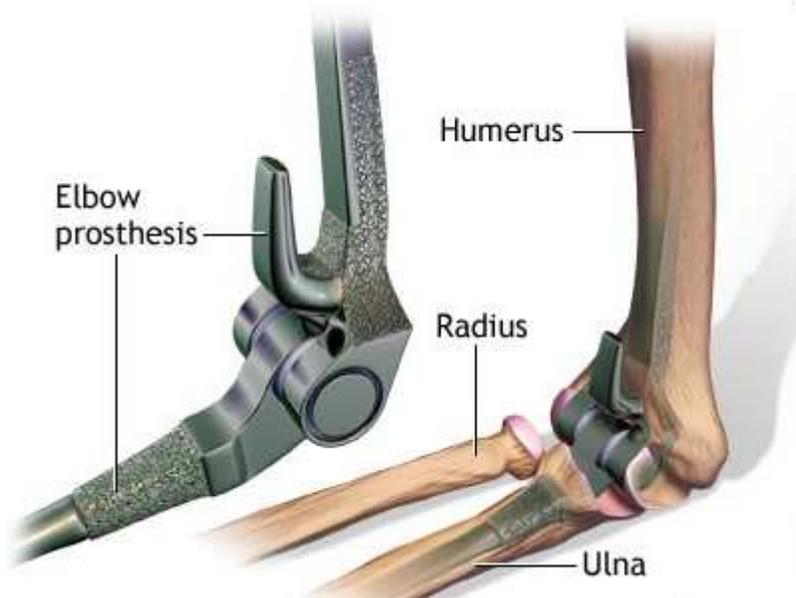
- Core joint data
  - DOFs ( $n$  floats)
  - Local matrix:  $L$
  - World matrix:  $W$



- Additional Data
  - DOF limits (min & max value per DOF)
  - Type-specific data (rotation/translation axes, constants...)
  - Tree data (pointers to children, siblings, parent...)

# Reality Check

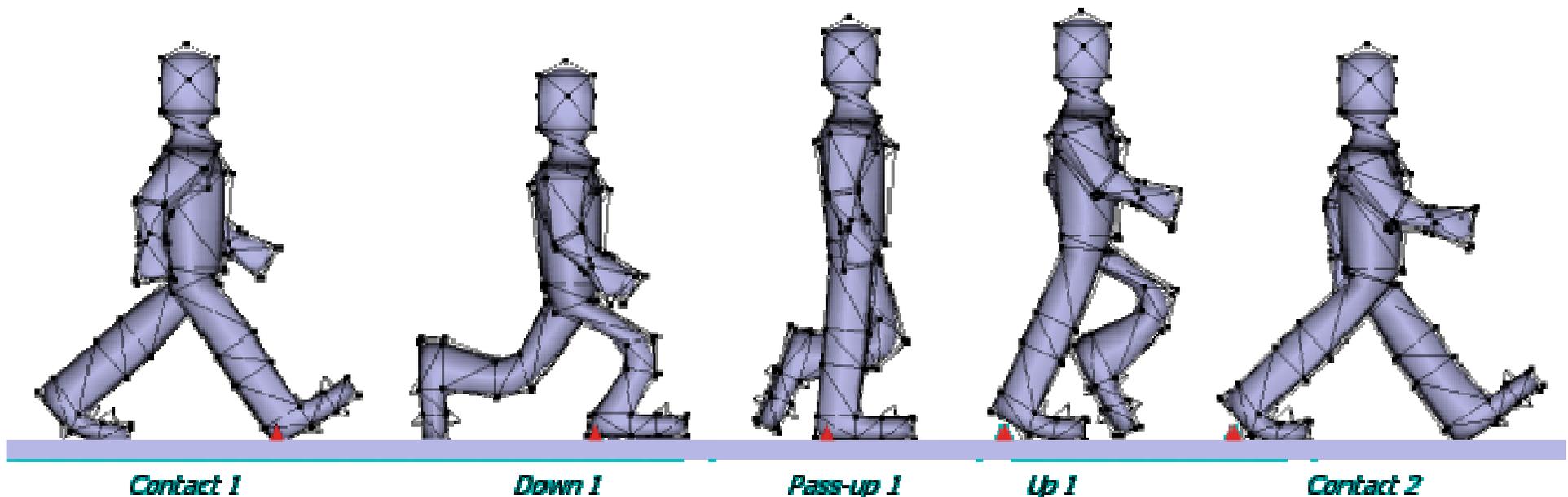
- Elbow has 1 DOF: the angle the forearm makes with the upper arm (rotation in plane)
- Wrist has 3 DOF
- ...



# Pose

- Setting of all DOFs (specify in Blender, Maya)

$$\Phi = (\varphi_1 \varphi_2 \dots \varphi_N)$$



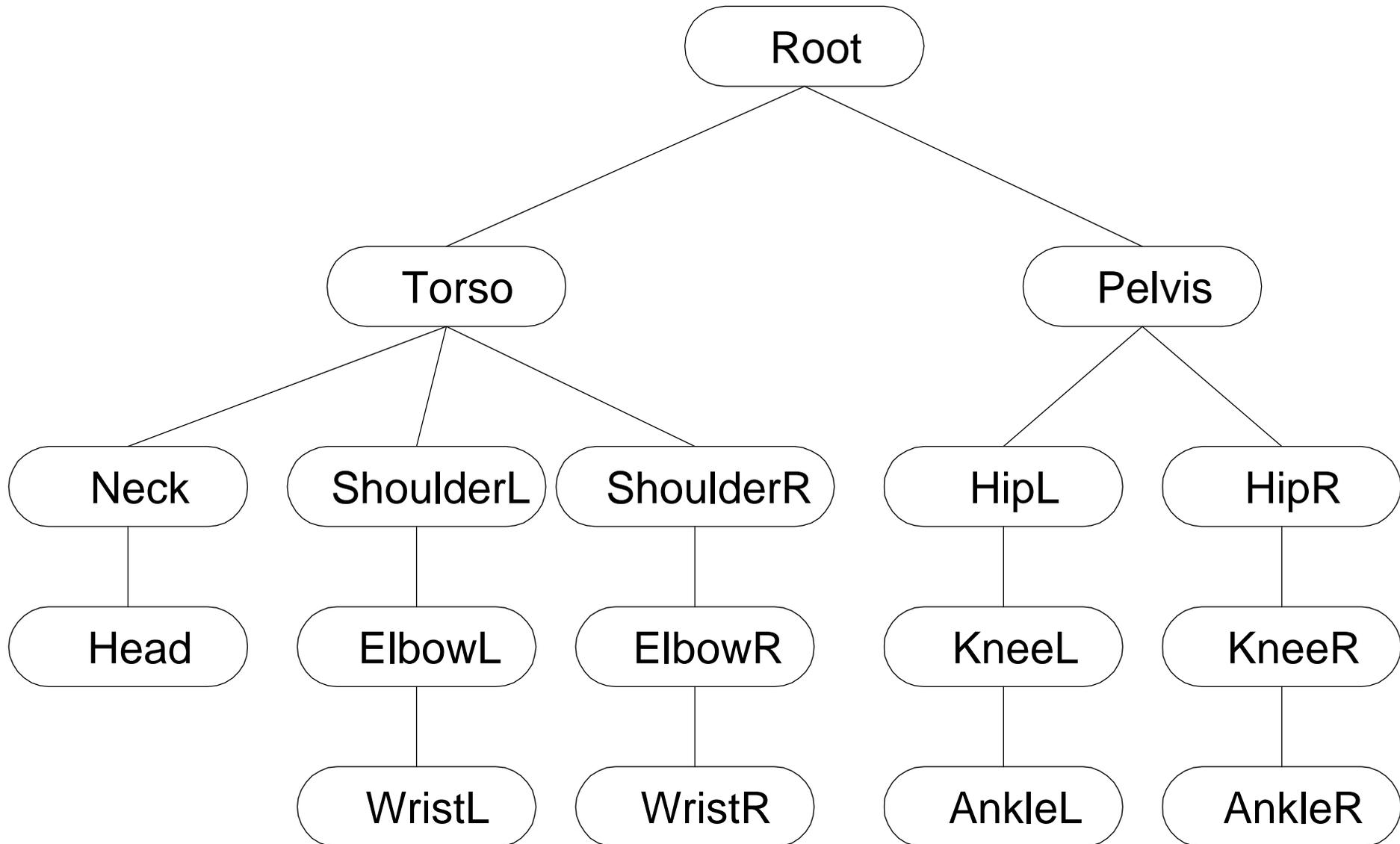
# Pose



*The famous half-filled flour sack, guide to maintaining volume in any animatable shape, and proof that attitudes can be achieved with the simplest of shapes.*



# Forward Kinematics



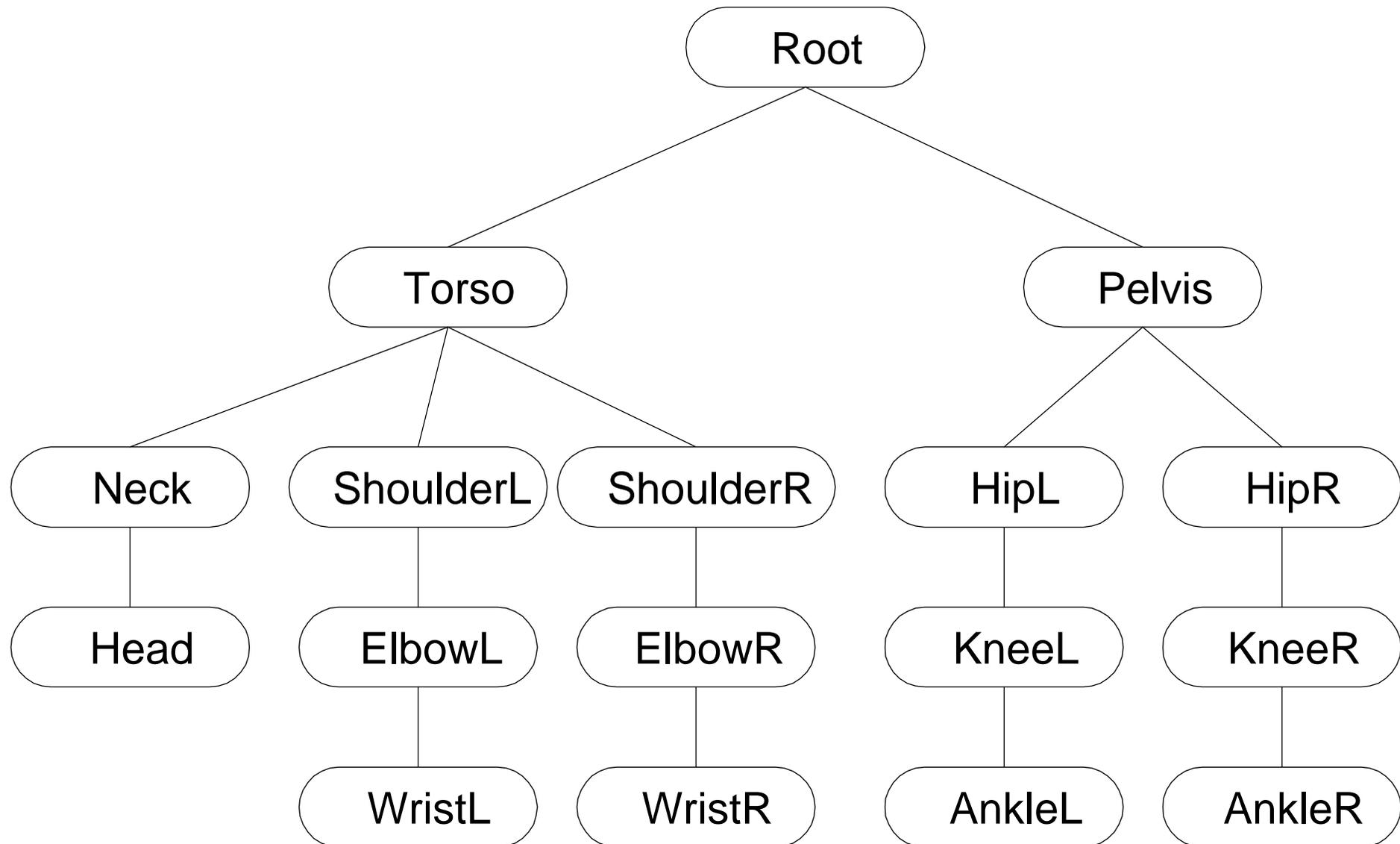
# Forward Kinematics

- Top down recursive tree traversal
- Each joint computes local matrix  $\mathbf{L}$ 
  - Based on the values of DOFs ( $\varphi_1 \varphi_2 \dots \varphi_N$ )
  - And joint type (rotational, translational, ...)
  - Local matrix  $\mathbf{L} = \mathbf{L}_{\text{joint}}(\varphi_1, \varphi_2, \dots, \varphi_N)$
- Each joint computes world matrix  $\mathbf{W}$ 
  - Multiply  $\mathbf{L}$  with world matrix of parent joint
  - World matrix  $\mathbf{W} = \mathbf{W}_{\text{parent}} \cdot \mathbf{L}$

# Pros and Cons

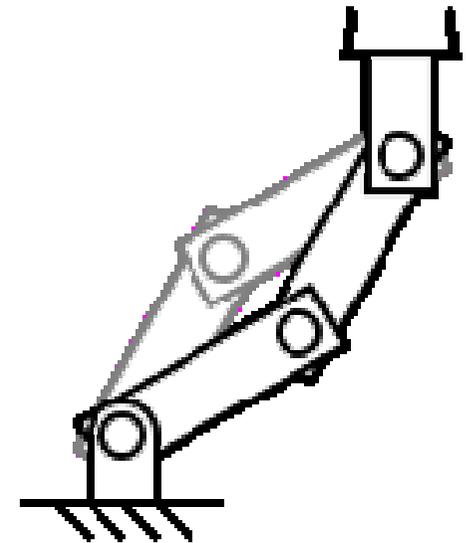
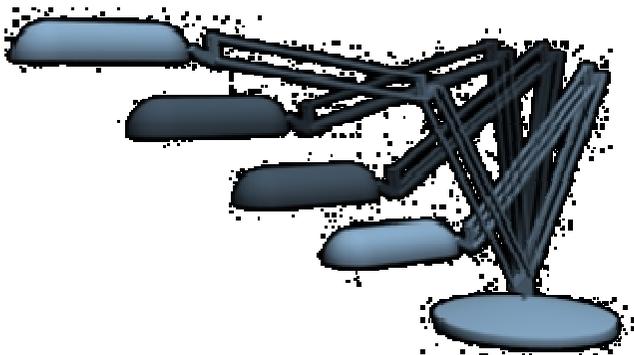
- A simple layered approach
  - Get the root link moving first (e.g. the pelvis)
  - Fix the pose outward, link by link (the back and the legs next, then the head, the arms, the hands, the fingers, ...)
- Great for certain types of motion
  - General acting, moving in free space, ...
- Problems when interacting with other objects
  - Fingers grabbing a doorknob
  - Feet stay on the ground

# Inverse Kinematics (IK)

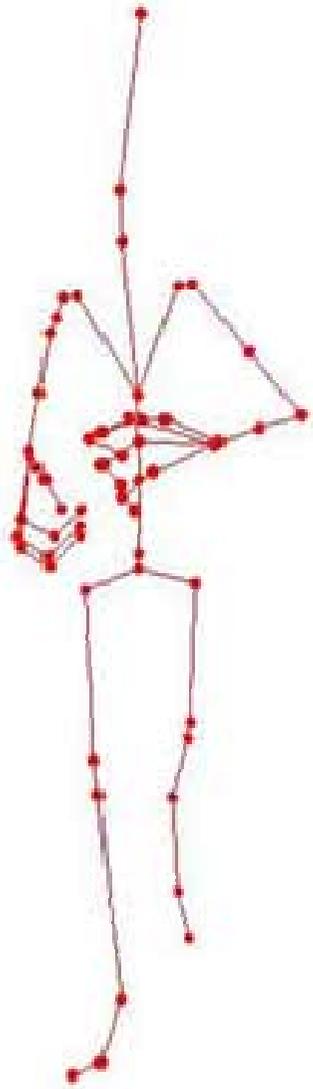


# Inverse Kinematics (IK)

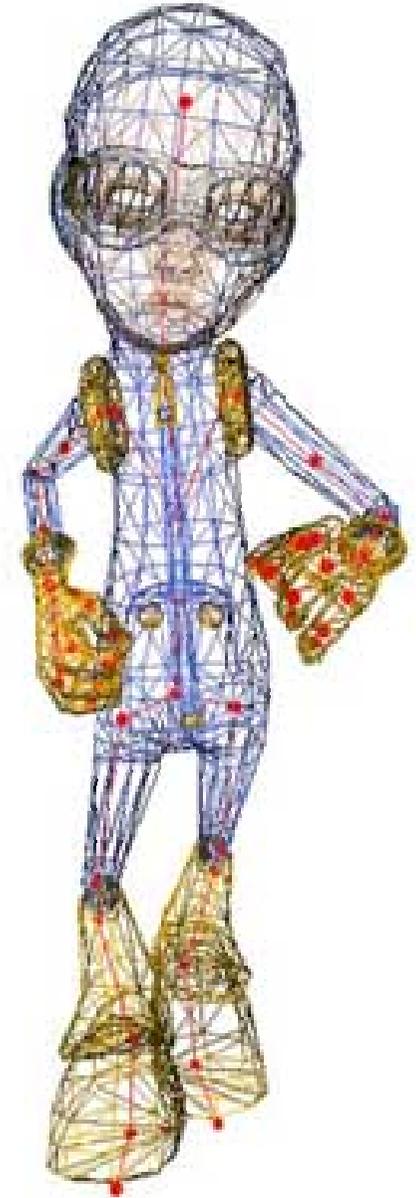
- Given the desired displacement of a point
  - Hand on doorknob, foot on the ground, ...
- How to compute the necessary joint motions?
  - Solving joint chain
  - Solving (linear) equation system



# Skinning

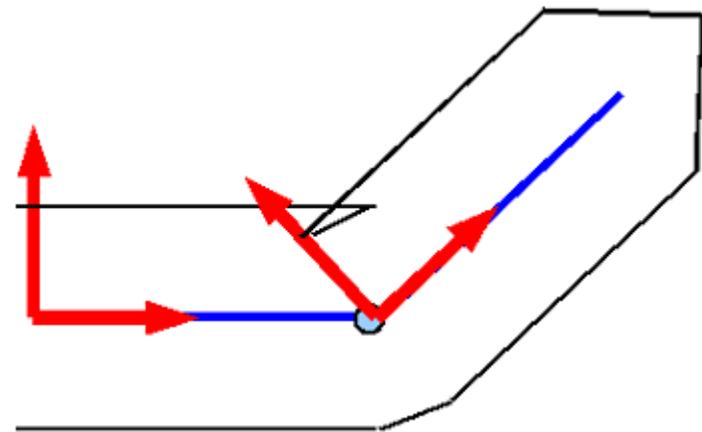
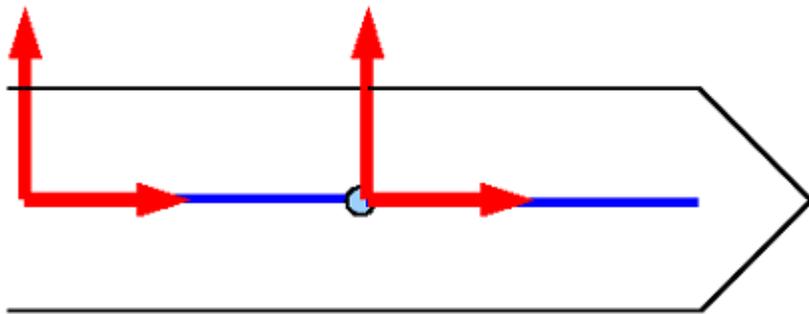


- Till now only animated skeleton
- Rigid geometry (at joints) usually looks very strange (maybe OK for robots)
- Need to wrap skin (a mesh), flesh, clothes ... around the animated skeleton
- Continuous mesh deformations



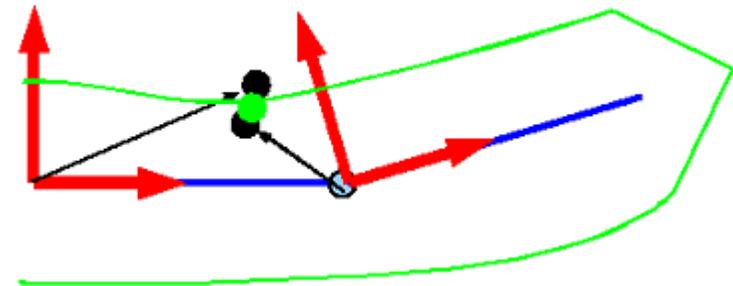
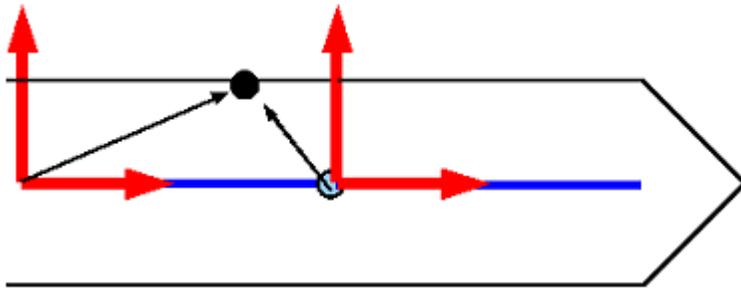
# Why trivial methods do not work

- Attach each vertex to the closest solid
  - Discontinuities
  - Self-intersections



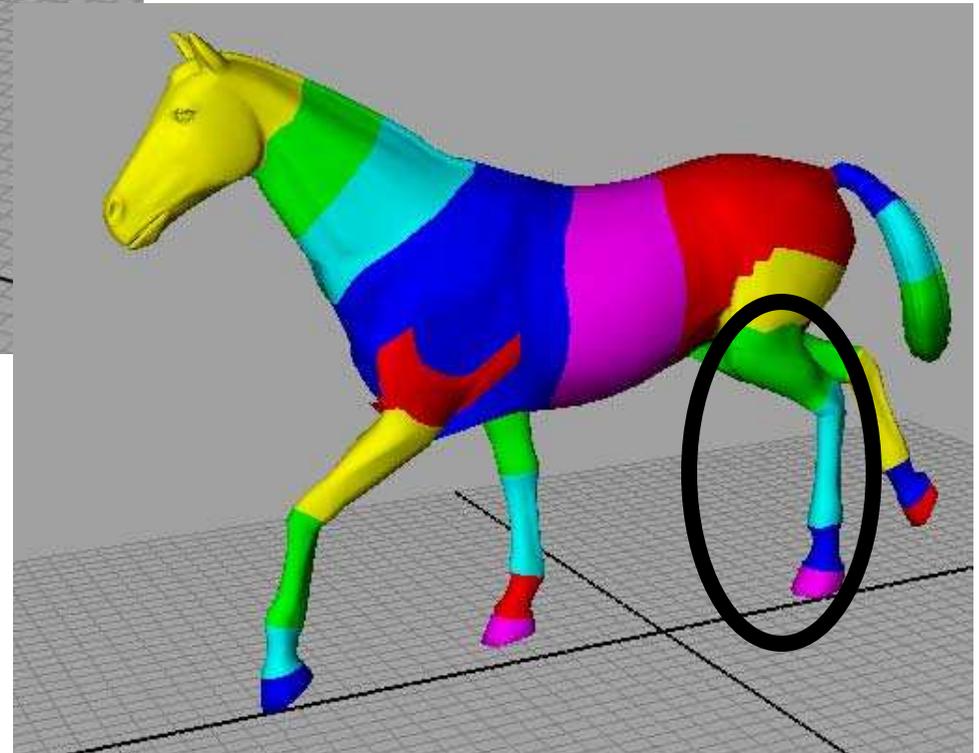
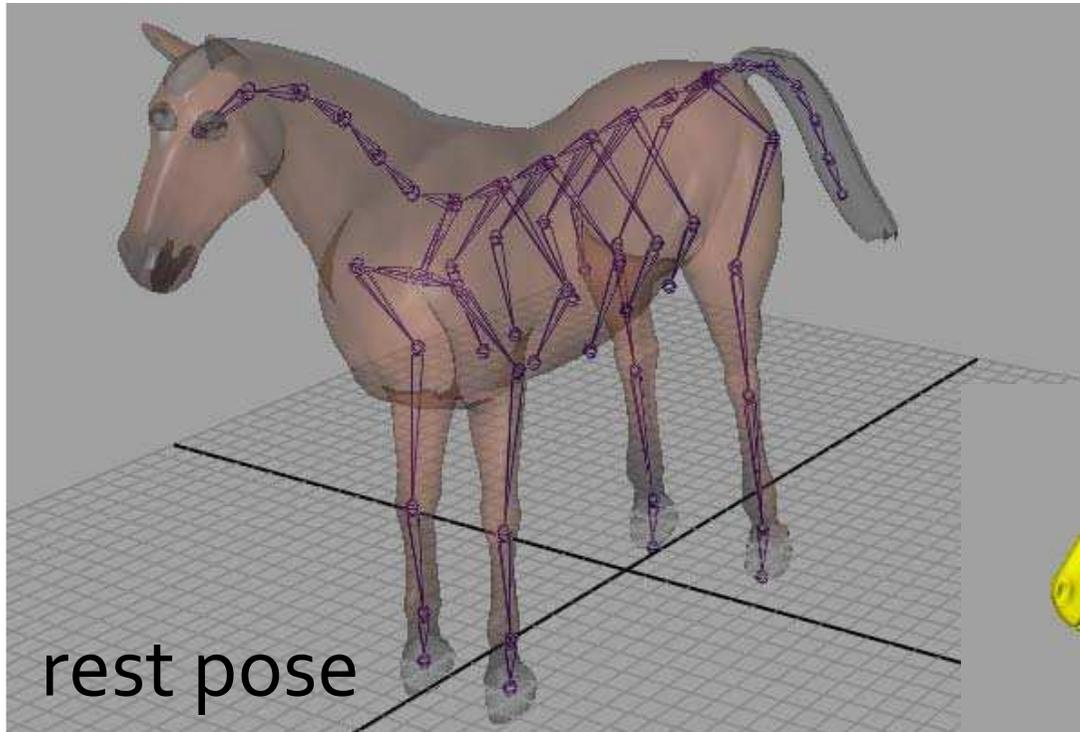
# Skinning: Linear Blending

- Basic idea
  - Record vertex position in the closest solids
  - Apply a weighted sum

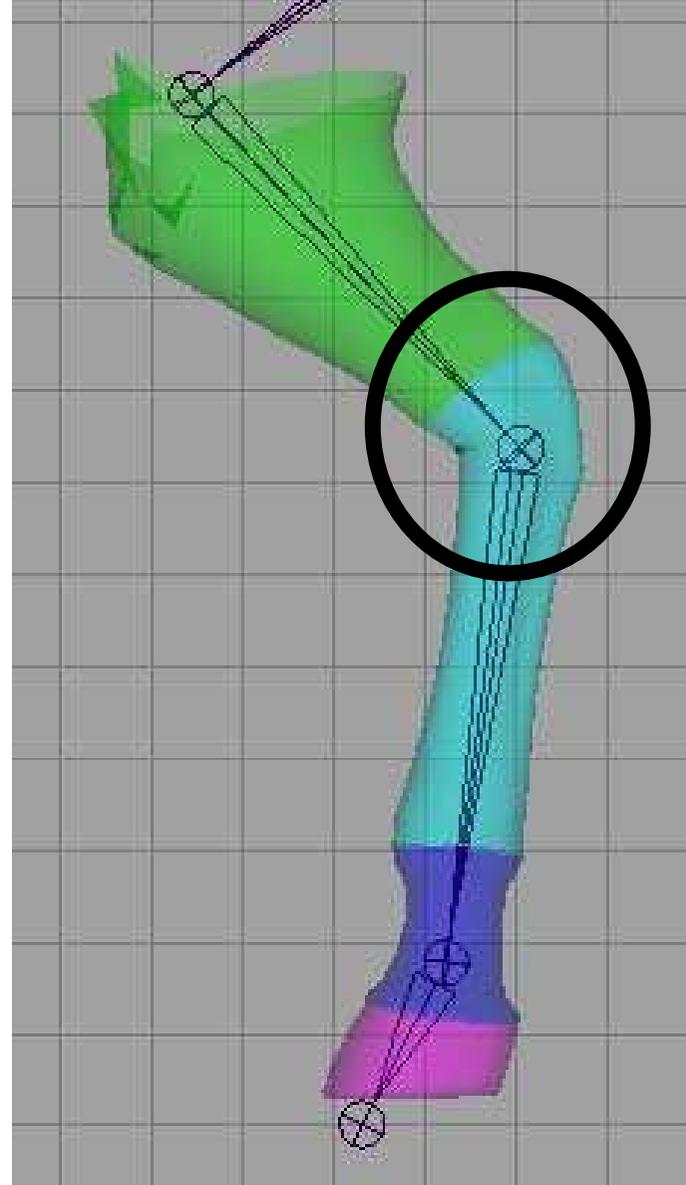
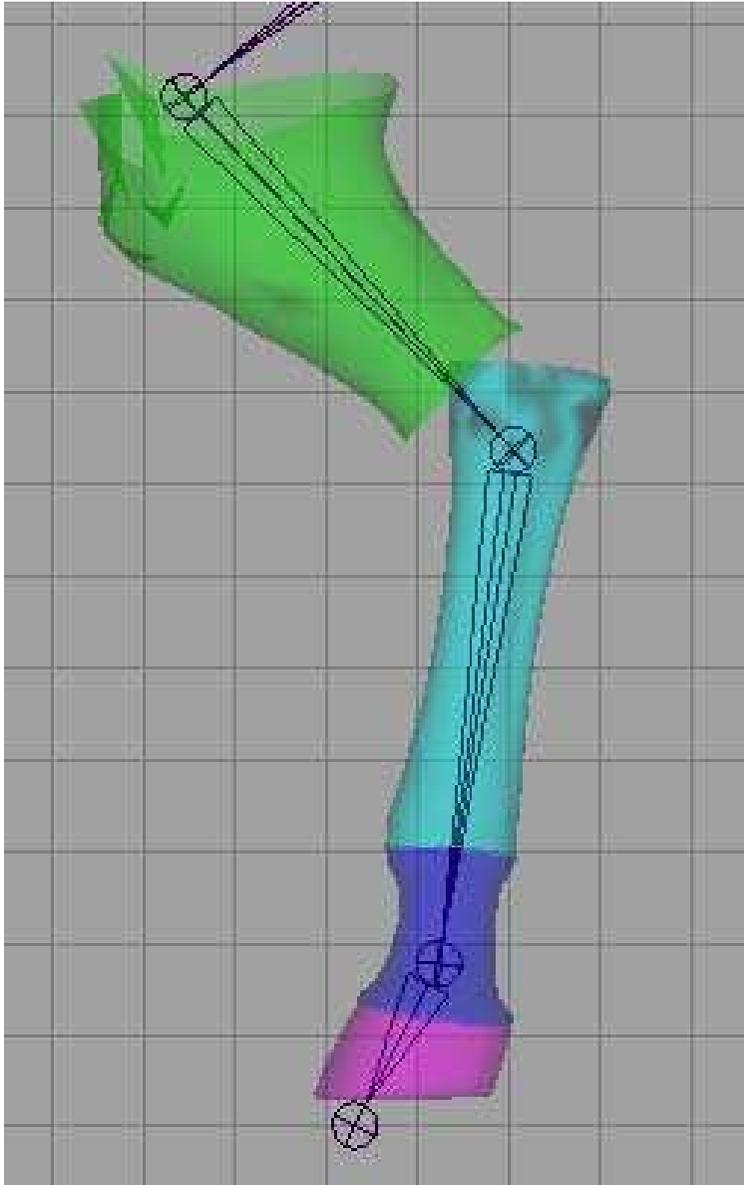


- Difficulties
  - Which solids to use?
  - Which weights?
  - Chosen by artist

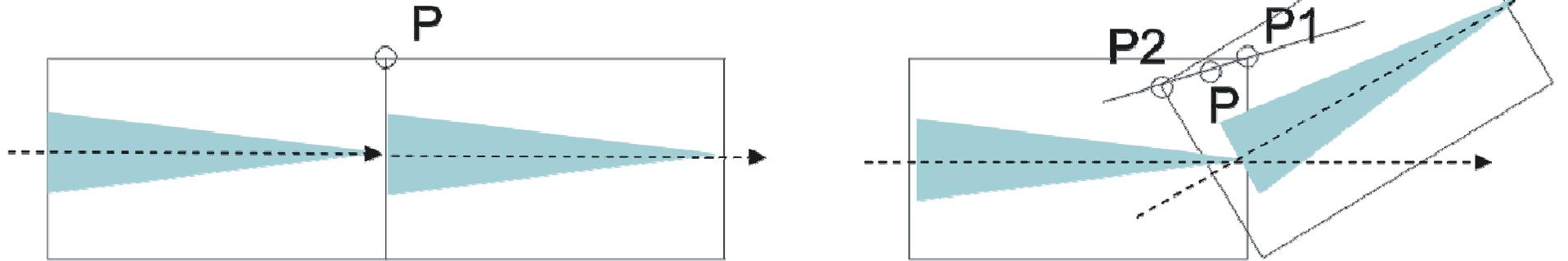
# Skinning: Example



# Skinning: Example

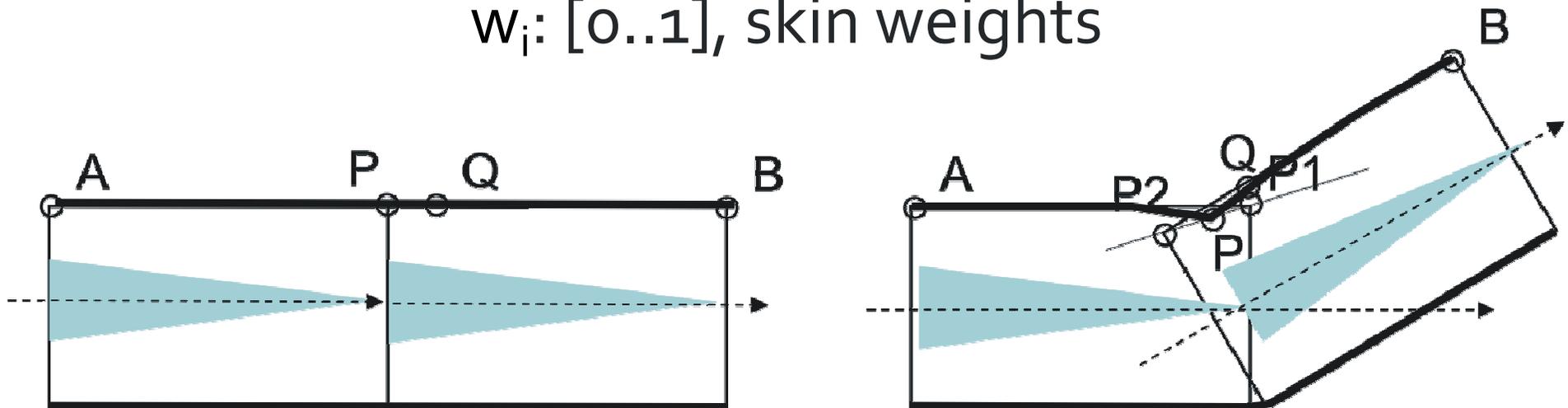


# Skinning: Linear Blending



$$\mathbf{P} = w_1 * \mathbf{P}_1 + w_2 * \mathbf{P}_2$$

$w_i: [0..1]$ , skin weights



# Skeletal Subspace Deformation

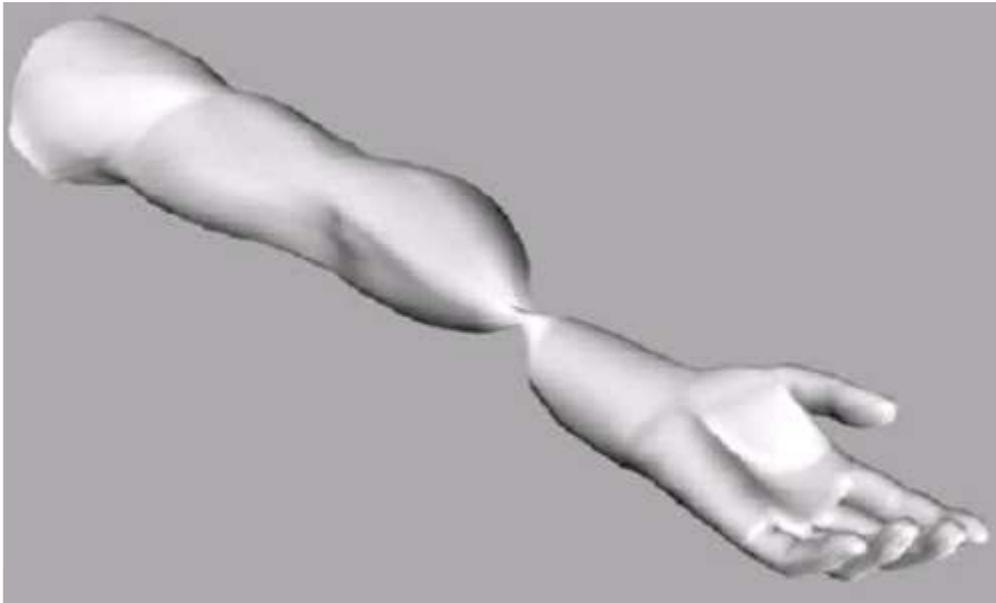
- Define skin geometry around skeleton in rest pose
- For each vertex
  - Figure out weights for each bone
    - based on distance
    - painted on by artist
  - Weights sum to 1
  - New position is weighted average of positions indicated by nearby bones

# Controlling SSD's

- Note: rigid parts, will want to have all but one weight equal to zero
  - “Skin” moves rigidly with bone
- Flexible parts near joints
  - Smoothly change weights from emphasizing one bone to the other
  - Skin will stay smooth as skeleton moves

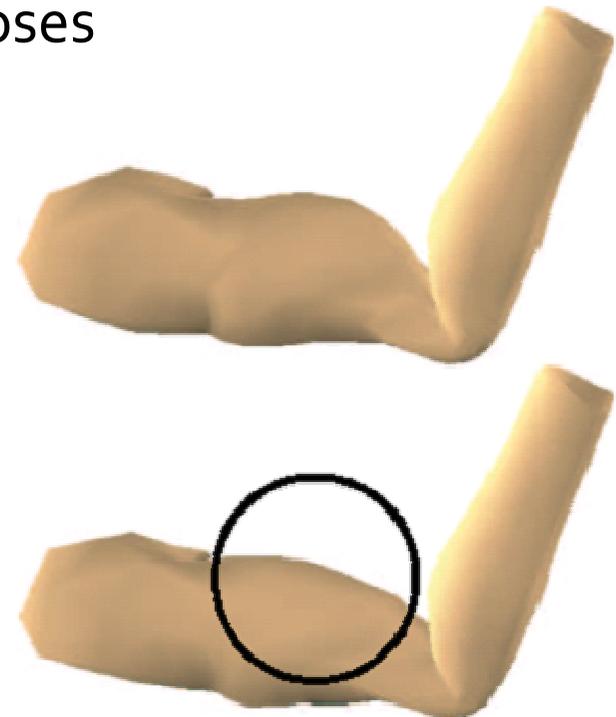
# SSD Problems

- Joint pinching
  - Large rotations at a joint
  - Skin deflating
  - Folding over itself, ...



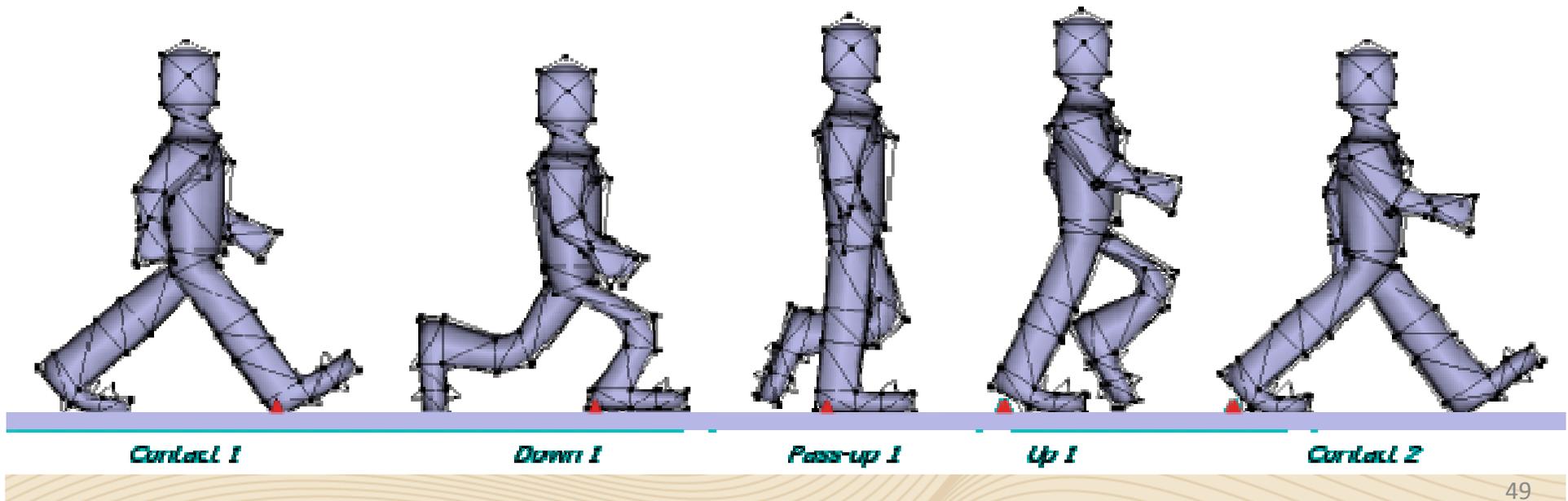
# SSD Problems

- Missing effect of underlying anatomy
  - Muscles bulging, wrinkles, ...
- Advanced solutions
  - Interpolate from several example poses
  - Simulate volumetric deformation
    - Masses and springs
  - ...



# Skeleton Posing Process

1. Specify DOF values for skeleton in animation system
2. Traverse through the hierarchy starting at the root down to the leaves (forward kinematics) and compute the world matrices
3. Use world matrices to deform skin & render



# Animation

## Programming Practice



# Animation Process: Programmers View

```
while(not finished) {  
    //each frame once  
    moveEverythingALittleBit();  
    drawEverything();  
}
```

# Ogre Animation File Format

```
<mesh> <!-- Ninja.mesh -->
...
<skeletonlink name="ninja.skeleton" />
<boneassignments>
  <vertexboneassignment vertexindex="0"
    boneindex="27" weight="1" />
  ...
</boneassignments>
</mesh>
```

# Ogre Animation File Format

```
<skeleton> <!-- Ninja.skeleton -->
  <bones>
    <bone id="0" name="Joint1">
      <position x="0" y="0.02" z="0" />
      <rotation angle="0">
        <axis x="1" y="0" z="0" />
      </rotation>
    </bone>
    ...
  </bones>
  ...
```

# Ogre Animation File Format

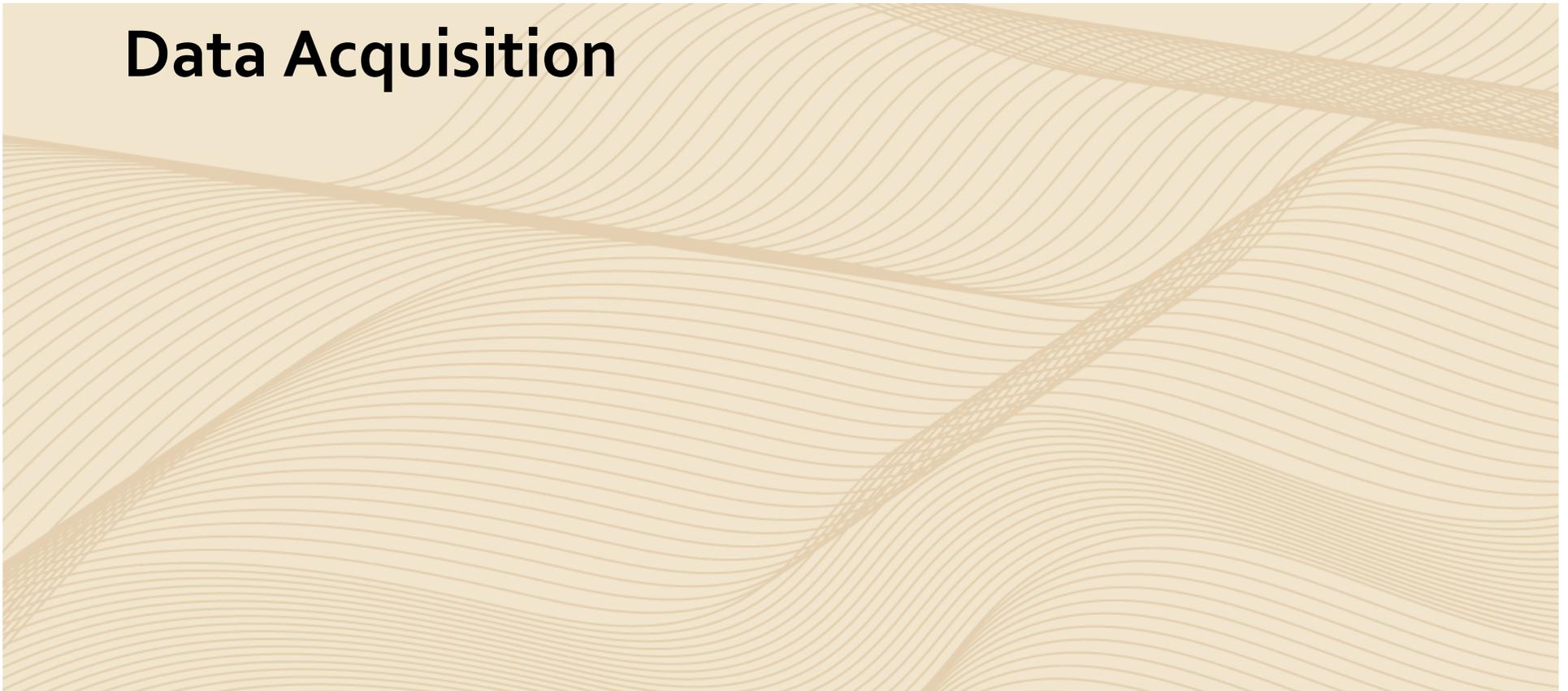
```
<skeleton> <!-- Ninja.skeleton -->
...
<bonehierarchy>
  <boneparent bone="Joint2" parent="Joint1" />
  <boneparent bone="Joint23" parent="Joint2" />
  ...
</bonehierarchy>
...
```

# Ogre Animation File Format

```
...
<animations>
  <animation name="Jump" length="0.46">
    <tracks>
      <track bone="Joint1">
        <keyframes>
          <keyframe time="0">
            <translate x="0" y="-0.67" z="0" />
            <rotate angle="0.08">
              <axis x="0" y="-1" z="0" />
            </rotate>
          </keyframe>
          ...
        </track>
```

# Animation

## Data Acquisition



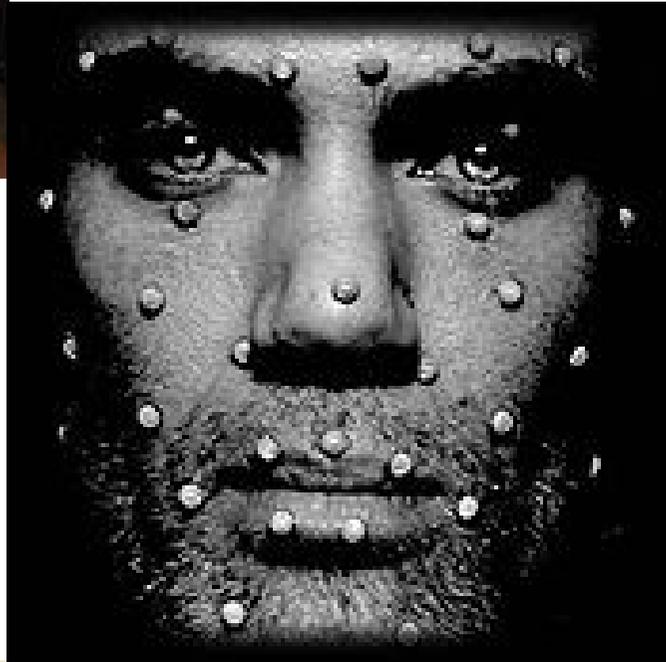
# Motion Capture

- Human motion very subtle
  - E.g. shifting balance, complex joints, personality...
- Motion capture (mocap) records real motion from actors
  - E.g. Gollum, Polar Express, Beowulf, a lot of TV shows, plenty of games
- Technical difficulties:
  - How do you record?
  - What do you do with the data?

# Mocap Methods

- Most common: “marker-based”
  - E.g. draw dots on the actor’s face, or dress in black and attach retro-reflective balls in key places
  - Film from one or more cameras (preferably calibrated and synchronized, preferably with a strobe light)
  - Reconstruct 3D positions of markers in each frame through inverse solve
- Some “markerless” systems: rely on good computer vision algorithms
- Some use direct or electromagnetic measurement

# Motion Capture



# Move trees

- Standard videogame solution
- Design a graph corresponding to available player actions
  - E.g. walk forward, turn, jump, ...
- Design and record corresponding actions with mocap
- Warp/retime/edit to make clips easily transition where needed
- Note: in playback need to keep separate track of global position/orientation

# Morphing

- Closely related family of effects
- Warp two images or models to roughly match each other's geometry
  - Often based on artist-selected features
  - Modern computer vision and/or geometry algorithms getting better at automatically finding matches

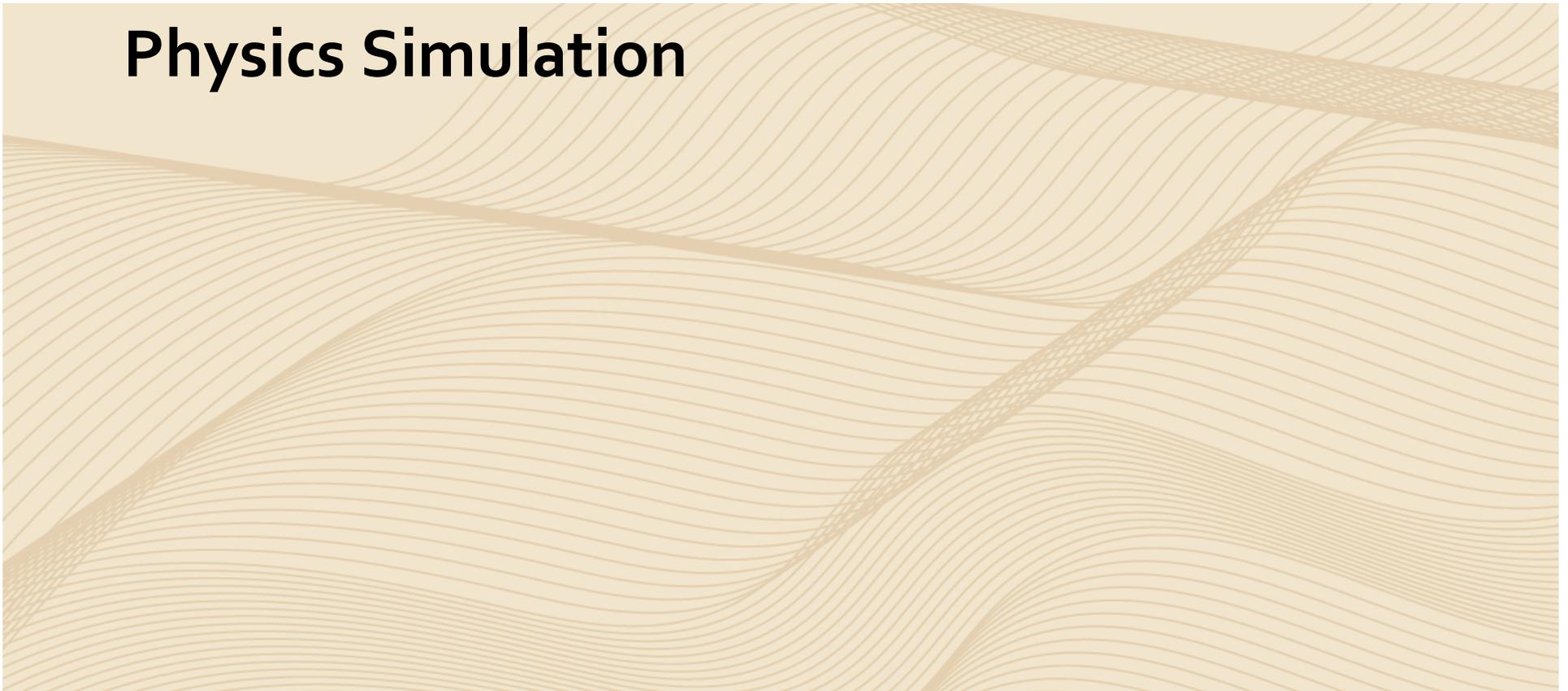


# Morphing

- Closely related family of effects
- Warp two images or models to roughly match each other's geometry
  - Often based on artist-selected features
  - Modern computer vision and/or geometry algorithms getting better at automatically finding matches
- Cross-fade between the two to get in-between frames
  - For images, just average pixels
  - For 3D geometry, helps to have a common parameterization...

# Animation

## Physics Simulation

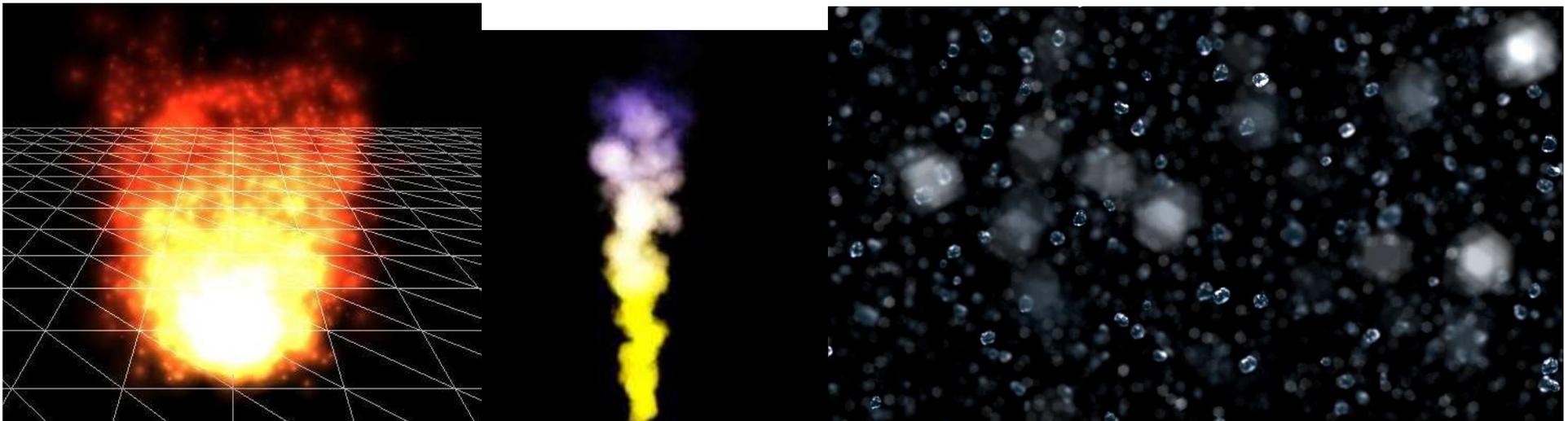


# Physics Simulation

- Particles
- Rigid bodies
  - Collisions, contact, stacking, rolling, sliding
- Articulated bodies
  - Hinges, constraints
- Deformable bodies (solid mechanics)
  - Elasticity, plasticity, viscosity
  - Fracture
  - Cloth
- Fluid dynamics
  - Fluid flow (liquids & gasses)
  - Combustion (fire, smoke, explosions...)
  - Phase changes (melting, freezing, boiling...)
- Vehicle dynamics
  - Cars, boats, airplanes, helicopters, motorcycles...
- Character dynamics
  - Body motion, skin & muscle, hair, clothing

# Particle Systems

- For fuzzily defined phenomena
- Highly complex motion
- Break up complex phenomena into many component parts - particles
  - E.g. fire into tiny flames
- Instead of animating each part by hand, provide rules and overall guidance for computer to construct animation



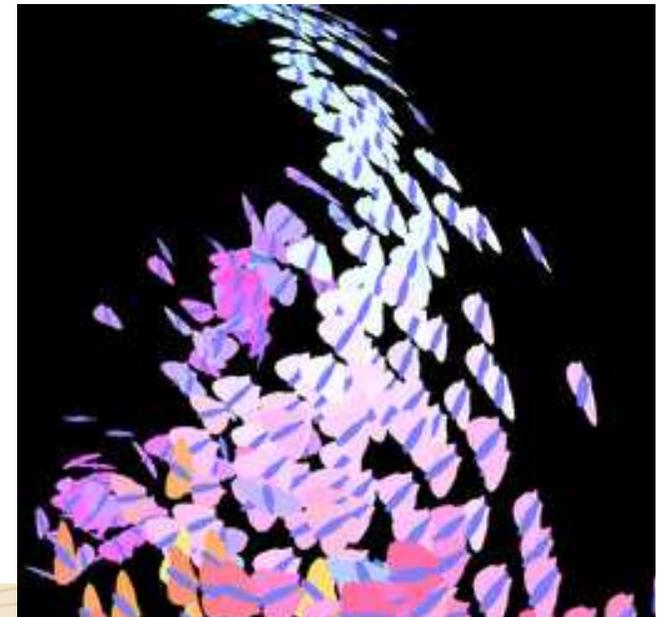
# Particle Systems

- Dust, sparks, fireworks, leaves, flocks, water spray...
- Also phenomena with many DOF:  
fluids (water, mud, smoke, ...), fire, explosions, hair,  
fur, grass, clothing, ...
- Three things to consider:
  - When and where particles start/end
  - The rules that govern motion (and additional attached variables, e.g. color)
  - How to render the particles



# What is a Particle?

- Most basic particle only has a position
- Usually add other attributes, such as:
  - Age
  - Colour
  - Radius
  - Orientation
  - Velocity  $v$
  - Mass  $m$
  - Temperature
  - Type
- The sky is the limit
  - e.g. AI models of agent behaviour
  - e.x.: flocking Behaviour



# Particle Seeding

- Need to add (or seed) particles to the scene
- Where?
  - Randomly within a shaped volume or on a surface
    - Uniform, jittered grid, ...
  - At a point (maybe another particle)
  - Where there aren't many particles currently
- When?
  - At the start
  - Several per frame
  - When there aren't enough particles somewhere
- Need to figure out other attributes, not just position
  - E.g. velocity pointing outwards in an explosion

# Basic Animation

- Specify a velocity field  $v(x,t)$  for any point in space  $x$ , any time  $t$
- Break time into steps
  - E.g. per frame  $\Delta t = (1/\text{fps})\text{th}$  of a second
  - Or several steps per frame
- Change each particle's position  $x_i$  by “integrating” over the time step (Forward Euler)

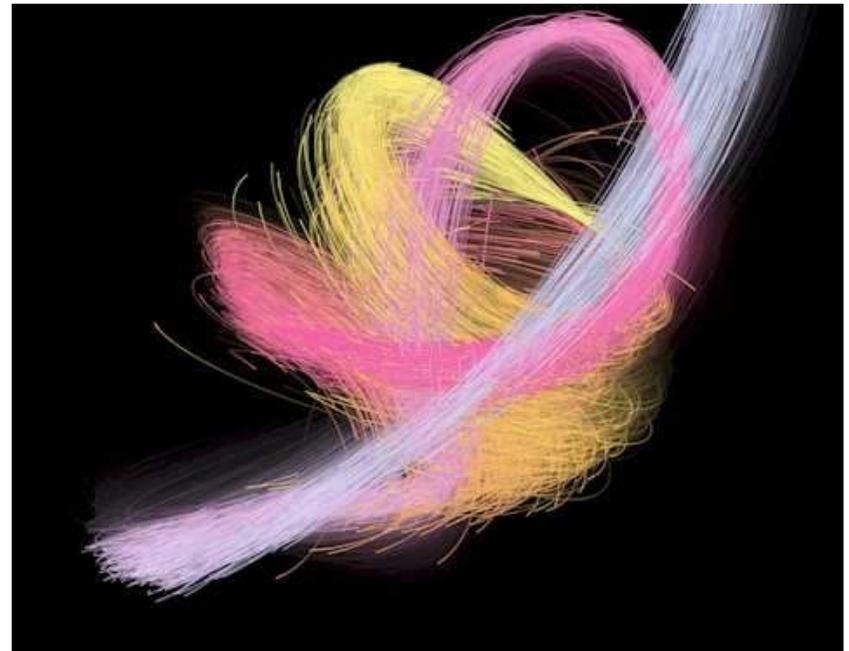
$$x_i^{new} = x_i + \Delta t v(x_i, t)$$

# Basic Rendering

- Draw a dot for each particle
- But what do you do with several particles per pixel?
  - No special handling
  - Add: models each point emitting (but not absorbing) light -- good for sparks, fire, ...
  - Compute depth order, do alpha-compositing (and worry about shadows etc.)
- Anti-aliasing
  - Blur edges of particle, make sure blurred to cover at least a pixel
- Particle with radius: kernel function

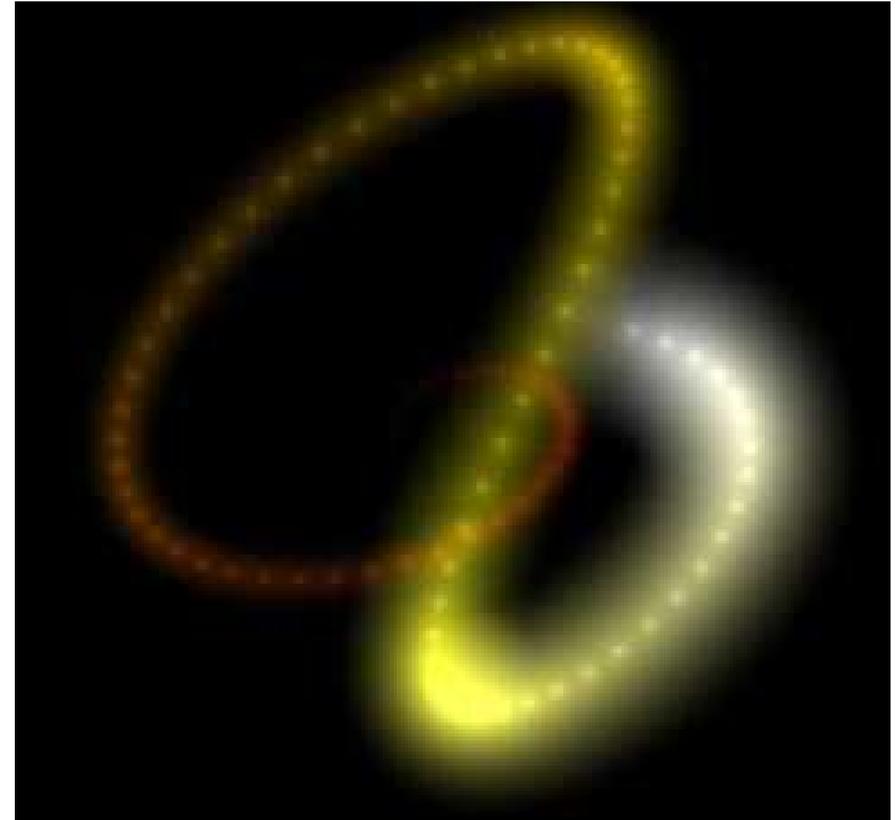
# Motion blur

- One case where you can actually do exact solution instead of sampling
- Really easy for simple particles
  - Instead of a dot, draw a line  
(from old position to new position - the shutter time)



# Motion blur

- May involve decrease in alpha
- More accurately, draw a spline curve
- May need to take into account radius as well...



# More Detailed Particle Rendering

- Stick a texture (or even a little movie) on each particle: “sprites” or “billboards”
  - E.g. a noise function
  - E.g. a video of real flames



# More Detailed Particle Rendering

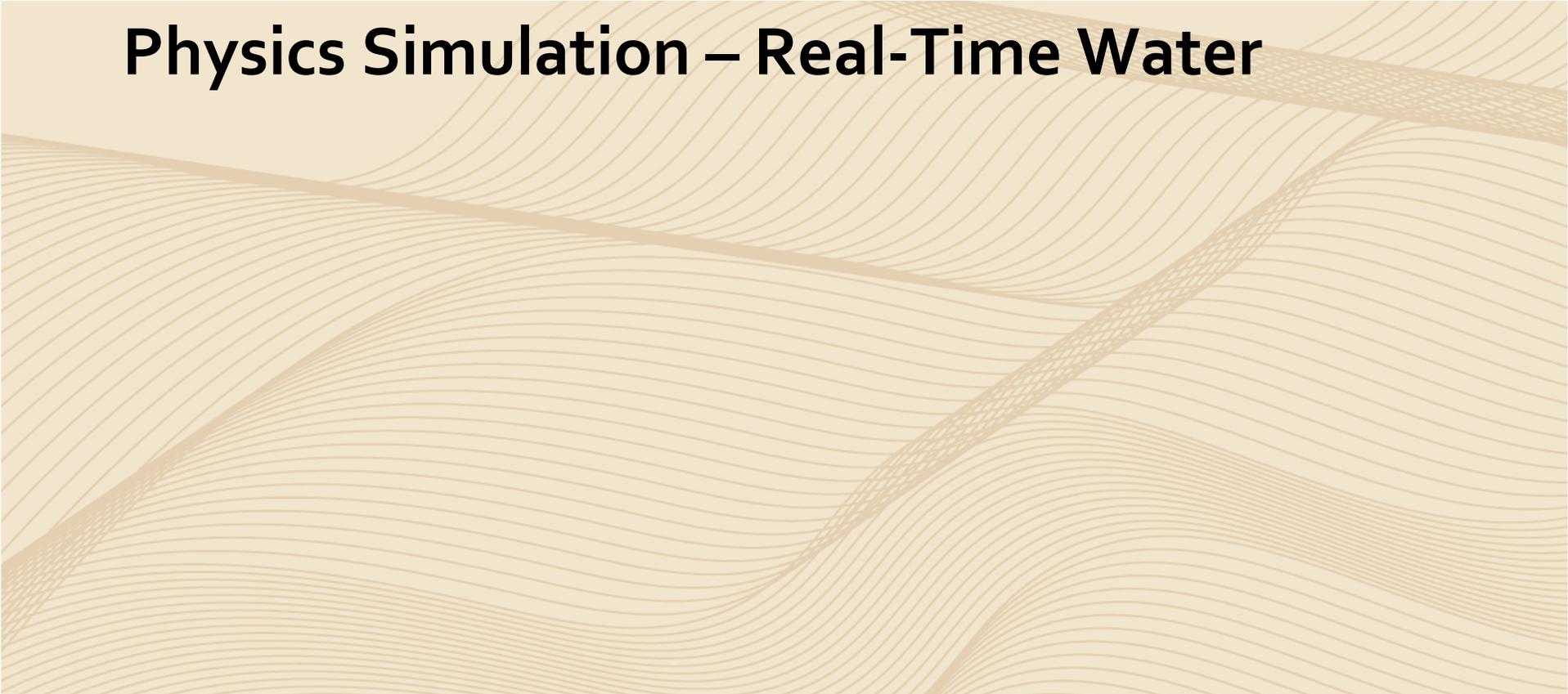
- Stick a texture (or even a little movie) on each particle: “sprites” or “billboards”
  - E.g. a noise function
  - E.g. a video of real flames
- Draw a little object for each particle
  - Need to keep track of orientation as well, unless spherical
- Draw between particles
  - curve (hair), surface (cloth)
- Implicit surface wrapped around virtual particles (e.g. water)

# Physics Simulation

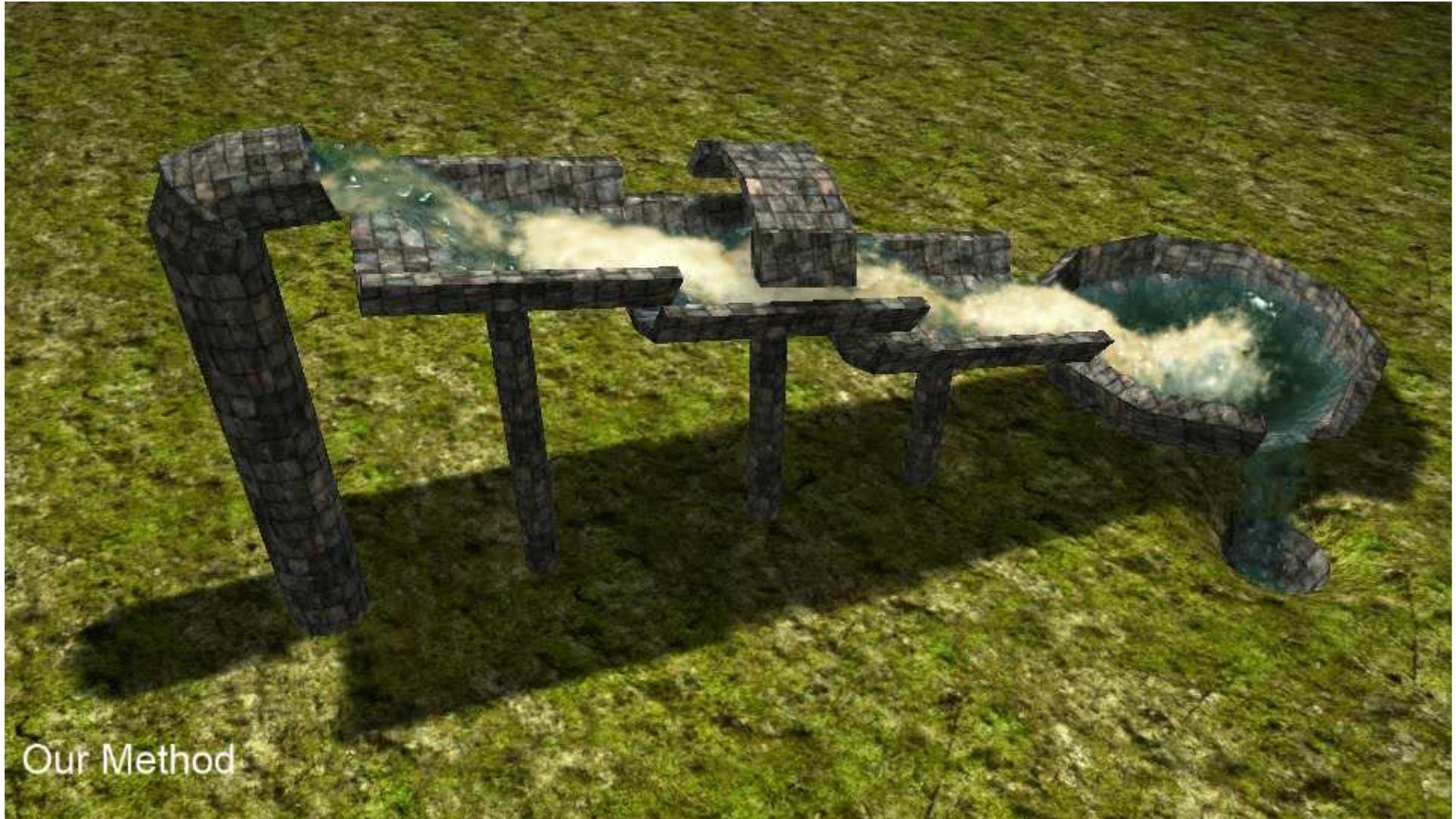


# Animation

**Physics Simulation – Real-Time Water**



# Motivation



Our Method

# SPH Simulation Data

- SPH = Smoothed Particle Hydrodynamics
- Numeric method to solve hydrodynamic equations
- Non-sorted 3D point cloud
- Fluid is able to flow everywhere
- Difficult to extract surface for rendering
- Available in PhysX

# Direct Rendering of SPH Simulation Data



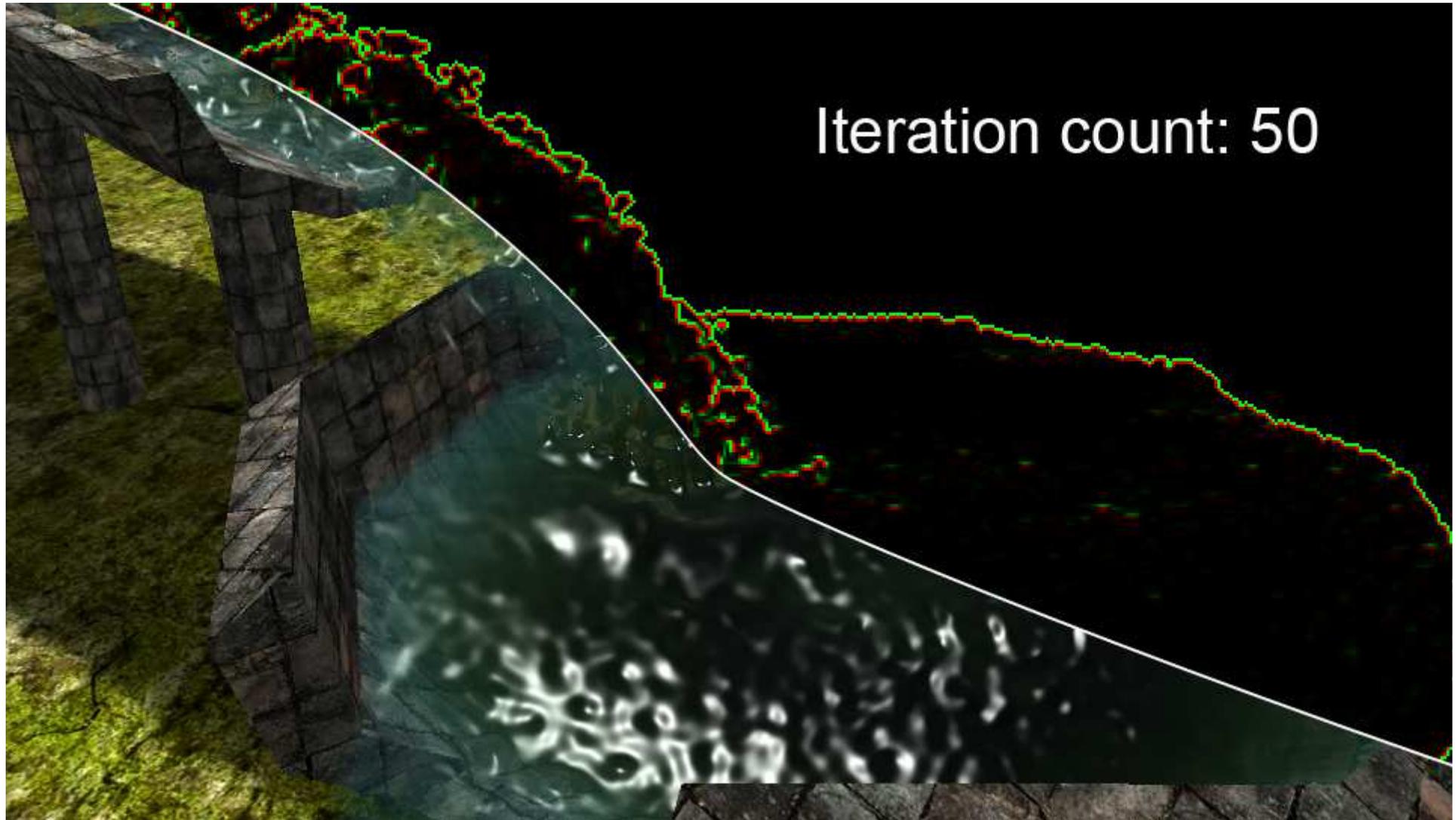
# Approaches

- Screen space fluid rendering with curvature flow.
  - van der Laan et al. [vdLGS09]
  - Thickness based rendering
  - Screen-space curvature flow filtering
- Simulation of two-phase flow with sub-scale droplet and bubble effects.
  - Mihalef et al. [MMS09]
  - Weber number thresholding
- A Layered Particle-Based Fluid Model for Real-Time Rendering of Water
  - Builds on [vdLGS09]
  - View dependent filtering
  - Volumetric Foam

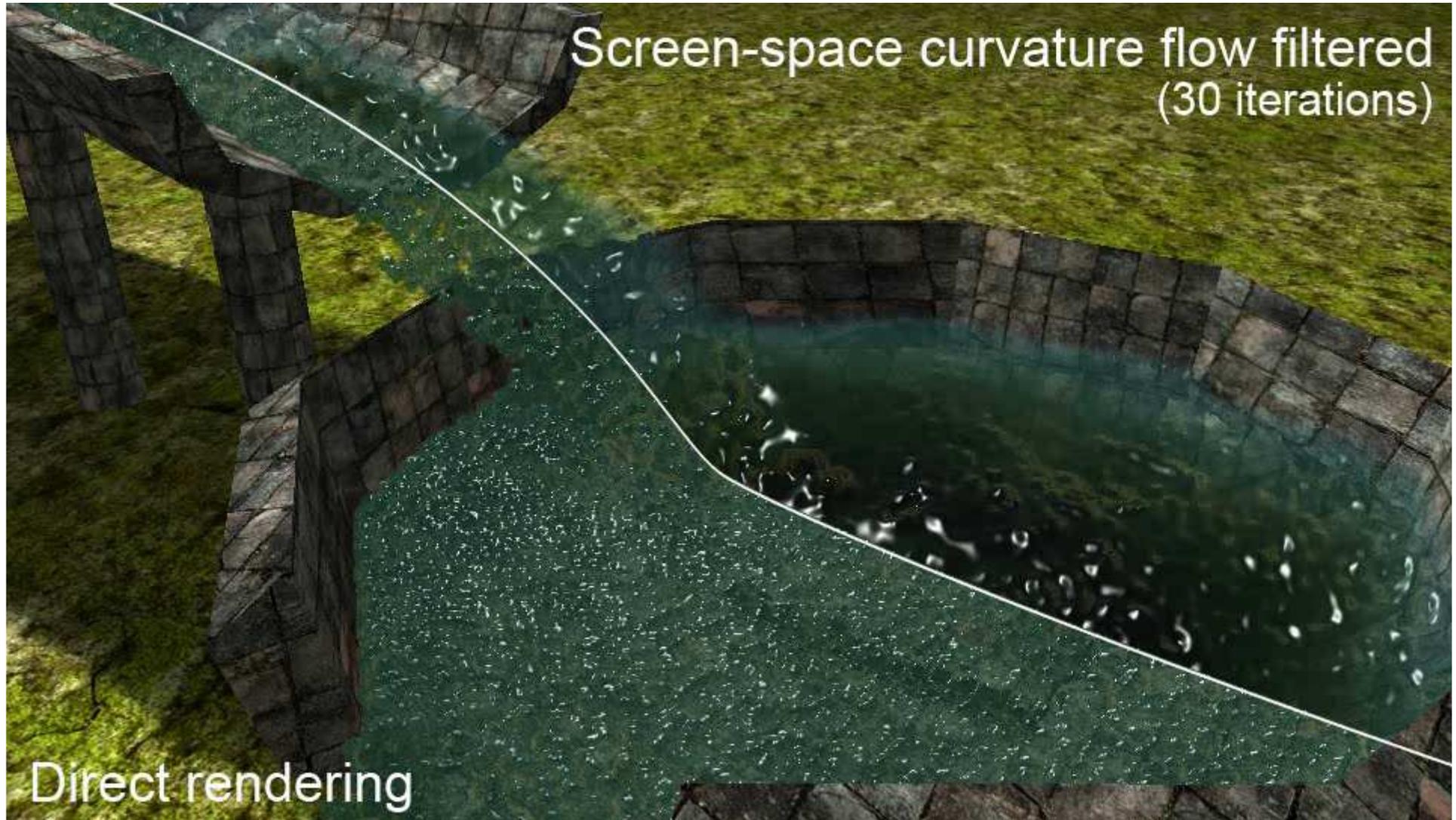
# Thickness Based Rendering



# How to smooth the surface?



# Screen Space Curvature Flow



# Smoothing Artefacts



# Adaptive Curvature Flow

- Interpret each integration step as a filtering step with a  $3 \times 3$  kernel in view space
- Vary number of iterations depending on the view space distance  $z$

# Improved Filtering

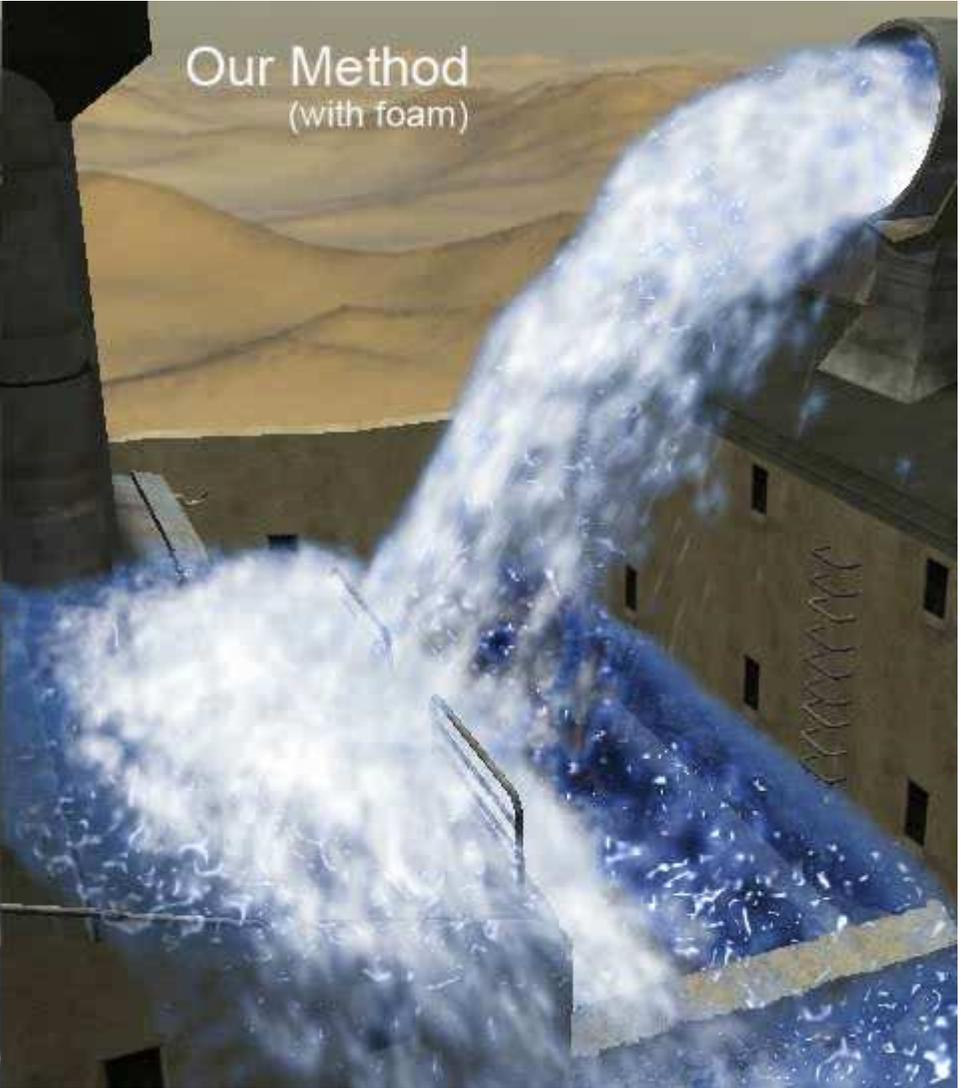


# Real-Time Foam

Screen Space Curvature Flow  
(30 iterations)



Our Method  
(with foam)



# Definitions

- Foam: trapped air bubbles in the liquid
- Two main effects in real-time
  - Spray or bubbles onto the water surface
  - Foam that occurs behind a water surface

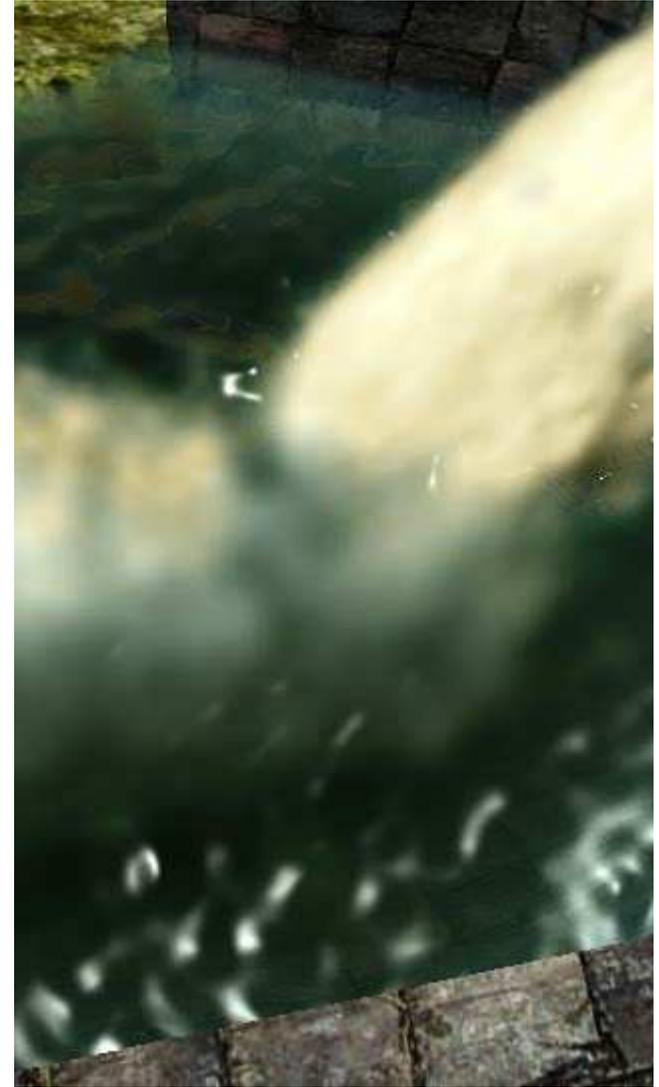
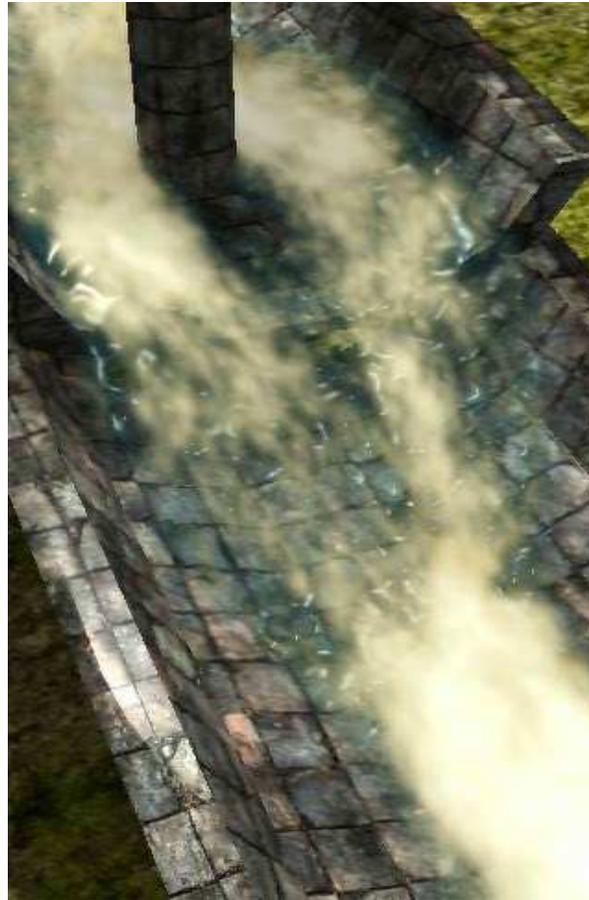
# Foam Formation

- Foam formation
  - Based on Weber number thresholding
  - Physical formula used in off-line systems
  - Classify particles as water or foam

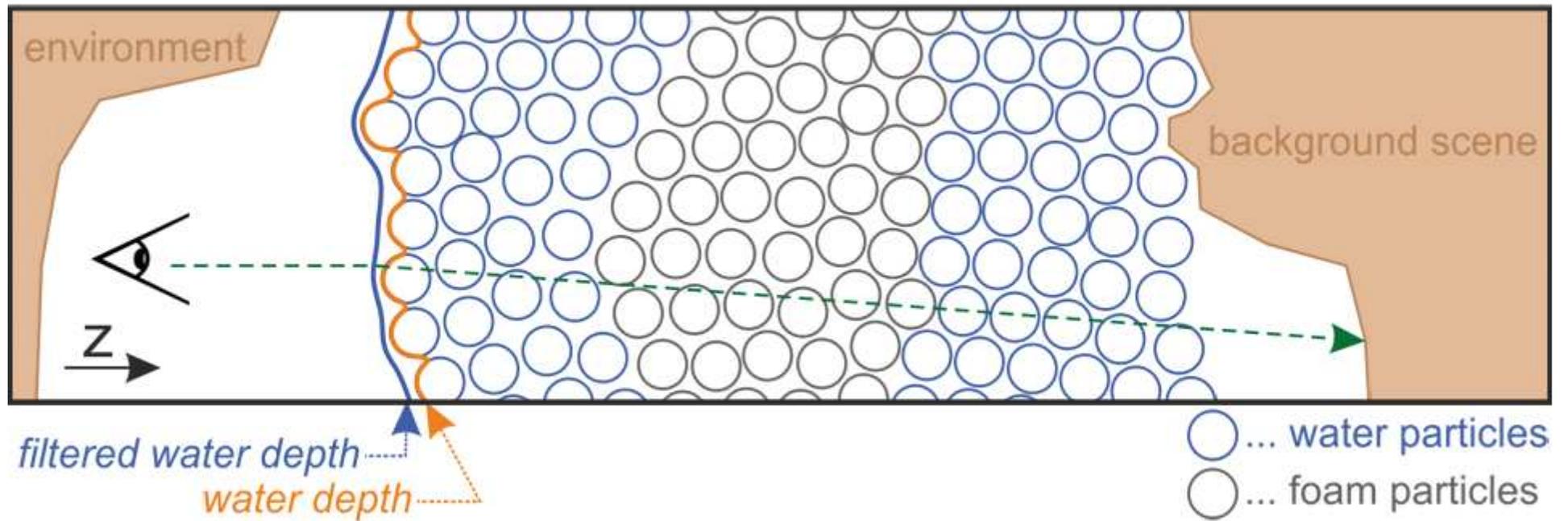
# Weber Number Threshold



# Rendering of Foam



# Scene Configuration and View Ray



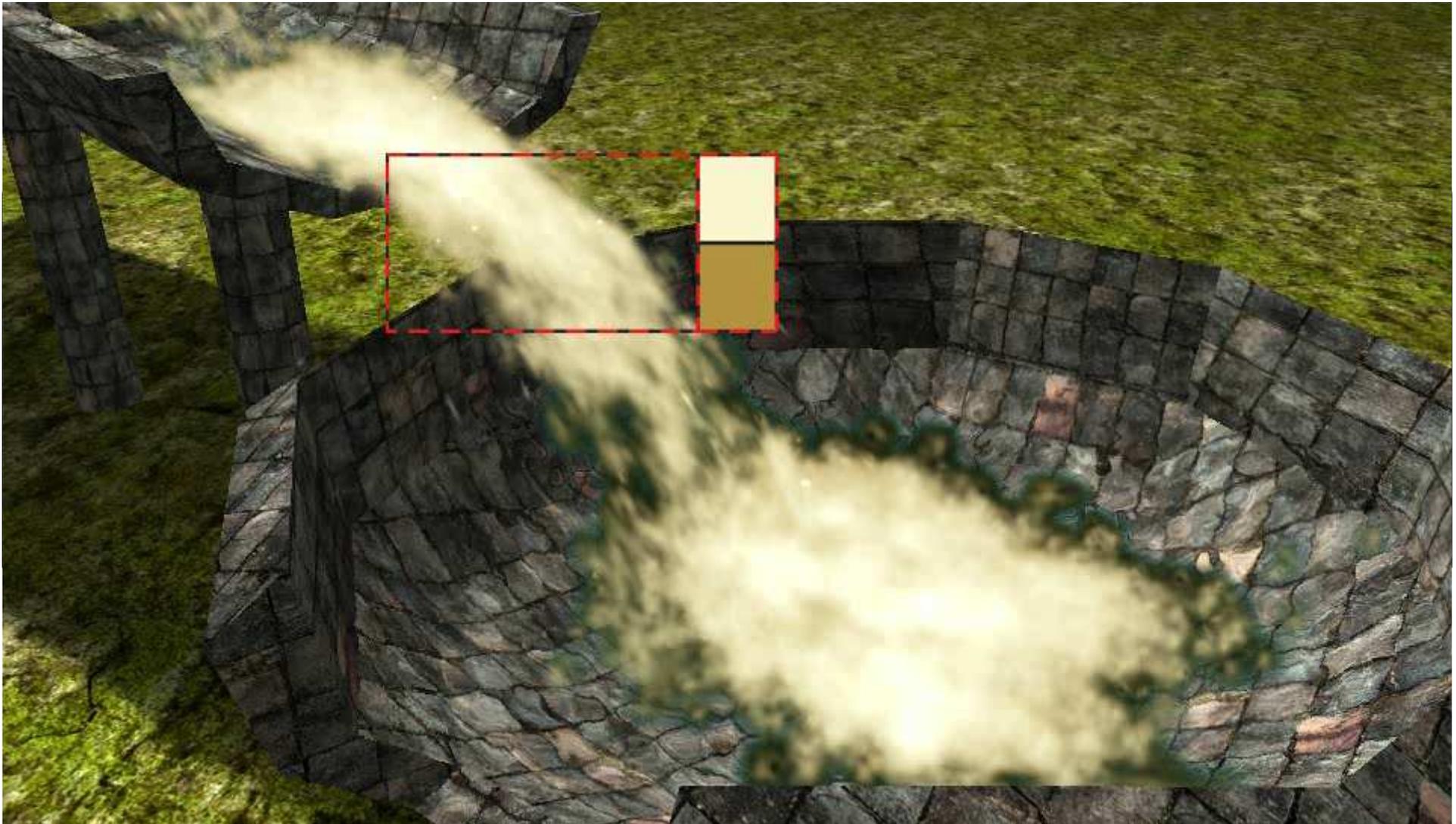
# Background Scene



# Back Water Layer



# Foam Layer



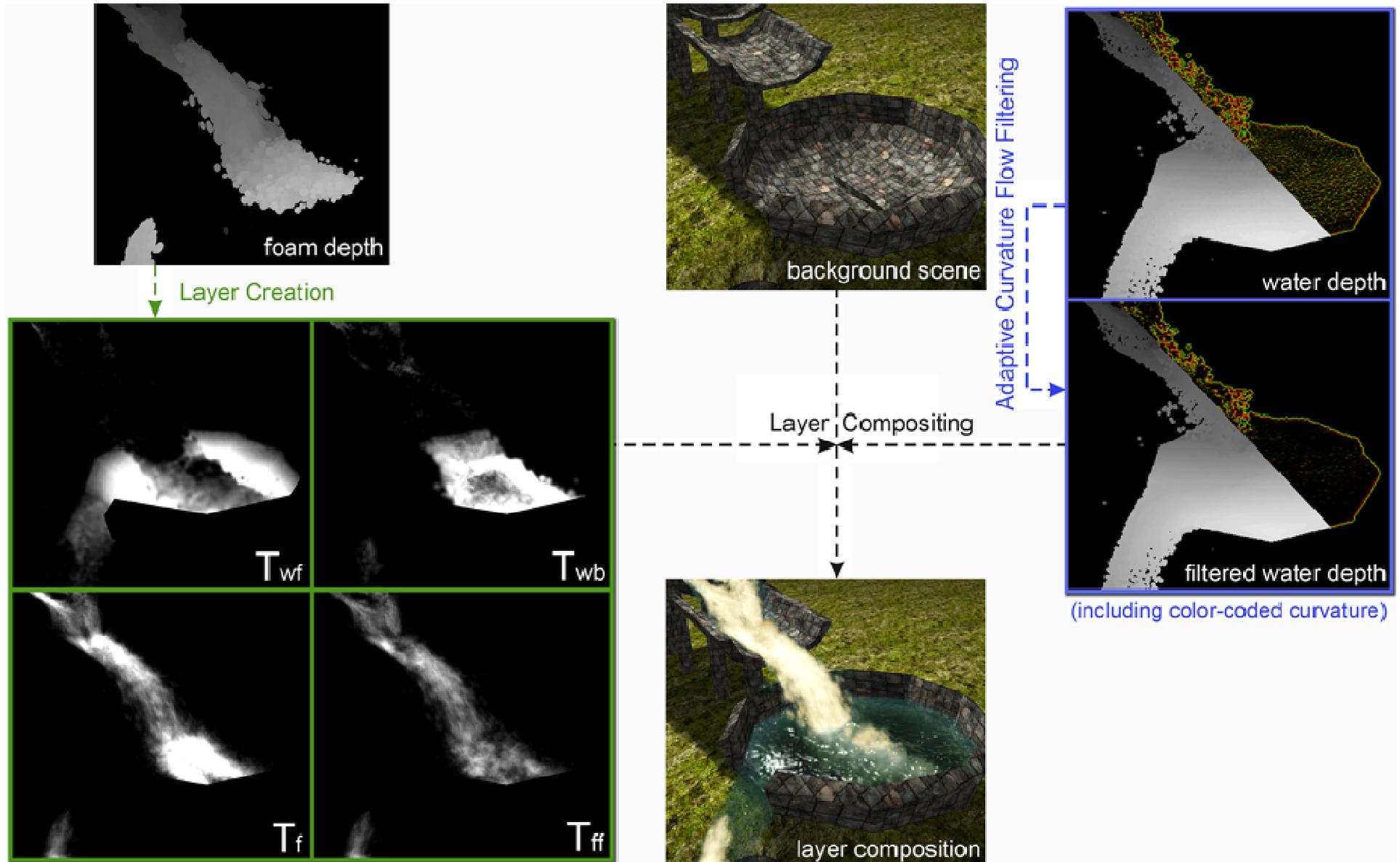
# Front Water Layer



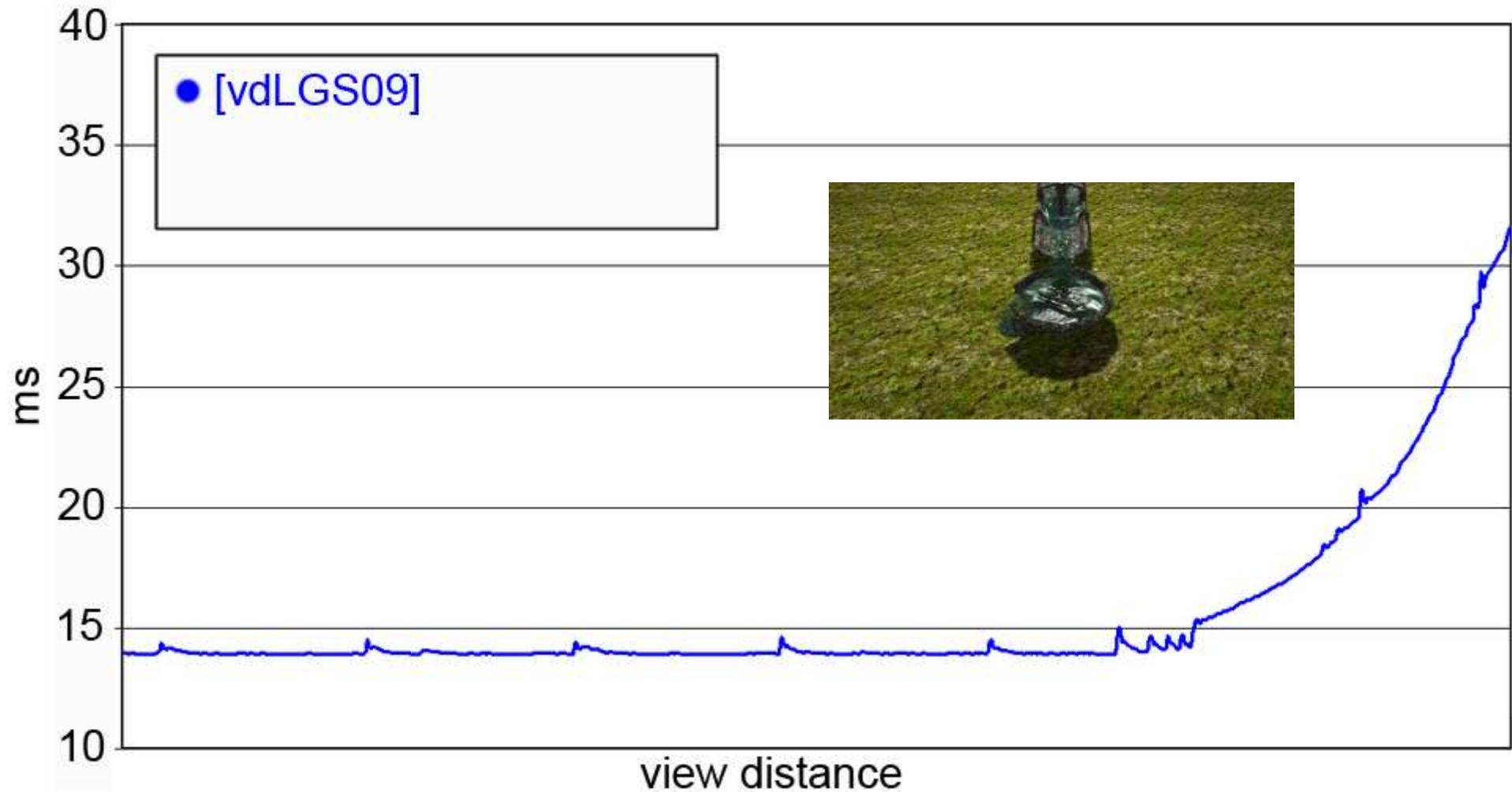
# Reflection and Specular Highlights



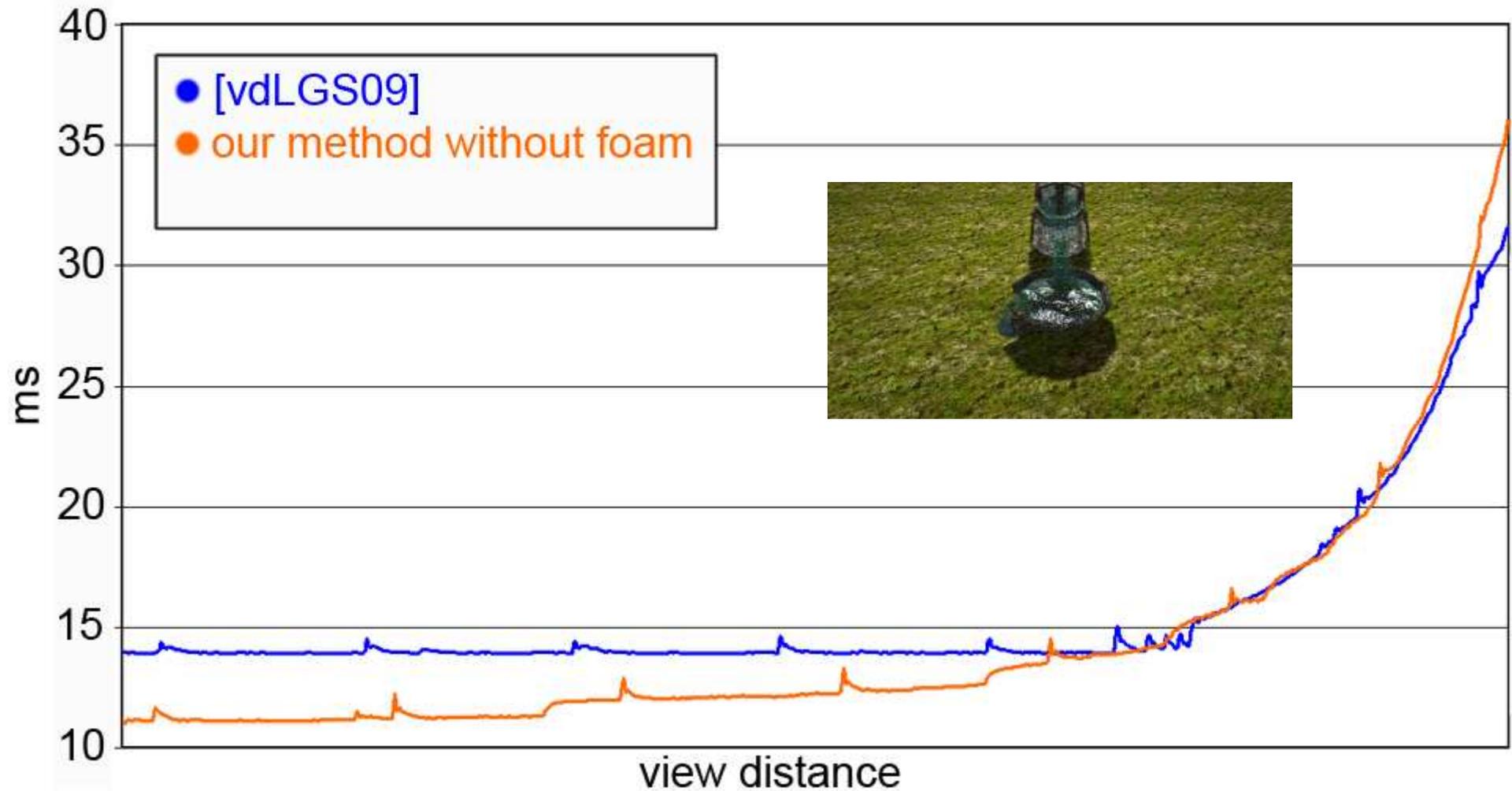
# Algorithm Summary



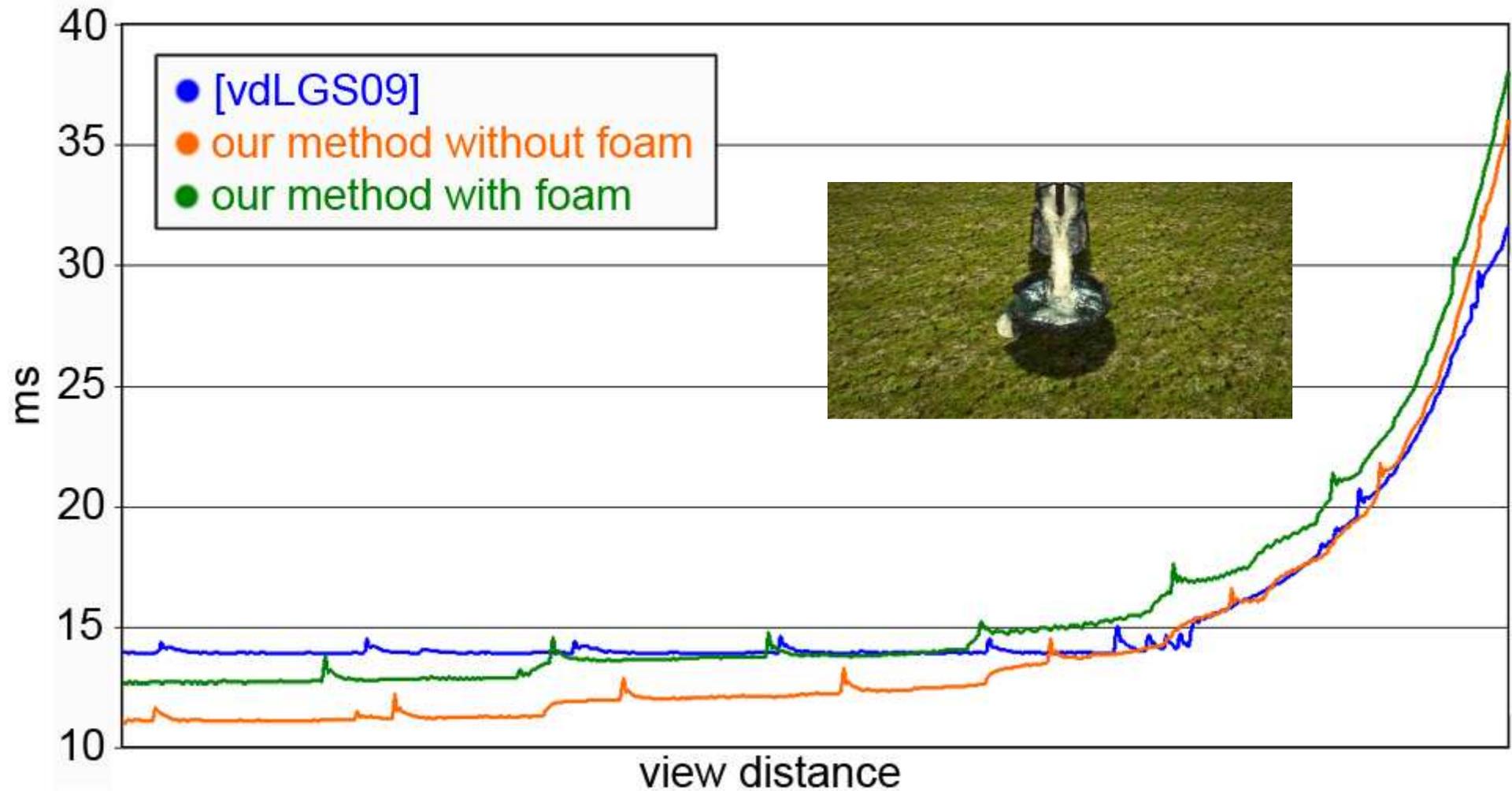
# Performance Comparison



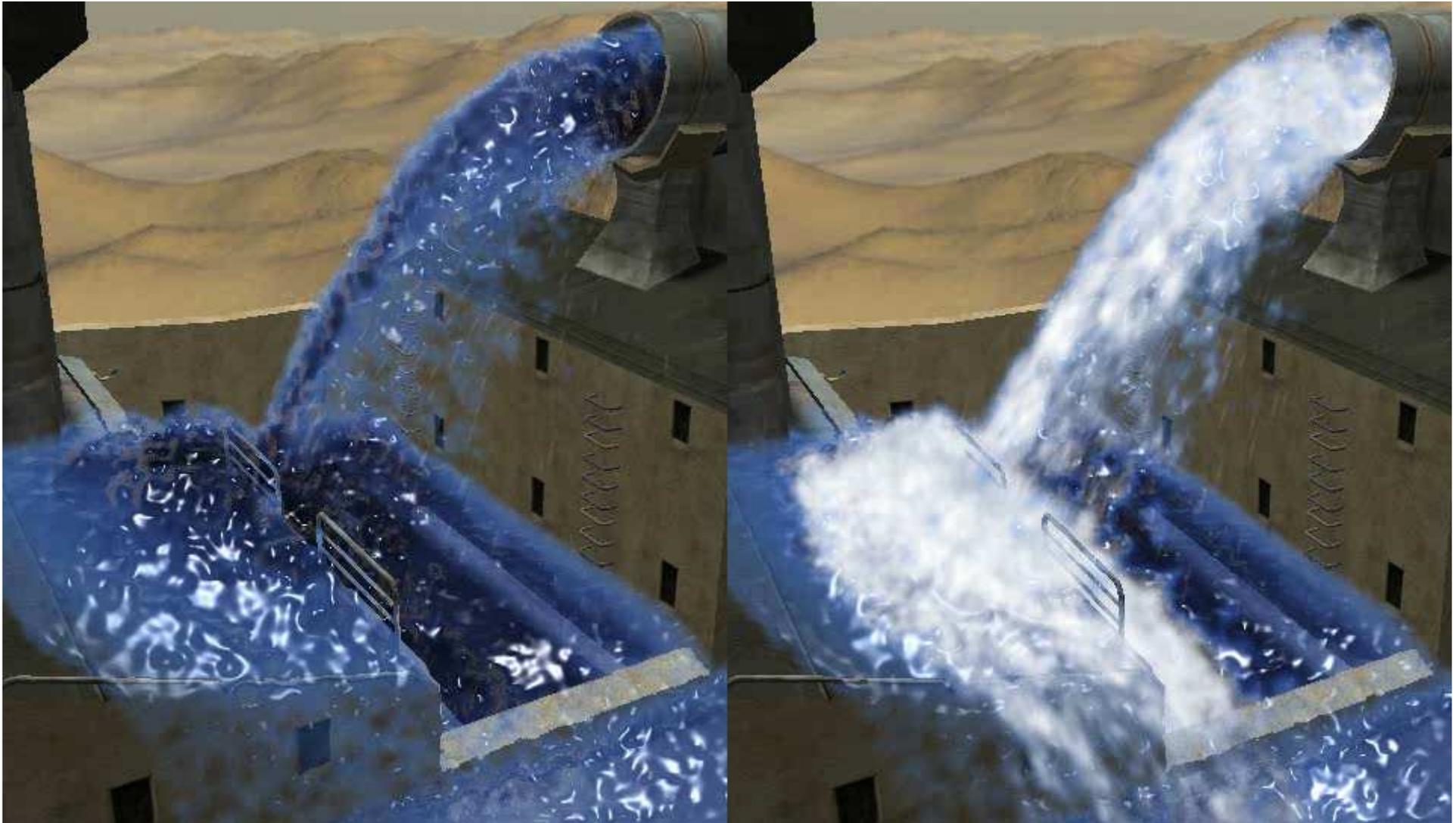
# Without Foam



# Including Foam



# Comparison – w/o Foam – with Foam



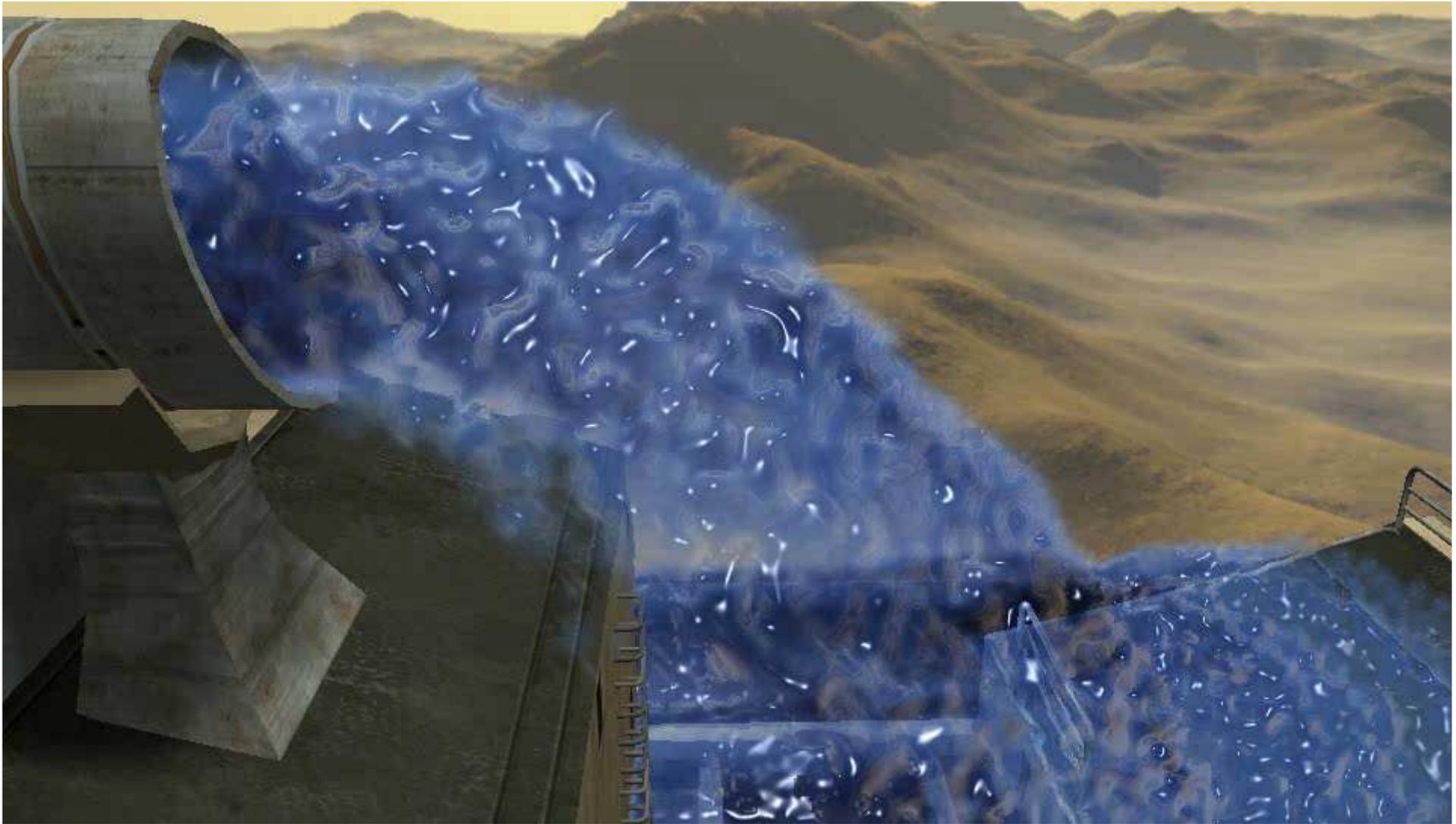
# Dynamic Scenes



# Ground Truth



# Limitation



# Conclusion

- Rendering particle-based fluids with volumetric foam in real time
- Adaptive curvature flow smoothing
- Physically guided foam rendering
- Layered compositing